

Received 06/04/17

Fibonacci Sequence and Running Expressions with Equalities - I

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Abstract

In previous work [12], running inequalities are written in terms of 1 to 9 and 9 to 1 or 9 to 0 separated by single or double equality signs. Each digits is used with basic operations, along with **factorial** and **square-root**. These types of equalities, we called as **running expressions**. This work bring running expressions with double and triple equality signs using **Fibonacci sequence** numbers along with basic operations. The work is up to 3 digits in increasing and decreasing orders. For 4 digits onwards the results are given in second part [21].

I N D E X

The work is divided in following sections and subsections:

- 1 Introduction;**
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 - 1.2 Flexible Power Representations;**
 - 1.3 Pyramidal-Type Representations;**
 - 1.4 Single Digit Representations;**
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- 2 Running Expressions with Fibonacci Sequence;**
 - 2.1 Fibonacci Sequence;**
 - 2.2 Double Equalities;**
- 3 Single Equality Expressions;**
 - 3.1 Increasing Order;**
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1 Introduction

Before starting the work, below are some representations of numbers in different situations done by author [18, 19]. The work is for 9 digits from 1 to 9 in increasing case and 9 or 10 digits, i.e., from 9 to 1 or 9 to 0 in the decreasing case. In some cases, the results are symmetric and are uses all the 10 digits, i.e., from 0 to 9.

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1.1 Crazy Representations of Natural Numbers

In 2014, author [9] wrote natural numbers in increasing and decreasing orders of 1 to 9 and 9 to 1. See examples below:

$$\begin{aligned}
 100 &= 1 + 2 + 3 + 4 + 5 + 6 + 7 + 8 \times 9 = 9 \times 8 + 7 + 6 + 5 + 4 + 3 + 2 + 1. \\
 101 &= 1 + 2 + 34 + 5 + 6 \times 7 + 8 + 9 = 9 \times 8 + 7 + 6 + 5 + 4 + 3 \times 2 + 1. \\
 102 &= 12 + 3 \times 4 \times 5 + 6 + 7 + 8 + 9 = 9 + 8 + 7 + 6 + 5 + 4^3 + 2 + 1. \\
 103 &= 1 \times 2 \times 34 + 5 + 6 + 7 + 8 + 9 = 9 + 8 + 7 \times 6 + 5 \times 4 + 3 + 21. \\
 104 &= 1 + 23 + 4 + 5 + 6 + 7 \times 8 + 9 = 9 + 8 + 7 + 65 + 4 \times 3 + 2 + 1. \\
 105 &= 1 + 2 \times 3 \times 4 + 56 + 7 + 8 + 9 = 9 + 8 \times 7 + 6 \times 5 + 4 + 3 + 2 + 1. \\
 106 &= 12 + 3 + 4 \times 5 + 6 + 7 \times 8 + 9 = 9 + 8 \times 7 + 6 \times 5 + 4 + 3 \times 2 + 1. \\
 107 &= 1 \times 23 + 4 + 56 + 7 + 8 + 9 = 9 + 8 + 76 + 5 + 4 + 3 + 2 \times 1. \\
 108 &= 1 + 2 + 3 + 4 + 5 + 6 + 78 + 9 = 9 + 8 + 76 + 5 + 4 + 3 + 2 + 1.
 \end{aligned}$$

For comments on this work see [1, 2, 7, 8].

1.2 Flexible Power Representations

Instead working with increasing and decreasing cases separated, here we worked in such a way that the results are always symmetric. This we have done using all the 10 digits, i.e., from 0 to 9. The results obtained are symmetric, i.e., writing in 0 to 9 or 9 to 0, the resulting number is same. The idea used is in such a way that numbers are written in 0 to 9 with permutations of powers also used the same digits i.e., 0 to 9. See below some examples,

$$\begin{aligned}
 201 &:= 0^3 + 1^9 + 2^4 + 3^7 - 4^8 + 5^1 + 6^6 + 7^5 + 8^2 + 9^0. \\
 202 &:= 0^0 + 1^9 + 2^6 + 3^8 - 4^7 + 5^5 + 6^3 + 7^2 + 8^1 + 9^4. \\
 203 &:= 0^3 - 1^9 + 2^4 + 3^7 - 4^8 + 5^0 + 6^6 + 7^5 + 8^2 + 9^1. \\
 204 &:= 0^8 + 1^9 + 2^5 + 3^7 - 4^6 + 5^1 + 6^4 + 7^2 + 8^0 + 9^3. \\
 205 &:= 0^3 + 1^9 + 2^4 + 3^7 - 4^8 + 5^0 + 6^6 + 7^5 + 8^2 + 9^1. \\
 206 &:= 0^7 - 1^9 - 2^5 - 3^8 + 4^6 + 5^1 + 6^3 + 7^4 + 8^0 + 9^2. \\
 207 &:= 0^8 + 1^9 + 2^5 + 3^7 - 4^6 + 5^0 + 6^4 + 7^2 + 8^1 + 9^3. \\
 208 &:= 0^7 + 1^9 - 2^5 - 3^8 + 4^6 + 5^1 + 6^3 + 7^4 + 8^0 + 9^2. \\
 209 &:= 0^7 - 1^9 - 2^5 - 3^8 + 4^6 + 5^0 + 6^3 + 7^4 + 8^1 + 9^2. \\
 210 &:= 0^5 - 1^7 - 2^8 - 3^9 + 4^1 + 5^6 + 6^0 + 7^3 + 8^4 + 9^2. \\
 211 &:= 0^7 + 1^9 - 2^5 - 3^8 + 4^6 + 5^0 + 6^3 + 7^4 + 8^1 + 9^2. \\
 212 &:= 0^5 + 1^7 - 2^8 - 3^9 + 4^1 + 5^6 + 6^0 + 7^3 + 8^4 + 9^2. \\
 213 &:= 0^5 + 1^8 - 2^7 - 3^9 + 4^1 + 5^6 + 6^3 + 7^0 + 8^4 + 9^2. \\
 214 &:= 0^5 + 1^7 - 2^8 - 3^9 + 4^0 + 5^6 + 6^1 + 7^3 + 8^4 + 9^2. \\
 215 &:= 0^5 + 1^9 + 2^8 + 3^7 - 4^6 + 5^0 + 6^4 + 7^2 + 8^3 + 9^1.
 \end{aligned}$$

For complete representations of numbers from 0 to 11111 refer to author's work [17]:

1.3 Pyramidal-Type Representations

Following of the same idea of subsection 1.2, below are numbers with pyramid-type representations:

- $22 = 0^1 - 1^0 - 2^2 + 3^3$
 $= 0^2 + 1^3 + 2^4 + 3^0 + 4^1$
 $= 0^4 - 1^5 + 2^3 + 3^2 + 4^0 + 5^1$
 $= 0^2 + 1^6 + 2^5 - 3^4 + 4^3 + 5^1 + 6^0$
 $= 0^5 + 1^7 - 2^6 - 3^4 + 4^1 + 5^3 + 6^2 + 7^0$
 $= 0^1 + 1^4 + 2^8 + 3^5 - 4^7 + 5^6 + 6^3 + 7^0 + 8^2$
 $= 0^6 - 1^9 + 2^8 - 3^7 + 4^5 + 5^4 + 6^3 + 7^1 + 8^0 + 9^2.$

- $1089 = 0^1 + 1^0 + 2^3 + 3^4 + 4^5 - 5^2$
 $= 0^4 - 1^6 + 2^1 + 3^3 + 4^5 + 5^0 + 6^2$
 $= 0^2 + 1^6 - 2^7 + 3^5 + 4^1 + 5^4 + 6^0 + 7^3$
 $= 0^0 - 1^7 + 2^4 - 3^8 + 4^6 + 5^5 + 6^1 + 7^3 + 8^2$
 $= 0^6 - 1^9 + 2^7 - 3^8 + 4^1 + 5^5 + 6^3 + 7^0 + 8^4 + 9^2.$

- $1179 = 0^1 + 1^0 + 2^5 + 3^6 + 4^4 + 5^3 + 6^2$
 $= 0^2 + 1^6 + 2^4 - 3^7 + 4^0 + 5^5 + 6^3 + 7^1$
 $= 0^6 + 1^7 - 2^8 + 3^5 + 4^1 + 5^4 + 6^0 + 7^2 + 8^3$
 $= 0^6 + 1^9 - 2^8 - 3^7 + 4^5 + 5^3 + 6^1 + 7^4 + 8^2 + 9^0.$

The digits appearing in bases and exponents are same in each case. For complete representations of natural numbers from 0 to 1500 refer to [15, 16]:

1.4 Single Digit Representations

In subsection 1.1, all the nine digits are used to write natural numbers. Here the work is done writing numbers for each digit separately. See examples below:

$717 = (1+1)^{11} - 11^{(1+1+1)}$ $= 22^2 + 222 + 22/2$ $= 3^{(3+3)} - 3 - 3 \times 3$ $= 4 \times (4 \times 44 + 4) - 4 + 4/4$ $= (55 \times (55 + 5 + 5) + 5 + 5)/5$ $= (6 \times 6/(6+6))^6 - 6 - 6$ $= 777 - 7 \times 7 - 77/7$ $= 8 \times 88 + (88 + 8 + 8)/8$ $= 9 \times 9 \times 9 - (99 + 9)/9.$	$995 = (11-1)^{(1+1+1)} - (11-1)/(1+1)$ $= 22 + 2 \times (22^2 + 2) + 2/2$ $= 3 \times 333 - 3 - 3/3$ $= 4 \times (4^4 - 4 - 4) + 4 - 4/4$ $= 5 \times (5+5) \times (5 \times 5 - 5) - 5$ $= 666 + 6 \times 66 - 66 - 6/6$ $= (7+7) \times (77-7) + 7+7+7/7$ $= 888 + 88 + 8 + 88/8$ $= 999 - (9+9+9+9)/9.$
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Values are calculated up to 1.000.000, but the work is written only from 0 to 1000. For details, refer to [10]:

1.5 Single Letter Representations

We observe that the numbers written in previous subsection 1.4 are not in a symmetrical way. But there are numbers, that can be written in a symmetric way. Motivated by this idea, instead working for each digit separately, we can work with a **single letter** " a ". See examples below:

$$\begin{array}{ll}
 5 := (aa - a) / (a + a). & 1089 := (aaaa - aa - aa) / a. \\
 6 := (aa + a) / (a + a). & 1991 := (aaaaaaaa / aaa \times (a + a) - aa) / a. \\
 55 := (aaa - a) / (a + a). & 2020 := (aaaaaa - a) / aa \times (a + a) / a. \\
 56 := (aaa + a) / (a + a). & 2035 := (aaaa - a) / (a + a + a) \times aa / (a + a). \\
 561 := (aaaa + aa) / (a + a). & 4477 := (aaa / (a + a + a) \times aa \times aa) / (a \times a). \\
 666 := aaa \times (aa + a) / ((a + a) \times a). & 4999 := (aaaaaa - aaaa - a - a) / (a + a). \\
 925 := (aaaaa - aa) / (aa + a). & 5000 := (aaaaa - aaaa) / (a + a).
 \end{array}$$

where $a \in \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$, and $aa = 10^2 \times a + a$, $aaa = 10^3 \times a + 10^2 \times a + a$, etc.

For full work, refer to [11, 13]. The first reference is up to 3000 [11] numbers, while second reference extend it to 5000 [13] numbers.

For study on numbers in different situations refer to [3, 4, 5, 6]. Summary of above work can be seen in [18, 19].

1.6 Running Expressions

Previous section 1 give idea how we can write natural numbers in different situations using 9 or 10 digits. In this section also we shall do similar kind of work, but in little different way. It is based on the idea of subsection 1.1. We divide the numbers in equal parts, two or three in such a way that the results are increasing and decreasing order of 9 or 10 digits, for example we can write,

$$\begin{aligned}
 1^{234} &= (5 + 67) / (8 \times 9) \\
 98/7 + 6 &= 54/3 + 2 \times 1.
 \end{aligned}$$

Below are more examples, written in increasing and decreasing ways:

- **Increasing Order**

$$\begin{aligned}
 12 &= 3 + 4 + (5 \times 6 + 7 + 8) / 9 \\
 123 &= 4 + 5 + 6 \times 7 + 8 \times 9 \\
 1234 &= -5 + 6! + 7 + 8^{\sqrt{9}}
 \end{aligned}$$

$$\begin{aligned}
 12 + 3 \times 4 + 5 \times (6 + 7) &= 89 \\
 1 + 23 + 45 + 6! &= 789
 \end{aligned}$$

... (1)

- **Decreasing Order**

$$\begin{aligned} 98 - 7 \times (6 + 5) \times (4 - 3) &= 21 \\ \sqrt{9} \times 87 + 6 + 54 &= 321 \\ 9 - 8 + 7! - 6 \times 5! &= 4321 \end{aligned}$$

$$\begin{aligned} 9 - 8 + 7 - 6 + 5 + 4 - 3 + 2 &= 10 \\ 9 \times (8 + 7) + 6 + 5 + 4^3 &= 210 \\ (9 - 87 + 6!) \times 5! / 4! &= 3210 \end{aligned}$$

$$\begin{aligned} 98 &= (7 + 6) \times 5 + 4 \times 3 + 21 \\ 987 &= 6! + 5! + (4 + 3) \times 21 \end{aligned}$$

$$\begin{aligned} 98 &= 7 + 65 + 4 + 32 - 10 \\ 987 &= 6! + 54 + 3 + 210 \end{aligned}$$

... (2)

Above examples give representations separated by equality sign having the digits in either increasing and/or decreasing orders. There are numbers that can be written in increasing as well as decreasing orders at the same time with single or double equality signs, such as

$$\begin{aligned} \bullet 16 &:= 12/3 \times 4 = 5 + 6 + (7 + 8)/\sqrt{9} \\ &:= (9 + 87)/6 = 5 + 4 + 3 \times 2 + 1. \end{aligned}$$

$$\begin{aligned} \bullet 18 &= 12 + 3! = \sqrt{4 + 5} \times 6 = 7 + 8 + \sqrt{9} \\ &= \sqrt{9} + 8 + 7 = \sqrt{6 \times 54} = -3 + 21 = 3! + 2 + 10. \end{aligned}$$

$$\begin{aligned} \bullet 120 &:= (1 \times 2 + 3)! = 4 \times 5 \times 6 = ((7 + 8)/\sqrt{9})! \\ &:= ((\sqrt{9})! - 8 + 7)! = 6 \times 5 \times 4 = (3 \times 2 - 1)! = 3! \times 2 \times 10 \end{aligned}$$

... (3)

The above three examples divide the numbers in two and three parts respectively with equality signs using the numbers in increasing as well as decreasing orders. From the examples (1), (2) and (3), we observe that the operations used are **addition, subtraction, multiplication, division, potentiation, factorial and square-root**. More details can be seen in [20, 21]. In this work, our interest is to found examples similar to (1), (2) and (3) using **Fibonacci sequence** values.

2 Running Expressions with Fibonacci Sequence

This section bring results similar to (1), (2) and (3), but by use of **Fibonacci sequence** values along with basic operations. and worked up to 999. The results are in both increasing and decreasing orders.

2.1 Fibonacci Sequence

Fibonacci sequence numbers are well known in literature. This sequence is defined as

$$F(0) = 0, \quad F(1) = 1, \quad F(n+1) = F(n) + F(n-1), \quad n \geq 1.$$

Similar to (1) and (2) given above, below are examples of running expressions using **Fibonacci sequence** numbers. Most of the results uses basic operations, except numbers 21 and 9876, where extra operations, such as factorial are used.

- **Increasing Order**

$$\begin{aligned} 12 &= F(3) \times F(4) \times F(5) + 6 - 7 - 8 - 9 \\ 123 &= -4 \times 5 \times (6 - F(7)) - 8 - 9 \\ 1234 &= 5 \times F(6) \times F(7) + F(8) \times F(9) \\ \\ 1 + F(2^3 + F(4)) + (5 - 6)^7 &= 89 \\ 1 \times 2 \times 3^4 \times 5 - F(F(6)) &= 789 \\ 1 + 23 + F(4 \times 5) &= 6789. \\ &\dots \quad (4) \end{aligned}$$

- **Decreasing Order**

$$\begin{aligned} 9 + (-F(8)/7 + 6) \times 5 - F(4)! + 3 &= 21 \\ -98 - F(7) + F(6) \times 54 &= 321 \\ (F(9) \times F(8) + 7) \times 6 - 5 &= 4321 \\ \\ 98 &= (7 - 6) \times 5 + F(4) \times (32 - 1) \\ 987 &= (6 - 5) \times F(4 \times (3 + 2 - 1)) \\ \\ 98 &= -5 - 4 - 3 + 2 \times F(10) \\ 987 &= (6 - 5)^4 \times F(3 \times 2 + 10) \\ 9876 &= (\sqrt{5 + 4})! + F(F(3!) \times 2) \times 10 \\ &\dots \quad (5) \end{aligned}$$

This work deals with the **running expressions** in terms of nine or ten digits of natural numbers in increasing and decreasing cases respectively with use of **Fibonacci sequence** numbers. This is given in following two subsections.

2.2 Double Equalities

Below are examples in double equality signs, similar to example (3). The increasing and decreasing orders are together. We have considered only the situations where $[1, 2, 3] = [4, 5, 6] = [7, 8, 9]$ and $[9, 8, 7] = [6, 5, 4] = [3, 2, 1]$ or $= [3, 2, 1, 0]$. As there are few examples, we worked up to five digits.

$$\bullet 8 := 9 - 8 + 7 = F(6) \times (5 - 4) = F(3 \times 2) \times 1$$

$$\bullet 9 := 9 \times (8 - 7) = F(6) + 5 - 4 = 3 \times (2 + 1)$$

$$\begin{aligned} \bullet 10 &:= 12 - F(3) = -F(4) + 5 + F(6) = -7 + 8 + 9 \\ &:= 9 + 8 - 7 = F(6) \times 5/4 = 3^2 + 1 \\ &\quad = (3 - 2) \times 10 \end{aligned}$$

$$\bullet 11 := 9 + F(F(8)/7) = F(6) + 5 - F(F(4)) = 3 - 2 + 10$$

$$\bullet 12 := 9 + F(8)/7 = (F(6) - 5) \times 4 = F(F(F(3) + 2)) + 10$$

$$\begin{aligned} \bullet 13 &:= F((9 - 8) \times 7) = F(6 + 5 - 4) = F(3 \times 2 + 1) \\ &:= F(1 + 2 \times 3) = F(-4 + 5 + 6) = F(7) \times (-8 + 9) \end{aligned}$$

$$\begin{aligned} \bullet 14 &:= 12 + F(3) = 4 \times 5 - 6 = F(7) - 8 + 9 \\ &:= 98/7 = 6 + 5 + F(4) = F(3) + 2 + 10 \end{aligned}$$

$$\bullet 17 := 9 + F(8) - F(7) = F(6) + 5 + 4 = -3 + 2 \times 10$$

$$\begin{aligned} \bullet 18 &:= 9 \times F(F(8)/7) = 6 \times (5 - F(F(4))) = -3 + 21 \\ &\quad = F(3 \times 2) + 10 \end{aligned}$$

$$\begin{aligned} \bullet 19 &:= F(9) - 8 - 7 = F(F(6)) - 5 + F(4) = -F(3) + 21 \\ &\quad = 3^2 + 10 \end{aligned}$$

$$\begin{aligned} \bullet 20 &:= -1 + F(2^3) = 4 - 5 + F(F(6)) = 7 - F(8) + F(9) \\ &:= F(9) - F(8) + 7 = F(F(6)) - 5 + 4 = F(F(3 \times 2)) - 1 \end{aligned}$$

$$\begin{aligned} \bullet 21 &:= F(1 \times 2^3) = F(4) \times 5 + 6 = F(7 - 8 + 9) \\ &:= F(9 - 8 + 7) = 6 + 5 \times F(4) = F(3^2 - 1) \end{aligned}$$

$$\begin{aligned} \bullet 22 &:= -1 + 23 = F(F(4)) \times (5 + 6) = 7 \times 8 - F(9) \\ &:= -F(9) + 8 \times 7 = F(F(6)) + 5 - 4 = F(F(3 \times 2)) + 1 \\ &\quad = 32 - 10 \end{aligned}$$

$$\begin{aligned} \bullet 23 &:= 1 \times 23 = F(4) \times 5 + F(6) = -7 + F(8) + 9 \\ &:= 9 + F(8) - 7 = F(6) + 5 \times F(4) = F(3) + 21 \\ &\quad = 3 + 2 \times 10 \end{aligned}$$

$$\bullet \mathbf{24} := 1 + 23 = 45 - F(F(6)) = 7 + 8 + 9 \\ := 9 + 8 + 7 = F(6) \times (5 - F(F(4))) = 3 + 21$$

$$\bullet \mathbf{27} := 9 \times F(8)/7 = 6 \times 5 - F(4) = 3^{(2+1)}$$

$$\bullet \mathbf{30} := 9 + 8 + F(7) = F(F(6)) + 5 + 4 \\ = F(F(3) + 2) \times 10$$

$$\bullet \mathbf{31} := F(9) - F(8)/7 = 6 + 5^{(F(F(4)))} = 32 - 1$$

$$\bullet \mathbf{32} := F(9) - F(F(8)/7) = 6 \times 5 + F(F(4)) = 32 \times 1$$

$$\bullet \mathbf{33} := F(9) - 8 + 7 = (6 + 5) \times F(4) = (32 + 1)$$

$$\bullet \mathbf{34} := F(12 - 3) = 4 + 5 \times 6 = F((-7 + 8) \\ := F(9 \times (8 - 7)) = 6 \times 5 + 4 = F(3^2 \times 1)$$

$$\bullet \mathbf{36} := F(9) + F(F(8)/7) = 6^{(5 - F(4))} = 3 \times (2 + 10)$$

$$\bullet \mathbf{42} := F(9) + F(8) - F(7) = F(6) + F(5 + 4) = F(3) \times 21 \\ = 32 + 10$$

$$\bullet \mathbf{47} := -9 + 8 \times 7 = -F(6) + F(5 \times F(F(4))) = -F(3 \times 2) + F(10)$$

$$\bullet \mathbf{55} := F(12 - F(3)) = F(4 + 5) + F(F(6)) = F(-7 + 8 + 9)$$

$$\bullet \mathbf{55} := F(9 + 8 - 7) = F(F(6) \times 5/4) = F(3^2 + 1) \\ = (3 - 2) \times F(10)$$

$$\bullet \mathbf{89} := F(9 + F(F(8)/7)) = F(F(6) + 5 - F(F(4))) = F(3 - 2 + 10)$$

$$\bullet \mathbf{90} := F(9) + 8 \times 7 = 6 \times 5 \times F(4) = 3^2 \times 10$$

$$\bullet \mathbf{144} := 12^F(3) = F(4 \times 5 - F(6)) = F(F(7)) - 89$$

$$\bullet \mathbf{233} := F(F(1 + 2 \times 3)) = F(F(-4 + 5 + 6)) = F(F(7)) \times (-8 + 9)$$

$$\bullet \mathbf{377} := F(12 + F(3)) = F(4 \times 5 - 6) = F(F(7) - 8 + 9)$$

- **144** := $F(9 + F(8)/7) = F((F(6) - 5) \times 4) = F(F(F(F(3) + 2)) + 10)$

- **210** := $(9 + F(8)) \times 7 = F(F(6)) \times 5 \times F(F(4)) = F(F(3 \times 2)) \times 10$

- **233** := $(9 - 8) \times F(F(7)) = F(F(6 + 5 - 4)) = F(F(3 \times 2 + 1))$

- **377** := $F(98/7) = F(6 + 5 + F(4)) = F(F(3) + 2 + 10)$

- **1597** := $F(9 + F(8) - F(7)) = F(F(6) + 5 + 4) = F(-3 + 2 \times 10)$

- **2584** := $F(9 \times F(F(8)/7)) = F(6 \times (5 - F(F(4)))) = F(-3 + 21)$

- **4181** := $F(F(9) - 8 - 7) = F(F(F(6)) - 5 + F(4)) = F(-F(3) + 21)$
 $= F(3^2 + 10)$

- **6765** := $F(-1 + F(2^3)) = F(4 - 5 + F(F(6))) = F(7 - F(8) + F(9))$

- **6765** := $F(F(9) - F(8) + 7) = F(F(F(6)) - 5 + 4) = F(F(F(3 \times 2)) - 1)$

- **10944** := $-9 + F(F(8)) + 7 = F(F(F(6))) - 5 + F(4) = -F(3) + F(21)$

- **10946** := $F(F(1 \times 2^3)) = F(F(4) \times 5 + 6) = F(F(7 - 8 + 9))$
 $= F(F(9 - 8 + 7)) = F(6 + 5 \times F(4)) = F(F(3^2 - 1))$

- **10948** := $9 + F(F(8)) - 7 = F(F(F(6))) + 5 - F(4) = F(3) + F(21)$

- **17711** := $F(-1 + 23) = F(F(F(4)) \times (5 + 6)) = F(7 \times 8 - F(9))$
 $= F(-F(9) + 8 \times 7) = F(F(F(6)) + 5 - 4) = F(F(F(3 \times 2)) + 1)$
 $= F(32 - 10)$

- **28657** := $F(1 \times 23) = F(F(4) \times 5 + F(6)) = F(-7 + F(8) + 9)$
 $= F(9 + F(8) - 7) = F(F(6) + 5 \times F(4)) = F(F(3) + 21)$
 $= F(3 + 2 \times 10)$

- **46368** := $F(1 + 23) = F(45 - F(F(6))) = F(7 + 8 + 9)$
 $= F(9 + 8 + 7) = F(F(6) \times (5 - F(F(4)))) = F(3 + 21)$

- **196418** := $F(9 \times F(8)/7) = F(6 \times 5 - F(4)) = F(3^{2+1})$

- **832040** := $F(9 + 8 + F(7)) = F(F(F(6)) + 5 + 4) = F(F(F(3) + 2) \times 10)$

3 Single Equality Expressions

3.1 Increasing Order

Below are examples of running expressions with Fibonacci sequence values in increasing order using the digits 1 to 9 separated by single equality sign.

- $2 := 1 - 2 + 3 = F(4) - ((56/7)/8)^9$
 $:= 1^{23} - 4 + 5 = F(6 \times (7 - 8) + 9)$
- $3 := F(12/3) = 4 - ((56/7)/8)^9$
- $7 := 12/3 + F(4) = 56/7 + 8 - 9$
- $7 := 12 - 3 + F(4) - 5 = 6 - (7 - 8)^9$
- $9 := 1^{2345} + F(6) = (-7 + 8) \times 9$
- $10 := 12 - F(3) = (4 - 5)^{678} + 9$
- $11 := 12 + 3 - 4 = 56 - (F(7) - 8) \times 9$
 $:= 12/3 \times 4 - 5 = -6 \times F(7) + 89$
- $12 := F(12)/(3 \times 4) = 56 - 78 + F(9)$
 $:= 1^{234} + 5 + 6 = F(7) + 8 - 9$
 $:= 12 + 3 - 45 + 6 \times 7 = F(8) - 9$
- $13 := F(1 + 2 \times 3) = (45 - 6 + 78)/9$
 $:= (123 - 45)/6 = F(7 \times (-8 + 9))$
 $:= 1^{23456} \times F(7) = -F(8) + F(9)$
- $14 := 12 + F(3) = 4 + 5 - 67 + 8 \times 9$
 $:= 1^{234} + 5 + F(6) = F(7) - 8 + 9$
- $17 := 12 + 3 + F(F(4)) = -5 - 67 + 89$
 $:= 1 + 23 + 4 - 5 - 6 = -F(7) + F(8) + 9$
- $18 := 12 - 3 + 4 + 5 = 6 + F(7) + 8 - 9$
- $19 := 12 + 3 \times 4 - 5 = 6 + F(7) \times (-8 + 9)$
 $:= (123 - 4 - 5)/6 = 7 + F(8) - 9$
- $20 := -1 + F(2^3) = F(4) - 5 - 67 + 89$
 $:= 1^{23} \times 4 \times 5 = 6 + F(7) - 8 + 9$
 $:= -1 \times 2 - 34 + 56 = 7 - F(8) + F(9)$
- $21 := F(1 \times 2^3) = 4 - 5 - 67 + 89$
 $:= F(12/3 + 4) = 56 + 7 - 8 - F(9)$
 $:= 12/3 \times 4 + 5 = 6 \times (F(7) - 8) - 9$
 $:= 1 - 2 - 34 + 56 = F(7 - 8 + 9)$

- 22 := $(F(12) - 34)/5 = -67 + 89$
 $:= (1 - 2) \times 34 + 56 = 7 \times 8 - F(9)$
- 23 := $1 - 23 + 45 = 6 - F(7) + F(8) + 9$
 $:= 1^2 - 34 + 56 = -7 + F(8) + 9$
- 24 := $1 + 23 = 4 - 56 - F(7) + 89$
 $:= 12 \times (3 + 4 - 5) = 6 \times (-F(7) + 8 + 9)$
- 25 := $12 + F(3 + 4) = 56/7 + 8 + 9$
 $:= 1 + 2 - 34 + 56 = F(7) + F(8) - 9$
- 26 := $1 \times 23 + F(4) = -56 - 7 + 89$
 $:= -F(12) + 34 \times 5 = (6 - 7) \times (8 - F(9))$
 $:= 1^2 + 3^4 - 56 = F(7) - F(8) + F(9)$
 $:= 12/3 + 4 + 5 + 6 + 7 = -8 + F(9)$
- 27 := $-12 + 34 + 5 = 6 + F(7 - 8 + 9)$
- 28 := $1 + 23 + 4 = -5 - F(6) \times 7 + 89$
 $:= 1 - 2 + 34 - 5 = 6 + 7 \times 8 - F(9)$
- 29 := $1 \times 2 + 3^{F(4)} = 5 \times 6 + (7 - 8)^9$
 $:= 12 - 3 + 4 \times 5 = 6 - 7 + F(8) + 9$
 $:= 12 \times 3 + 4 - 5 - 6 = -F(7) + 8 + F(9)$
- 30 := $F(12 - 3) - 4 = 5 + 67 - 8 - F(9)$
 $:= 1^{234} \times 5 \times 6 = F(7) + 8 + 9$
 $:= -12 - 3 + 45 \times (-6 + 7) = F(8) + 9$
- 31 := $1 \times 2 + 34 - 5 = 6 + F(7) + F(8) - 9$
- 32 := $1 + 2 + 34 - 5 = F(6) + 7 + 8 + 9$
- 33 := $1 - 2 + 34 = 56 + 7 - F(8) - 9$
 $:= 1 + 23 + 4 + 5 = -F(6) \times 7 + 89$
 $:= 12 \times 3 - 4 - 5 + 6 = 7 - 8 + F(9)$
- 34 := $F(12 - 3) = F(4) - 56 + 78 + 9$
 $:= 1^2 \times 34 = 56/7 - 8 + F(9)$
 $:= 1 - 2 + (3 + 4) \times 5 = (6 - 7)^8 \times F(9)$
 $:= 12 - 34 + 56 = F((-7 + 8) \times 9)$
- 35 := $12 + 3 + 4 \times 5 = (6 - 7)^8 + F(9)$
 $:= 12 + 34 - 5 - 6 = -7 + 8 + F(9)$
- 36 := $(12 - 3) \times 4 = 567/F(8) + 9$

$$\bullet 37 := 1 + 2 + 34 = 56 + 7 + 8 - F(9)$$

$$:= 12 \times 3 - 4 + 5 = 67 - F(8) - 9$$

$$:= 1^2 - 3 + 45 - 6 = 7 + F(8) + 9$$

$$\bullet 38 := F(12 - 3) + 4 = F(56/7) + 8 + 9$$

$$:= 1 - 2 + 34 + 5 = -6 + 78 - F(9)$$

$$\bullet 39 := 12 \times 3 + F(4) = -5 \times 6 + 78 - 9$$

$$:= 1^2 \times 34 + 5 = 6 \times (F(7) - 8) + 9$$

$$:= 12 \times 3 + 4 + 5 - 6 = F(7) - 8 + F(9)$$

$$\bullet 40 := 1 - 2 \times 3 + 45 = 6 + (-7 + 8) \times F(9)$$

$$\bullet 41 := 123/F(4) = (5 + 6 - 7) \times 8 + 9$$

$$:= 12 + 34 - 5 = 67 + 8 - F(9)$$

$$\bullet 42 := (12 + F(3)) \times F(4) = 56 - F(7) + 8 - 9$$

$$:= 1^2 \times (3 + 45 - 6) = -F(7) + F(8) + F(9)$$

$$:= 1^{2345} \times 6 \times 7 = 8 + F(9)$$

$$\bullet 43 := 1 + 2 \times F(F(3) \times 4) = 5 - 6 + 78 - F(9)$$

$$:= 12/3 + 45 - 6 = F(7) + F(8) + 9$$

$$\bullet 44 := F(12)/3 - 4 = 56 - F(7) - 8 + 9$$

$$:= 1 \times 2 - 3 + 45 = F(6) \times 7 - F(8) + 9$$

$$:= 12 \times (3 - 4) + 56 = 78 - F(9)$$

$$\bullet 45 := (12 + 3) \times F(4) = -5 + 67 - 8 - 9$$

$$:= 12 + 34 + 5 - 6 = (F(7) - 8) \times 9$$

$$\bullet 46 := 1^{23} + 45 = F(F(6)) + F(7) + F(8) - 9$$

$$\bullet 47 := (F(12) - 3)/F(4) = 56 + (7 - 8) \times 9$$

$$\bullet 48 := F(12)/3 = 45 - 6 + (-7 + 8) \times 9$$

$$:= (1 + 23) \times F(F(4)) = 56 - 7 + 8 - 9$$

$$:= 12 - 3 + 45 - 6 = -7 + F(8) + F(9)$$

$$\bullet 49 := (F(12) + 3)/F(4) = 56 + 7 \times (8 - 9)$$

$$:= 12/3 + 45 = 6 + F(7) + F(8) + 9$$

$$:= 1^2 - 3 + 45 + 6 = 7 + 8 + F(9)$$

$$\bullet 50 := F(12 - F(3)) - 4 = 56 + 7 - F(8) + 9$$

$$:= F(12)/3 + F(F(4)) = 56 - 7 - 8 + 9$$

$$:= 12 + 34 + 5 = 6 + (F(7) - 8) \times 9$$

$$\bullet 52 := F(12)/3 + 4 = 5 - 6 \times 7 + 89$$

$$\bullet 53 := -1 + 2 \times 3^{F(4)} = 5 + 6 \times (7 - 8 + 9)$$

$$\bullet \mathbf{54} := (12 - 3) + 45 = 6 \times 7 + F(8) - 9 \\ := 1 \times 2 \times 3^{F(4)} = 5 \times 6 + 7 + 8 + 9$$

$$\bullet \mathbf{55} := F(12 - F(3)) = F(4) + 56 + F(7) - 8 - 9 \\ := F(1 \times 2 \times 3 + 4) = 5 + 67 - 8 - 9 \\ := 12 - F(3) + 45 = 67 - F(8) + 9 \\ := -1^{234} + 56 = F(-7 + 8 + 9) \\ := 1 \times 23 + 4 \times 56/7 = F(8) + F(9)$$

$$\bullet \mathbf{56} := (12 + F(3)) \times 4 = (56 + 7) \times 8/9 \\ := 12 \times 3 + 4 \times 5 = 6 \times (7 + 8) - F(9)$$

$$\bullet \mathbf{57} := F(12 - F(3)) + F(F(4)) = 5 + 6 \times 78/9 \\ := -1 + 2 \times (34 - 5) = F(6) \times 7 - 8 + 9$$

$$\bullet \mathbf{58} := F(12 - F(3)) + F(4) = 56 \times 7/8 + 9 \\ := 1 \times 2 \times (34 - 5) = F(F(6)) \times 7 - 89$$

$$\bullet \mathbf{59} := F(12 - F(3)) + 4 = 5 + 6 \times (-7 + 8) \times 9 \\ := 12 + F(3) + 45 = 6 \times 7 + 8 + 9 \\ := 12 - 3 \times F(4) + 56 = -F(7) + 8 \times 9$$

$$\bullet \mathbf{60} := (12 + 3) \times 4 = 56 - F(7) + 8 + 9 \\ \mathbf{61} := (12 + F(3)) \times 4 + 5 = -F(6) + 78 - 9$$

$$\bullet \mathbf{62} := -1 + F(2^3) \times F(4) = 56 + 7 + 8 - 9 \\ := 1 \times 2 + 3 \times 4 \times 5 = F(6) \times F(7) - 8 - F(9) \\ := 1 \times 23 + 45 - 6 = 7 + F(8) + F(9)$$

$$\bullet \mathbf{63} := F(12) - 3^4 = 56 - 7 \times (8 - 9)$$

$$\bullet \mathbf{64} := (12/3)^{F(4)} = 56 + 7 - 8 + 9 \\ := 1 + 2 \times 34 - 5 = F(6) \times (7 - 8 + 9)$$

$$\bullet \mathbf{65} := 1 + 2^{3+F(4)} = 56 - (7 - 8) \times 9 \\ := (12 - 3 + 4) \times 5 = 6 - F(7) + 8 \times 9 \\ := 123 - F(F(4)) - 56 = 7 \times 8 + 9$$

$$\bullet \mathbf{66} := (-1 + 23) \times F(4) = 56 - 7 + 8 + 9 \\ := 1 \times F(2^3) + 45 = 67 + 8 - 9$$

$$\bullet \mathbf{67} := -1 + 2 \times 34 = 5 \times 6 + 7 + F(8) + 9 \\ \bullet \mathbf{68} := F(12)/3/4 + 56 = F(7) + F(8) + F(9)$$

$$\bullet \mathbf{69} := 1 + 2 \times 34 = 56 - F(7) \times (8 - 9) \\ := 1 + 23 + 45 = -F(F(6))/7 + 8 \times 9$$

- **70** := $1 + 23 \times F(4)$ = $-5 + 6 + 78 - 9$
 $:= 12 \times 3 + F(4 + 5) = -6 - F(7) + 89$
- **70** := $123 - 45 - F(6)$ = $F(7) \times 8 - F(9)$
- **71** := $(F(12) - F(3))/F(F(4)) = 567 + 8 - 9$
- **72** := $F(12)/F(3)$ = $45 + F(F(6)) + 7 + 8 - 9$
 $:= (1 + 23) \times F(4) = 5 - 67 \times (8 - 9)$
 $:= (1 + 2)^3 + 45 = 6 \times 7 + F(8) + 9$
 $:= 123 - 45 - 6 = (-F(7) + F(8)) \times 9$
- **73** := $(F(12) + F(3))/F(F(4)) = 5 + 67 - 8 + 9$
 $:= 1 \times 2 \times 34 + 5 = F(6) + 7 \times 8 + 9$
- **74** := $1 + 2 \times 34 + 5 = -F(6) - 7 + 89$
 $:= F(12)/F(3) + F(F(4)) = -5 + 67 + F(8) - 9$
- **75** := $F(12)/F(3) + F(4) = 56 - 7 - 8 + F(9)$
- **76** := $F(12)/F(3) + 4 = (5 - 6) \times F(7) + 89$
 $:= F(12/3)^4 - 5 = -6 - 7 + 89$
 $:= 1 + 23 - 4 + 56 = -F(7) + 89$
- **77** := $-1 + 2 \times (34 + 5) = F(6) + 78 - 9$
- **78** := $123 - 45 = 6 - (F(7) - F(8)) \times 9$
- **79** := $1 + 2 \times (34 + 5) = 67 + F(8) - 9$
- **80** := $12/3 \times 4 \times 5 = 67 - F(8) + F(9)$
- **82** := $1 \times 2 + F(3)^4 \times 5 = 6 - F(7) + 89$
- **83** := $(-1 + 23) \times 4 - 5 = -F(6) + 7 \times (-F(8) + F(9))$
- **84** := $123 - 45 + 6 = 7 \times (F(8) - 9)$
- **85** := $1 + F(2^3) \times 4 = 5 + 67 - F(8) + F(9)$
 $:= -1 + 2 + F(3) \times 45 - 6 = F(7) + 8 \times 9$
- **86** := $-1 + 23 \times 4 - 5 = F(F(6)) - 7 + 8 \times 9$
- **87** := $(1 + 2) \times (34 - 5) = F(6) + 7 + 8 \times 9$
- **89** := $F(12 + 3 - 4) = 5 + 67 + 8 + 9$
 $:= 1 - 2 + 34 + 56 = F(F(7)) - F(F(8) - 9)$
- **90** := $1 + F(2^3 + F(4)) = -(5 - 6)^7 + 89$
 $:= 1^2 \times 34 + 56 = 7 \times 8 + F(9)$
- **91** := $-1 + 23 \times 4 = 56 - 7 + 8 + F(9)$
 $:= (1 + 23) \times 4 - 5 = 6 + F(7) + 8 \times 9$
 $:= 1^2 + 34 + 56 = 7 \times (-F(8) + F(9))$

$$\bullet \mathbf{92} := 1 \times 23 \times 4 = F(5 + 6 - 7) + 89$$

$$:= 1 \times 2 + F(3) \times 45 = F(F(6))/7 + 89$$

$$\bullet \mathbf{93} := F(12)/3 + 45 = 6 + 78 + 9$$

$$\bullet \mathbf{94} := 1 \times 2 \times (F(3) + 45) = -F(6) + F(7) + 89$$

$$\bullet \mathbf{95} := 1 \times (23 - 4) \times 5 = F(6) + 78 + 9$$

$$:= F(12) + 3 + 4 - 56 = F(7) \times 8 - 9$$

$$\bullet \mathbf{98} := 12 + 3^4 + 5 = 6 \times 7 \times F(8)/9$$

$$\bullet \mathbf{99} := 12^{F(3)} - 45 = 6 \times (7 + 8) + 9$$

$$\bullet \mathbf{100} := (12 - F(3))^{F(F(4))} = 56 + 78 - F(9)$$

$$:= (1 + 23 - 4) \times 5 = F(F(6)) + 7 + 8 \times 9$$

$$\bullet \mathbf{101} := (1 + 23) \times 4 + 5 = 6 + F(7) \times 8 - 9$$

$$\bullet \mathbf{102} := (1 + 2) \times 34 = 5 + 67 + F(8) + 9$$

$$:= 12 + F(3) \times 45 = 6 + 7 + 89$$

$$:= 12 + 34 + 56 = F(7) + 89$$

$$\bullet \mathbf{103} := 123 - 4 \times 5 = F(F(6)) - 7 + 89$$

$$\bullet \mathbf{104} := 1 \times 2 + 3 \times F(4 + 5) = F(6) + 7 + 89$$

$$\bullet \mathbf{105} := F(12) - 34 - 5 = F(6) \times F(7) - 8 + 9$$

$$\bullet \mathbf{106} := (1 + 23^{F(F(4))})/5 = -6 + 78 + F(9)$$

$$\bullet \mathbf{107} := (1 + 2) \times 34 + 5 = -6 + F(7) \times 8 + 9$$

$$\bullet \mathbf{108} := F(12) \times 3/4 = (5 + 6 - 7 + 8) \times 9$$

$$:= 123 - F(4) \times 5 = 6 + F(7) + 89$$

$$\bullet \mathbf{109} := F(12) - (3 + 4) \times 5 = 67 + 8 + F(9)$$

$$\bullet \mathbf{110} := F(12) - 34 = 5 \times (-67 + 89)$$

$$:= (-12 + 34) \times 5 = F(6) + F(7) + 89$$

$$\bullet \mathbf{111} := (1 + 2) \times (3 + F(4 + 5)) = F(6) \times (7 + 8) - 9$$

$$\bullet \mathbf{112} := F(12) + F(3) - F(4 + 5) = F(6) \times (F(7) - 8 + 9)$$

$$:= 1 \times 2 \times (3 \times 4 - 5) \times F(6) = 78 + F(9)$$

$$\bullet \mathbf{113} := F(12) + 3 - F(4 + 5) = (6 + 7) \times 8 + 9$$

$$:= (1 + 2) \times 34 + 5 + 6 = F(7) \times 8 + 9$$

$$\bullet \mathbf{116} := 123 - F(F(4)) - 5 = F(F(6)) + F(7) \times 8 - 9$$

$$\bullet \mathbf{117} := F(12) - 3^{F(4)} = 5 \times 6 + 78 + 9$$

$$:= (1 + 2) \times (34 + 5) = F(F(6)) + 7 + 89$$

$$\bullet \mathbf{118} := F(12) - F(F(3) \times 4) - 5 = 6 + 78 + F(9)$$

- **119** := $-1 + 2 \times 3 \times 4 \times 5 = 6 + (F(7) \times 8) + 9$
 $\quad := F(12) - 3^4 + 56 = 7 \times (8 + 9)$
- **120** := $123 - F(4) = (5 + 6 - 7) \times (F(8) + 9)$
 $\quad := (12 + 3 \times 4) \times 5 = F(6) + 78 + F(9)$
- **121** := $123 - F(F(4)) = 56 + 7 \times 8 + 9$
 $\quad := 123 + F(4) - 5 = F(6) + F(7) \times 8 + 9$
- **122** := $123 + 4 - 5 = -67 + F(8) \times 9$
- **123** := $123 = 4 \times 5 \times (-6 + F(7)) - 8 - 9$
 $\quad := F(12) - F(F(3) \times 4) = 5 + 6 + 78 + F(9)$
 $\quad := 123 \times (-4 + 5) = F(6 + F(7) - 8) + F(9)$
- **124** := $-1 + (2 + 3)^{F(4)} = 5 + 6 + F(7) \times 8 + 9$
 $\quad := 123 - 4 + 5 = 6 \times (7 + 8) + F(9)$
- **125** := $123 + F(F(4)) = 56 + 78 - 9$
 $\quad := 123 - F(4) + 5 = 6 + 7 \times (8 + 9)$
- **126** := $123 + F(4) = 5 \times 6 + 7 + 89$
 $\quad := (1 + 2) \times (-3 + 45) = 6 \times F(7 - 8 + 9)$
 $\quad := 123 + 4 + 5 - 6 = (-7 + F(8)) \times 9$
- **127** := $123 + 4 = 5 \times F(6) + 78 + 9$
 $\quad := F(12) + 3 - 4 \times 5 = F(6) + 7 \times (8 + 9)$
- **128** := $1 \times 2^{3+4} = 5 + F(F(6)) + F(7) + 89$
 $\quad := 1 \times 2^{3 \times 4 - 5} = F(6) \times 7 + 8 \times 9$
- **129** := $1 + 2^{3+4} = 5 + 6 \times (7 + 8) + F(9)$
 $\quad := 12^{F(3)} - F(4) \times 5 = F(6) \times (7 + 8) + 9$
- **130** := $(-1 + 23 + 4) \times 5 = F(F(6)) \times 7 - 8 - 9$
- **131** := $123 + F(4) + 5 = 6 \times 7 + 89$
 $\quad := 123 \times (-4 + 5) + F(6) = -F(7) + F(F(8) - 9)$
 $\quad := F(12) - F(3 + 4) = -5 \times 6 + F(F(7)) - 8 \times 9$
- **132** := $F(12) - 3 \times 4 = 56 - F(7) + 89$
 $\quad := 123 + 4 + 5 = 6 - (7 - F(8)) \times 9$
- **133** := $-1 \times 2 + 3 \times 45 = F(F(6)) + 78 + F(9)$
- **134** := $1 - 2 + 3 \times 45 = 6 \times (7 + F(8)) - F(9)$
- **135** := $F(12) - 3 \times F(4) = 56 + 7 + 8 \times 9$
 $\quad := 1^2 \times 3 \times 45 = 6 \times (F(7) + 8) + 9$

- **136** := $F(12 - 3) \times 4 = 5 + 6 \times 7 + 89$
 $\quad := 1^2 + 3 \times 45 = -F(6) + F(F(7)) - 89$

- **137** := $F(12) - 3 - 4 = 5 - 6 + 7 \times F(8) - 9$
 $\quad := 1 \times 2 + 3 \times 45 = 6 - F(7) + F(F(8) - 9)$
 $\quad := 123 + 4 \times 5 - 6 = -7 + F(F(8) - 9)$

- **138** := $F(12) - 3 - F(4) = 56 - 7 + 89$
 $\quad := 1 + 2 + 3 \times 45 = (6 + 7) \times 8 + F(9)$
 $\quad := 1^2 + 3^4 + 56 = 7 \times F(8) - 9$

- **139** := $F(12) - 3 - F(F(4)) = -5 + F(6 + 7) - 89$

- **140** := $12^{F(3)} - 4 = -5 + F(6) \times 7 + 89$
 $\quad := (1 + 23 + 4) \times 5 = F(F(6)) + 7 \times (8 + 9)$

- **141** := $F(12) - 3 = -F(4) \times 5 + 67 + 89$
 $\quad := 12^{F(3)} - F(4) = 56 + F(7) + 8 \times 9$
 $\quad := (1 + 2) \times (F(3) + 45) = 6 + (7 + 8) \times 9$

- **142** := $F(12) - F(3) = 4 + 56 - 7 + 89$
 $\quad := F(12) + F(3) - 4 = (5 + 6) \times F(7) + 8 - 9$
 $\quad := F(12) - 3 - 4 + 5 = -F(F(F(6))/7) + F(F(8) - 9)$

- **143** := $F(12) + 3 - 4 = 56 + 78 + 9$
 $\quad := 123 + 4 \times 5 = F(6) + (7 + 8) \times 9$

- **144** := $12^{F(3)} = 4 - 5 + F(6) \times 7 + 89$
 $\quad := F(12) \times (3 - 4)^{56} = F(F(7)) - 89$
 $\quad := (12/3 + 4) \times (5 + 6 + 7) = F(F(8) - 9)$

- **145** := $F(12) - 3 + 4 = (5 + 6) \times (-7 + F(8)) - 9$
 $\quad := 12^{F(3)} - 4 + 5 = F(6) \times 7 + 89$

- **146** := $F(12) + F(3) = 4 + 5 \times 6 + 78 + F(9)$
 $\quad := F(12) - F(3) + 4 = 5 + (6 + (7 + 8) \times 9)$
 $\quad := F(12) + 3 + 4 - 5 = F(6) + 7 \times F(8) - 9$

- **147** := $F(12) + 3 = 4 + 56 + 78 + 9$
 $\quad := 1 + 2 + F(3 \times 4) = -56 + F(F(7)) - F(8) - 9$
 $\quad := 12 + 3 \times 45 = -6 \times 7 + F(8) \times 9$

- **148** := $12^{F(3)} + 4 = 5 + (6 + F(7)) \times 8 - 9$
 $\quad := F(12) + 3 - 4 + 5 = F(F(6)) \times 7 - 8 + 9$

- **149** := $12 \times 3 \times 4 + 5 = -F(F(6)) + (F(7) - 8) \times F(9)$
 $\quad := F(12) + 3 + F(F(4)) = 5 + F(6 + 7) - 89$

$$\bullet \mathbf{150} := F(12) + F(3) + 4 = 5 + F(6) \times 7 + 89 \\ := F(12) - 3 + 4 + 5 = 6 + F(F(7)) - 89$$

$$\bullet \mathbf{151} := F(12) + 3 + 4 = -5 + 67 + 89 \\ := 12 + F(3 \times 4) - 5 = -6 + F(7) + F(F(8) - 9) \\ := -1 \times 2 + 3 \times (45 + 6) = 7 + F(F(8) - 9)$$

$$\bullet \mathbf{152} := F(12) + F(3) \times 4 = 56 + 7 + 89 \\ := 1 \times 2 \times (3^4 - 5) = F(6) + F(F(7)) - 89$$

$$\bullet \mathbf{153} := F(12) + 3 \times F(4) = 5 - F(6) + 7 \times F(8) + 9 \\ := 12^{F(3)} + 4 + 5 = -F(6) + F(F(7)) - 8 \times 9$$

$$\bullet \mathbf{154} := (-1 + 23) \times (F(F(4)) + 5) = F(6) \times (7 + 8) + F(9) \\ \bullet \mathbf{155} := (-1 - 2 + 34) \times 5 = -6 + F(F(7)) - 8 \times 9$$

$$\bullet \mathbf{156} := F(12) + 3 \times 4 = (5 + 6) \times (7 + 8) - 9 \\ := 12 + F(3 + 4 + 5) = 67 + 89 \\ := 123 + F(4) \times (5 + 6) = 7 \times F(8) + 9$$

$$\bullet \mathbf{157} := F(12) + F(3 + 4) = -5 + 6 + 7 \times F(8) + 9 \\ := 123 + F(4 + 5) = 6 + 7 + F(F(8) - 9) \\ := 123 + 4 + 5 \times 6 = F(7) + F(F(8) - 9)$$

$$\bullet \mathbf{158} := -12 + 34 \times 5 = F(F(6)) - 7 + F(F(8) - 9) \\ \bullet \mathbf{159} := -1 + (-2 + 34) \times 5 = 6 \times (7 + F(8)) - 9$$

$$\bullet \mathbf{160} := F(12) + F(3)^4 = (5 + 6) \times F(7) + 8 + 9 \\ := (12 \times 3 - 4) \times 5 = 6 \times (F(7) + 8) + F(9)$$

$$\bullet \mathbf{161} := 1 + (-2 + 34) \times 5 = F(6 + 7) - 8 \times 9 \\ := (-1 - 2 + 34) \times 5 + 6 = F(F(7)) - 8 \times 9$$

$$\bullet \mathbf{162} := 1 \times 2 \times 3^4 = -5 + 6 \times F(7) + 89 \\ := F(12) + F(3 + 4) + 5 = 6 + 7 \times F(8) + 9$$

$$\bullet \mathbf{163} := F(12) - F(3) + F(F(4) + 5) = 6 + F(7) + F(F(8) - 9) \\ := 1 + 2 \times 3^4 = (5 + 6) \times (-7 + F(8)) + 9$$

$$\bullet \mathbf{164} := 12^{F(3)} + 4 \times 5 = F(6) + 7 \times F(8) + 9$$

$$\bullet \mathbf{165} := F(12 - F(3)) \times F(4) = 5 \times 6 + (7 + 8) \times 9 \\ := (1 - 2 + 34) \times 5 = F(F(6)) + F(F(7)) - 89$$

$$\bullet \mathbf{166} := F(12) + F(3) + 4 \times 5 = -67 + F(-F(8) + F(9))$$

$$\bullet \mathbf{167} := -1 - 2 + 34 \times 5 = 6 \times F(7) + 89$$

$$\bullet \mathbf{168} := 123 + 45 = F(F(6)) \times (7 - 8 + 9)$$

- **169** := $F(1 + 2 \times 3)^{F(4)} = 56 + F(7) \times 8 + 9$
 $\quad := 1 - 2 + 34 \times 5 = (6 + 7) \times (-F(8) + F(9))$
 $\quad := (12 - 3 + 4) \times (5 + F(6)) = F(7) \times (-F(8) + F(9))$
- **170** := $1^2 \times 34 \times 5 = (6 + 7 - 8) \times F(9)$
 $\quad := (12 - F(3)) \times (4 + 5 + F(6)) = (F(7) - 8) \times F(9)$
- **171** := $F(12) + 3^{F(4)} = F(5 + 6) - 7 + 89$
 $\quad := 1^2 + 34 \times 5 = (-F(F(F(6))/7) + F(8)) \times 9$
- **172** := $1 \times 2 + 34 \times 5 = -6 + F(F(7)) - F(8) - F(9)$
- **173** := $F(12) + 34 - 5 = F(F(6)) \times 7 - 8 + F(9)$
- **174** := $F(12) + (3 + F(4)) \times 5 = 6 \times (-F(7) + 8 + F(9))$
- **175** := $(1^2 + 34) \times 5 = -6 + 7 \times F(8) + F(9)$
- **176** := $F(12) - F(3) + F(4 + 5) = -6 - 7 + F(8) \times 9$
 $\quad := 123 - F(4) + 56 = -F(7) + F(8) \times 9$
- **177** := $-1 + 2 \times F(3 + F(4) + 5) = 6 \times (7 + F(8)) + 9$
- **178** := $F(12) + 34 = (5 + 6 + 7) \times 8 + F(9)$
 $\quad := 12^{F(3)} + F(4 + 5) = F(6 + 7) - F(8) - F(9)$
 $\quad := 1 \times 234 - 56 = F(F(7)) - F(8) - F(9)$
- **180** := $12/3 \times 45 = 6 \times (F(7) + 8 + 9)$
- **181** := $1 + (2 + 34) \times 5 = -F(6) + (F(7) + 8) \times 9$
 $\quad := 1 + 2 \times (34 + 56) = 7 \times F(8) + F(9)$
- **182** := $12 + 34 \times 5 = (6 - F(7)) \times (8 - F(9))$
 $\quad := 123 + F(4) + 56 = 7 \times (-8 + F(9))$
- **183** := $F(12) + 34 + 5 = -6 + (F(7) + 8) \times 9$
- **184** := $1 \times 23 \times (F(4) + 5) = F(F(6)) \times F(7) - 89$
- **185** := $(1 + 2 + 34) \times 5 = -6 + F(F(7)) - 8 - F(9)$
- **186** := $F(12) - 3 + 45 = 6 \times 7 + F(F(8) - 9)$
- **187** := $F(12) - F(3) + 45 = 6 + 7 \times F(8) + F(9)$
- **188** := $F(F(1 + 2 \times 3)) - 45 = 6 - 7 + F(8) \times 9$
- **189** := $12^{F(3)} + 45 = (6 + 7 + 8) \times 9$
 $\quad := 12 + 3 \times (F(4) + 56) = (F(7) + 8) \times 9$
 $\quad := (1 \times 2 - 3 + 4) \times (56 + 7) = F(8) \times 9$
- **190** := $(F(12 - 3) + 4) \times 5 = -6 + 7 + F(8) \times 9$
- **191** := $F(12) + F(3) + 45 = F(6 + 7) - 8 - F(9)$
 $\quad := (1 + 2 + 34) \times 5 + 6 = F(F(7)) - 8 - F(9)$

- 192 := $F(12)/3 \times 4 = -5 - 6 + F(F(7)) - F(8) - 9$
 $\quad := F(12) + 3 + 45 = F(6) \times (7 + 8 + 9)$
- 193 := $1 + 2 \times 3 \times F(F(4))^5 = F(6) \times F(7) + 89$
- 195 := $(12 \times 3 + F(4)) \times 5 = 6 + (F(7) + 8) \times 9$
- 196 := $(12 + F(3))^{F(F(4))} = -56 + (7 + F(8)) \times 9$
 $\quad := (12 + F(3))^{-F(4)+5} = -6 + F(7) + F(8) \times 9$
 $\quad := (-1 + 2^3) \times (4 \times 5 + F(6)) = 7 + F(8) \times 9$
- 197 := $F(12)/3 \times 4 + 5 = F(6) + (F(7) + 8) \times 9$
- 198 := $(-1 + 23) \times (4 + 5) = 6 \times (7 - 8 + F(9))$
- 199 := $F(12) + F(3 + F(F(4)) + 5) = F(F(6 - 7 + 8)) - F(9)$
- 200 := $(12 \times 3 + 4) \times 5 = F(6) \times (F(F(7)) - 8)/9$
- 201 := $-F(12) + 345 = -6 + F(F(7)) + 8 - F(9)$
- 202 := $F(12) + 3 + F(F(F(4)) \times 5) = 6 + 7 + F(8) \times 9$
 $\quad := 1 - 23 + 4 \times 56 = F(7) + F(8) \times 9$
- 203 := $-1 + 2 \times 3 \times F(4 + 5) = F(6 + 7) - F(8) - 9$
 $\quad := -1 + 234 + 5 \times 6 = F(F(7)) - F(8) - 9$
- 204 := $12 \times (3 \times 4 + 5) = F(6) + 7 + F(8) \times 9$
- 205 := $123/F(4) \times 5 = -67 + 8 \times F(9)$
- 207 := $1 \times 23 \times (4 + 5) = (F(6) + 7 + 8) \times 9$
 $\quad := -F(12) + 345 + 6 = F(F(7)) + 8 - F(9)$
- 208 := $1 + 23 \times (4 + 5) = 6 + F(7) + F(8) \times 9$
- 209 := $F(12) + F(3 + 4) \times 5 = 6 + F(F(7)) - F(8) - 9$
- 210 := $(12 + F(3)) \times F(4) \times 5 = 6 \times (-7 + 8 + F(9))$
 $\quad := (12 \times 3 + 4 - 5) \times 6 = 7 \times (F(8) + 9)$
- 211 := $1 + 2 \times F(F(3) \times 4) \times 5 = 67 + F(F(8) - 9)$
- 212 := $1 + (2 \times 3)^{F(4)} - 5 = F(F(6)) + F(F(7)) - 8 - F(9)$
- 213 := $F(F(1 + 2 \times 3)) - 4 \times 5 = 6 \times (F(7) + F(8)) + 9$
- 215 := $-1 + (2 \times 3)^{F(4)} = (5 + 6) \times F(7) + 8 \times 9$
 $\quad := F(12 - F(3)) \times 4 - 5 = F(6) \times (7 + F(8)) - 9$
- 216 := $(1 \times 2 \times 3)^{F(4)} = -5 + F(6 + 7) - F(8) + 9$
 $\quad := (1 + 23) \times (4 + 5) = F(6 + 7) - 8 - 9$
 $\quad := (12/3)^4 - 5 \times F(6) = F(F(7)) - 8 - 9$
- 217 := $1 + (2 \times 3)^{F(4)} = 5 \times F(F(6)) + 78 + F(9)$
 $\quad := 1 + (2 \times 3)^{-F(F(4))+5} = F(F(6)) + 7 + F(8) \times 9$

- 218 := $-12 - 3 + F(F(F(4)) + 5)) = F(6) + 7 \times (F(8) + 9)$

- 219 := $-1 - 23 + F(4)^5 = F(F(6)) \times 7 + 8 \times 9$

- 220 := $F(12 - F(3)) \times 4 = 5 - 6 + F(7) \times (8 + 9)$

- $= F(12) + 3^4 - 5 = F(6 + 7) + F(8) - F(9)$

- $= F(12 - 3 + 4) - 5 - F(6) = F(F(7)) + F(8) - F(9)$

- 221 := $-12 + F(F(3 + 4)) = 5 \times (67 - F(8)) - 9$

- $= 1 - 23 + F(4)^5 = (6 + 7) \times (8 + 9)$

- $= 1 \times 234 - 5 - F(6) = F(7) \times (8 + 9)$

- 222 := $1 + (2 \times 3)^{F(4)} + 5 = 6 \times (7 + F(8) + 9)$

- 223 := $-12 + F(3) + F(F(F(4)) + 5)) = F(F(6)) + F(7) + F(8) \times 9$

- 224 := $-1 + (2 + 3) \times 45 = F(6) + F(F(7)) - 8 - 9$

- 225 := $F(12) + 3^4 = 5 \times (6 + 7 - 8) \times 9$

- $= 1 \times (2 + 3) \times 45 = -F(6) + F(F(7)) \times (-8 + 9)$

- 226 := $1 + (2 + 3) \times 45 = -6 + F(F(7)) + 8 - 9$

- $= -1 + 2 + 3 + F(4)^5 - F(F(6)) = -7 + F(-F(8) + F(9))$

- 227 := $1 - 2 + F(F(3 + 4)) - 5 = 6 + F(7) \times (8 + 9)$

- 228 := $-1 + 234 - 5 = -6 + F(F(7)) - 8 + 9$

- 229 := $F(F(1 + 2 \times 3)) - 4 = 5 \times (F(F(6)) + 7) + 89$

- $= 1 \times 234 - 5 = F(6) + F(7) \times (8 + 9)$

- 230 := $-1 - 2 + F(F(3 + 4)) = F(-5 + F(F(6)))/7 + 89$

- $= (12 + 34) \times 5 = -6 \times 7 + 8 \times F(9)$

- 231 := $-1 \times 2 + F(F(3 + 4)) = -5 + F(F(6)) \times 7 + 89$

- $= 1 + 23 \times F(F(4)) \times 5 = 6 \times 7 + F(8) \times 9$

- 232 := $1 - 2 + F(F(3 + 4)) = 56 - F(7) + F(8) \times 9$

- $= F(F(1 + 2 \times 3)) + 4 - 5 = F(6 + 7) + 8 - 9$

- $= (1^2 \times 34 - 5) \times F(6) = F(F(7)) + 8 - 9$

- 233 := $F(F(1 + 2 \times 3)) = F((45 - 6 + 78)/9)$

- $= -1 + 234 = F(-56 + 78 - 9)$

- $= F(12/3 + 4 + 5) = F(6 + 7 \times (-8 + 9))$

- $= 1 \times (2 + 3)^4 - 56 \times 7 = F(-F(8) + F(9))$

- $= 1 \times 234 + 5 - 6 = F(F(7)) \times (-8 + 9)$

- 234 := $1 + 234 + 5 - 6 = F(F(7)) - 8 + 9$

- $= F(12) + F(3) \times 45 = F(6 + 7) - 8 + 9$

- 235 := $1 + 234 = -5 + 6 + F(F(7)) - 8 + 9$

- $= -1 \times 2^3 + F(4)^5 = F(F(F(6))/7) + F(-F(8) + F(9))$

$$\bullet \mathbf{236} := 1 + 2 + F(F(3 + 4)) = 5 \times 6 \times 7 - 8 + F(9) \\ := 1 - 2^3 + F(4)^5 = F(F(6)) \times 7 + 89$$

$$\bullet \mathbf{237} := F(F(1 + 2 \times 3)) + 4 = 5 + F(6 + 7) + 8 - 9 \\ := 12/3 + F(F(F(4)) + 5)) = F(F(6)) + F(F(7)) - 8 - 9$$

$$\bullet \mathbf{238} := -1 + 234 + 5 = (6 - 7 + 8) \times F(9)$$

$$\bullet \mathbf{239} := 1 \times 234 + 5 = 6 - F(F(7)) \times (8 - 9) \\ := 1 - 2 + 3 + F(4)^5 - 6 = F(7) \times F(8) - F(9)$$

$$\bullet \mathbf{240} := 1 + 234 + 5 = 6 + F(F(7)) - 8 + 9 \\ := 12/3 \times (4 + 56) = 7 + F(-F(8) + F(9))$$

$$\bullet \mathbf{241} := 123 \times F(F(4)) - 5 = F(6) + F(F(7)) \times (-8 + 9)$$

$$\bullet \mathbf{242} := F(F(1 + 2 \times 3)) + 4 + 5 = F(F(6)) + F(7) \times (8 + 9)$$

$$\bullet \mathbf{243} := (1 + 2) \times 3^4 = (567/F(8)) \times 9 \\ := (12 - 3 \times F(4))^5 = (6 + F(7) + 8) \times 9$$

$$\bullet \mathbf{244} := 1^{23} + F(4)^5 = -6 + F(F(7)) + 8 + 9$$

$$\bullet \mathbf{245} := 12 + F(F(3 + 4)) = 56 + (F(7) + 8) \times 9 \\ := 1 - 2 + 3 + F(4)^5 = F(6 + 7) + F(8) - 9 \\ := 1 \times 234 + 5 + 6 = F(F(7)) + F(8) - 9$$

$$\bullet \mathbf{246} := 123 \times F(F(4)) = 5 \times 67 - 89 \\ := 123 \times (-F(4) + 5) = -6 + (7 + F(8)) \times 9 \\ := 1 + 234 + 5 + 6 = F(F(7)) - F(8) + F(9)$$

$$\bullet \mathbf{247} := 12/3 + F(4)^5 = F(F(6)) \times F(7) + 8 - F(9)$$

$$\bullet \mathbf{248} := (1 + 2) \times 3^4 + 5 = F(6) \times F(7) + F(F(8) - 9)$$

$$\bullet \mathbf{250} := 12 + F(F(3 + 4)) + 5 = F(6 + 7) + 8 + 9 \\ := 1 + (2 - 3 + 4)^5 + 6 = F(F(7)) + 8 + 9$$

$$\bullet \mathbf{251} := (12/3)^4 - 5 = 6 + F(F(7)) + F(8) - 9$$

$$\bullet \mathbf{252} := 12 \times F(F(3) \times 4) = (56 - 7 - F(8)) \times 9 \\ := 12 - 3 + F(4)^5 = (-6 + F(7) + F(8)) \times 9 \\ := (1 + 2 + 34 + 5) \times 6 = (7 + F(8)) \times 9$$

$$\bullet \mathbf{253} := 12 - F(3) + F(4)^5 = -6 - F(7) + 8 \times F(9)$$

$$\bullet \mathbf{254} := F(12) \times F(3) - F(4 + 5) = -F(F(6)) + F(F(7)) + 8 + F(9)$$

$$\bullet \mathbf{255} := -1 + (2 + F(3))^4 = 5 + F(6 + 7) + 8 + 9 \\ := (F(12)/3 + F(4)) \times 5 = (F(6) + 7) \times (8 + 9)$$

- 256 := $(12/3)^4 = F(5 + F(6)) - 7 + F(8) + 9$
 $:= 1 \times 2^{F(3+4)-5} = 67 + F(8) \times 9$
- 257 := $1 + (2 + F(3))^4 = F(5 + F(6)) + 7 + 8 + 9$
 $:= 12 \times F(F(3) \times 4) + 5 = -6 + F(F(7)) + F(8) + 9$
- 258 := $12 + 3 + F(4)^5 = 6 + (7 + F(8)) \times 9$
- 259 := $1 + 2 + F(3)^{F(4)+5} = F(6 + 7) - 8 + F(9)$
 $:= 1 + 2 \times (3 \times 45 - 6) = F(F(7)) - 8 + F(9)$
- 260 := $(F(12)/3 + 4) \times 5 = F(6) + (7 + F(8)) \times 9$
- 261 := $(12/3)^4 + 5 = (F(6) + F(7) + 8) \times 9$
- 263 := $-1 + F(2^3) + F(4)^5 = F(6 + 7) + F(8) + 9$
 $:= 1 - 2^3 + 45 \times 6 = F(F(7)) + F(8) + 9$
- 264 := $12 \times (F(3) + 4 \times 5) = 6 \times (78 - F(9))$
 $:= 12 \times (-34 + 56) = F(7) \times F(8) - 9$
- 265 := $-1 + 23 + F(4)^5 = 6 - F(7) + 8 \times F(9)$
 $:= 1 + 2 \times 3 \times 45 - 6 = -7 + 8 \times F(9)$
- 266 := $1 \times 23 + F(4)^5 = F(F(6)) + F(F(7)) + F(8) - 9$
- 267 := $1 + 23 + F(4)^5 = F(F(6))/7 \times 89$
- 269 := $-1 + 2 \times 3 \times 45 = 6 + F(F(7)) + F(8) + 9$
- 270 := $1 \times 2 \times 3 \times 45 = 6 \times (F(7) - 8) \times 9$
- 271 := $1 + 2 \times 3 \times 45 = 6 - 7 + 8 \times F(9)$
- 272 := $F(12 - 3) \times (F(4) + 5) = (-6 + 7) \times 8 \times F(9)$
 $:= 1 - 2 + 3 + 45 \times 6 = (-F(7) + F(8)) \times F(9)$
 $:= -1^{23} + (45 - 6) \times 7 = 8 \times F(9)$
- 273 := $F(12) \times F(3) - F(4) \times 5 = F(6) - 7 + 8 \times F(9)$
- 274 := $-1 + F(2 \times 3 + 4) \times 5 = F(F(6)) \times F(7) - 8 + 9$
- 275 := $(1 + 2 \times 3^{F(4)}) \times 5 = F(6 + 7) + 8 + F(9)$
 $:= 1 + 234 + 5 \times F(6) = F(F(7)) + 8 + F(9)$
- 276 := $12 \times (3 + 4 \times 5) = -6 + F(7) \times F(8) + 9$
- 277 := $F(12 - 3) + F(4)^5 = -F(6) + F(7) + 8 \times F(9)$
- 278 := $F(F(1 + 2 \times 3)) + 45 = 6 + (-F(7) + F(8)) \times F(9)$
- 279 := $F(12) + 3 \times 45 = -6 + F(7) + 8 \times F(9)$
 $:= 12 - 3 + 45 \times 6 = 7 + 8 \times F(9)$
- 280 := $(12 + F(3)) \times 4 \times 5 = F(6) \times (-7 + 8 + F(9))$
- 281 := $F(12) \times F(3) - F(F(4)) - 5 = (F(F(6)) + F(7)) \times 8 + 9$

- 282 := $(F(12) - 3) \times F(F(4)) = 5 \times 6 \times 7 + 8 \times 9$
 $= -1 + 2 \times F(3 \times 4) - 5 = 6 \times (7 \times 8 - 9)$
 $= (1 + 234)/5 \times 6 = F(7) \times F(8) + 9$
- 283 := $1 \times 2 \times F(3 \times 4) - 5 = F(6) + F(F(7)) + 8 + F(9)$
- 284 := $F(12) \times F(3) - 4 = 5 - 6 + F(7) + 8 \times F(9)$
 $= 1 + 2 \times F(3 \times 4) - 5 = -F(F(6)) + F(F(7)) + 8 \times 9$
- 285 := $F(12) \times F(3) - F(4) = 5 \times (F(6) \times 7 - 8 + 9)$
 $= F(12) \times F(3) + F(F(4)) - 5 = 6 + 7 + 8 \times F(9)$
 $= 12 + 3 + 45 \times 6 = F(7) + 8 \times F(9)$
- 286 := $F(12) \times F(3) - F(F(4)) = 5 \times (67 - 8) - 9$
 $= (-1 + 23) \times F(F(F(4)) + 5) = F(F(6)) - 7 + 8 \times F(9)$
- 287 := $-1 + 2 \times F(3 \times 4) = (5 \times 6 + 7) \times 8 - 9$
 $= F(12) \times F(3) + 4 - 5 = F(6) + 7 + 8 \times F(9)$
- 288 := $F(12) \times F(3) = (4 + 5 - 6) \times (7 + 89)$
 $= F(12)/F(3) \times 4 = (5 + 6 - 7) \times 8 \times 9$
 $= 12 \times 3 \times (F(4) + 5) = -6 + 7 \times (8 + F(9))$
 $= 1^2 \times (3 + 45) \times 6 = F(F(7)) + F(8) + F(9)$
- 289 := $1 + 2 \times F(3 \times 4) = 56 \times (F(7) - 8) + 9$
 $= F(12) \times F(3) - 4 + 5 = F(6) \times 7 + F(-F(8) + F(9))$
- 290 := $F(12) \times F(3) + F(F(4)) = 56 + F(F(7)) - 8 + 9$
 $= (F(12 - F(3)) + F(4)) \times 5 = F(F(6)) \times F(7) + 8 + 9$
- 291 := $F(12) \times F(3) + F(4) = 5 - F(6) + 7 \times (8 + F(9))$
 $= F(12) \times F(3) - F(F(4)) + 5 = 6 + F(7) + 8 \times F(9)$
- 292 := $F(12) \times F(3) + 4 = 5 + F(6) + 7 + 8 \times F(9)$
- 293 := $1 \times 2 \times F(3 \times 4) + 5 = F(6) \times F(7) + F(8) \times 9$
- 294 := $(F(12) + 3) \times F(F(4)) = 5 \times F(F(6)) + (F(7) + 8) \times 9$
 $= 1 + 2 \times F(3 \times 4) + 5 = 6 \times (7 + 8 + F(9))$
 $= 1 + 23 + 45 \times 6 = 7 \times (8 + F(9))$
- 296 := $F(12) \times F(3) + F(4) + 5 = F(6) \times (7 + F(8) + 9)$
- 297 := $F(12) \times F(3) + 4 + 5 = -F(6) + F(F(7)) + 8 \times 9$
- 298 := $F(12 - F(3)) + F(4)^5 = -F(6) + (F(7) + F(8)) \times 9$
- 299 := $1 \times 23 \times (F(F(F(4)) + 5)) = -6 + F(F(7)) + 8 \times 9$
- 300 := $(12 + 3) \times 4 \times 5 = 6 + 7 \times (8 + F(9))$
- 301 := $F(12) \times F(3) + F(F(F(4)) + 5) = -6 + F(7) \times F(8) + F(9)$
- 303 := $F(12) \times F(3) + F(4) \times 5 = (F(F(6)) - 7) \times F(8) + 9$

- 305 := $F(12 + 3)/F(F(4)) = (5 \times 6 + 7) \times 8 + 9$
 $\quad := F(12 + 3)/(-F(4) + 5) = F(6 + 7) + 8 \times 9$
 $\quad := (F(12) + 3) \times F(F(4)) + 5 + 6 = F(F(7)) + 8 \times 9$
- 306 := $F(12 - 3) \times (4 + 5) = (6 \times 7 - 8) \times 9$
 $\quad := 12 \times 3 + 45 \times 6 = (F(7) + F(8)) \times 9$
- 307 := $1 + 2 \times 3 \times (45 + 6) = F(7) \times F(8) + F(9)$
- 309 := $F(12) \times F(3) + F(F(4) + 5) = F(F(6)) + F(F(7)) + F(8) + F(9)$
- 312 := $(1 + 23) \times F(F(F(4))) + 5 = 6 + (F(7) + F(8)) \times 9$
- 314 := $F(12) + 34 \times 5 = 6 \times 7 + 8 \times F(9)$
- 315 := $(1 + 2 \times 3) \times 45 = (F(6) \times 7 - F(8)) \times 9$
- 316 := $1 + F(2^3) \times F(4) \times 5 = -6 + F(F(7)) + 89$
- 322 := $F(12) \times F(3) + F(4 + 5) = F(6 + 7) + 89$
 $\quad := 1 \times 23 \times (4 \times 5 - 6) = F(F(7)) + 89$
- 324 := $12 \times 3^{F(4)} = 5 \times 6 + 7 \times (8 + F(9))$
 $\quad := 12 \times 3 \times (4 + 5) = F(F(6)) \times (7 + 8) + 9$
- 330 := $(-1 + 23) \times F(4) \times 5 = F(6) + F(F(7)) + 89$
- 332 := $F(12 + F(3)) - 45 = -6 + F(7) \times (-8 + F(9))$
- 335 := $(-1 + 2 \times 34) \times 5 = F(F(F(6)) - 7) - 8 - F(9)$
- 336 := $F(12)/3 \times (F(F(4))) + 5 = F(F(6)) \times 7 + F(8) \times 9$
- 338 := $(1 + 2 \times 3)^{F(4)} - 5 = (6 + 7) \times (-8 + F(9))$
 $\quad := 1 - 2 + 345 - 6 = F(7) \times (-8 + F(9))$
- 339 := $(-1 + 2 \times 34 \times 5) = 67 + 8 \times F(9)$
- 340 := $1 \times 2 \times 34 \times 5 = (F(F(F(6))/7) + 8) \times F(9)$
- 343 := $(1 + 2 \times 3)^{F(4)} = 5 + (6 + 7) \times (-8 + F(9))$
 $\quad := -1 \times 2 + 345 = F(F(6)) + F(F(7)) + 89$
 $\quad := -1 + 2 \times F(3 \times 4) + 56 = F(-7 + F(8)) - F(9)$
- 344 := $1 - 2 + 345 = 6 + F(7) \times (-8 + F(9))$
- 346 := $1^2 + 345 = F(6) + F(7) \times (-8 + F(9))$
- 347 := $1 \times 2 + 345 = F(F(F(6)) - 7) - F(8) - 9$
- 350 := $(1 + 23 \times F(4)) \times 5 = 6 \times F(7) + 8 \times F(9)$
- 351 := $(1 + 2)^3 \times F(F(F(4))) + 5 = F(F(F(6)) - 7) + 8 - F(9)$
- 356 := $123 + F(F(F(F(4))) + 5)) = -F(F(6)) + F(F(7)) + F(F(8) - 9)$
- 357 := $12 + 345 = (F(6) + F(7)) \times (8 + 9)$
- 359 := $-1 + 2^3 \times 45 = F(F(6)) + F(7) \times (-8 + F(9))$
- 360 := $1 \times 2^3 \times 45 = (6 + F(7) + F(8)) \times 9$
- 362 := $F(12 + F(3)) - F(4) \times 5 = F(F(6)) \times F(7) + 89$
- 364 := $123 \times F(4) - 5 = (F(F(6)) - 7) \times (-8 + F(9))$
- 365 := $(F(12) + F(3))/F(F(4)) \times 5 = (6 + F(7)) \times F(8) - F(9)$

- 368 := $F(12 + F(3)) - 4 - 5 = F(6 - F(7) + F(8)) - 9$
 $= 123 \times F(4) + 5 - 6 = F(-7 + F(8)) - 9$
- 369 := $123 \times (-F(F(4)) + 5) = -F(F(6)) + F(7) \times (F(8) + 9)$
- 369 := $123 \times F(4) = (56 - 7 - 8) \times 9$
- 370 := $F(12 + F(3)) - F(F(4)) - 5 = 6 \times 7 \times 8 + F(9)$
- 371 := $-1 + F(2 \times (3 + 4)) - 5 = -6 + F(F(7) - 8 + 9)$
- 372 := $12 \times (-3 + F(4 + 5)) = 6 \times (7 + F(8) + F(9))$
- 373 := $F(12 + F(3)) - 4 = 5 \times 6 \times F(7) - 8 - 9$
- 374 := $F(12 + F(3)) - F(4) = (5 + 6 \times (-7 + 8)) \times F(9)$
 $= 123 \times F(4) + 5 = 6 + F(-7 + F(8)) - 9$
- 375 := $F(12 + F(3)) - F(F(4)) = 5 \times (6 + 78 - 9)$
- 376 := $-1 + F(2 \times (3 + 4)) = 5 - 6 + F(F(7) - 8 + 9)$
 $= F(12 + F(3)) + 4 - 5 = F(6) \times (7 \times 8 - 9)$
- 377 := $F(12 + F(3)) = 4 \times (5 + 67) + 89$
 $= 1 \times F(2 \times (3 + 4)) = 5 \times 67 + 8 + F(9)$
 $= 1 \times F(23 - 4 - 5) = F(6 + 7 - 8 + 9)$
 $= F(1^{234} + 5 + F(6)) = F(F(7) - 8 + 9)$
- 378 := $1 + F(2 \times (3 + 4)) = 567 - F(8) \times 9$
 $= F(12 + F(3)) - 4 + 5 = F(F(F(6)) - 7) - 8 + 9$
- 379 := $F(12 + F(3)) + F(F(4)) = 5 + 6 + F(-7 + F(8)) - 9$
 $= F(12 + F(3)) - F(4) + 5 = -6 + 7 \times (F(8) + F(9))$
- 380 := $F(12 + F(3)) + F(4) = 5 \times (-6 - 7 + 89)$
 $= (F(12)/F(3) + 4) \times 5 = -6 + F(-7 + F(8)) + 9$
- 381 := $F(12 + F(3)) + 4 = 5 + F(6) \times (7 \times 8 - 9)$
- 382 := $1 \times F(2 \times (3 + 4)) + 5 = -F(6) + F(7) \times (F(8) + 9)$
- 383 := $1 + F(2 \times (3 + 4)) + 5 = 6 + F(F(7) - 8 + 9)$
- 384 := $12 \times (3^{F(4)} + 5) = -6 + F(7) \times (F(8) + 9)$
- 385 := $F(12 + F(3)) + F(4) + 5 = (-6 + F(7)) \times (F(8) + F(9))$
 $= (-1 + 2 + 34) \times (5 + 6) = 7 \times (F(8) + F(9))$
- 386 := $F(12 + F(3)) + 4 + 5 = F(6 - F(7) + F(8)) + 9$
 $= 12 + 34 \times (5 + 6) = F(-7 + F(8)) + 9$
- 389 := $F(12) + F(3) + F(4)^5 = F(F(F(6)) - 7) + F(8) - 9$
- 390 := $F(12) + 3 + F(4)^5 = 6 \times (7 \times 8 + 9)$
 $= F(12 - F(3) + 4) + 5 + F(6) = F(7) \times (F(8) + 9)$

$$\bullet \mathbf{392} := F(12 + F(3)) + F(4) \times 5 = 6 + F(-7 + F(8)) + 9$$

$$\bullet \mathbf{393} := -12 + 3^4 \times 5 = F(6) + 7 \times (F(8) + F(9))$$

$$\bullet \mathbf{394} := -1 + (-2 + 3^4) \times 5 = F(F(6)) - 7 + 8 + 9$$

$$\bullet \mathbf{396} := 1 + (-2 + 3^4) \times 5 = 6 + F(7) \times (F(8) + 9)$$

$$\bullet \mathbf{398} := F(12) \times 3 - F(4 + 5) = F(6) + F(7) \times (F(8) + 9)$$

$$\bullet \mathbf{400} := (-1 + F(2^3))^{F(4)} = 5 \times (67 - F(8) + F(9))$$

$$\bullet \mathbf{403} := 12 \times 34 - 5 = F(F(6)) - 7 - 8 + F(9)$$

$$\bullet \mathbf{405} := (12 - 3) \times 45 = -6 + F(-7 + F(8)) + F(9)$$

$$\bullet \mathbf{406} := 1^2 + 3^4 \times 5 = F(F(6)) + 7 \times (F(8) + F(9))$$

$$\bullet \mathbf{407} := 1 \times 2 + 3^4 \times 5 = F(F(6)) - 7 + F(8) + 9$$

$$\bullet \mathbf{408} := 12 \times 34 = (5 + 6 + F(7)) \times (8 + 9)$$

$$:= 1 + 2 + 3^4 \times 5 = (6 + F(7)) \times F(8) + 9$$

$$\bullet \mathbf{411} := F(12 + F(3)) + F(4 + 5) = F(F(6)) + F(7) \times (F(8) + 9)$$

$$:= 12 \times 34 - 5 + F(6) = F(-7 + F(8)) + F(9)$$

$$\bullet \mathbf{416} := 1 + (2 + 3^4) \times 5 = -6 + F(F(7)) + F(8) \times 9$$

$$\bullet \mathbf{417} := 12 + 3^4 \times 5 = F(F(6)) \times F(7) + F(F(8) - 9)$$

$$\bullet \mathbf{419} := -1 + F(2^3) \times 4 \times 5 = F(F(6)) \times 7 + 8 \times F(9)$$

$$\bullet \mathbf{420} := 12 \times (3 + 4) \times 5 = 6 \times (F(7) \times 8 - F(9))$$

$$\bullet \mathbf{421} := 1 + F(2^3) \times 4 \times 5 = F(F(6) + 7) - F(8) \times 9$$

$$\bullet \mathbf{422} := F(12) \times 3 - F(F(4)) \times 5 = F(6 + 7) + F(8) \times 9$$

$$:= 1 - 2 + 3 + 4 \times 5 \times F(F(6)) = F(F(7)) + F(8) \times 9$$

$$\bullet \mathbf{423} := (F(12) - 3) \times F(4) = 567 - F(F(8) - 9)$$

$$\bullet \mathbf{426} := (F(12) - F(3)) \times F(4) = (56 - 7) \times 8 + F(9)$$

$$\bullet \mathbf{428} := F(12) \times 3 - 4 = -5 + (6 + F(7)) \times F(8) + F(9)$$

$$:= (F(12) - 3) \times F(4) + 5 = 6 + F(F(7)) + F(8) \times 9$$

$$\bullet \mathbf{429} := F(12) \times 3 - F(4) = 5 \times (6 + 78) + 9$$

$$\bullet \mathbf{430} := F(12) \times 3 - F(F(4)) = 5 \times (F(6) \times (7 + 8) - F(9))$$

$$:= F(12) \times 3 + F(4) - 5 = F(6) + F(F(7)) + F(8) \times 9$$

$$\bullet \mathbf{432} := F(12) \times 3 = 456 - 7 - 8 - 9$$

$$:= (1 + 2) \times F(3 \times 4) = F(56/7) \times F(8) - 9$$

$$:= F(12) \times 3 \times (-4 + 5) = (F(6) \times 7 - 8) \times 9$$

$$\bullet \mathbf{433} := F(12) \times 3 - 4 + 5 = (6 + F(7)) \times F(8) + F(9)$$

$$\bullet \mathbf{434} := F(12) \times 3 + F(F(4)) = 56 \times 7 + 8 + F(9)$$

$$:= F(12) \times 3 - F(4) + 5 = 6 \times 78 - F(9)$$

- 435 := $F(12) \times 3 + F(4) = -5 + F(6) \times (F(7) + 8 + F(9))$
- 436 := $F(12) \times 3 + 4 = -5 + (F(F(6)) + 7 + F(8)) \times 9$
- 438 := $(F(12) + F(3)) \times F(4) = 5 + (6 + F(7)) \times F(8) - F(9)$
- 439 := $F(12) \times 3 + F(F(4)) + 5 = F(6) \times 7 \times 8 - 9$

- 440 := $(-1 + F(2^3))^{F(F(4))} = 5 \times (6 - 7 + 89)$
 $= (-1 + 23) \times 4 \times 5 = F(6) \times (F(7) + 8 + F(9))$

- 441 := $(F(12) + 3) \times F(4) = 56 \times 7/8 \times 9$
 $= F(12) \times 3 + 4 + 5 = F(F(6)) \times F(7 - 8 + 9)$

- 442 := $1 + F(2^3)^{F(F(4))} = 56 + F(-7 + F(8)) + 9$
 $= F(12 - 3) \times F(F(F(4)) + 5) = F(6 - 7 + 8) \times F(9)$

- 443 := $(F(12) + F(3)) \times F(4) + 5 = F(F(6)) + F(F(7)) + F(8) \times 9$
- 445 := $F(12 + 3 - 4) \times 5 = (-F(6) + F(7)) \times 89$
- 450 := $(12 - F(3)) \times 45 = (6 \times 7 + 8) \times 9$
- 455 := $(-1 + 23 \times 4) \times 5 = -F(F(6)) + (-7 + F(8)) \times F(9)$
- 456 := $1 \times 2 \times (F(F(3 + 4)) - 5) = 6 \times (-F(7) + 89)$

- 457 := $1 + 2 \times (F(F(3 + 4)) - 5) = F(6) \times 7 \times 8 + 9$
- 460 := $1 \times 23 \times 4 \times 5 = -6 + F(F(7)) + F(-F(8) + F(9))$
- 462 := $(-1 + 23) \times F(F(4) + 5) = F(F(6)) \times (7 \times 8 - F(9))$
- 465 := $-1 + 2 \times F(F(3 + 4)) = 5 \times (6 + 78 + 9)$

- 466 := $1 \times 2 \times F(F(3 + 4)) = F(5 + 6) + F(F(7)) + F(F(8) - 9)$
 $= F(12) \times 3 + F(4 + 5) = F(F(F(6)) - 7) + 89$
 $= 12 - F(3) + 456 = F(F(7)) + F(-F(8) + F(9))$

- 467 := $1 + 2 \times F(F(3 + 4)) = F(5 + F(6)) + F(F(7)) - 8 + 9$
- 468 := $12 \times (34 + 5) = -F(6) + (-7 + F(8)) \times F(9)$

- 470 := $1 \times 2 \times (F(3) + F(F(F(4)) + 5))) = -6 + (-7 + F(8)) \times F(9)$

- 472 := $1 + 2 \times F(F(3 + 4)) + 5 = F(6) \times (-F(7) + 8 \times 9)$
- 473 := $1 + 2 \times (3 + F(F(F(4)) + 5))) = -F(6) - F(F(7)) + F(8) \times F(9)$
- 474 := $-12 + F(3) \times F(4)^5 = 6 \times (7 + 8 \times 9)$
- 475 := $-1 + 2 \times (F(F(3 + 4)) + 5) = F(F(6)) \times (F(7) + 8) + F(9)$

- 476 := $1 \times 2 \times (F(F(3 + 4)) + 5) = (F(F(6)) + 7) \times (8 + 9)$
 $= 12 \times (34 + 5) + F(6) = (-7 + F(8)) \times F(9)$

- 477 := $F(12) \times 3 + 45 = 6 \times 78 + 9$

- 481 := $-1 + 2 \times (-F(3) + F(4)^5) = -F(6 + 7) + F(8) \times F(9)$
 $= 123 \times 4 - 5 - 6 = -F(F(7)) + F(8) \times F(9)$

- **482** := $-1 + 23 \times F(F(4) + 5) = F(6) \times 7 \times 8 + F(9)$
- **483** := $1 \times 23 \times F(F(4) + 5) = -F(F(6)) + 7 \times 8 \times 9$
- **484** := $(-1 + 23)^{F(F(4))} = (5 + 6) \times (78 - F(9))$
 $\quad := (-1 + 23)^{-F(4)+5} = -F(F(6)) + F(F(7)) + 8 \times F(9)$
- **487** := $123 \times 4 - 5 = 6 - F(F(7)) + F(8) \times F(9)$
- **489** := $F(12) + 345 = -F(F(6)) + (7 + 8) \times F(9)$
- **492** := $123 \times 4 = -5 - F(6) + F(F(7)) + 8 \times F(9)$
 $\quad := 1 \times 2 \times (3 + F(4)^5) = 6 \times (-7 + 89)$
- **495** := $F(12 - F(3)) \times (4 + 5) = (F(F(6)) + F(7) + F(8)) \times 9$
- **497** := $123 \times 4 + 5 = F(F(6)) + (-7 + F(8)) \times F(9)$
- **498** := $12 + F(3) \times F(4)^5 = -6 + 7 \times 8 \times 9$
- **504** := $12 \times (-3 + 45) = 6 \times 7 \times (F(8) - 9)$
- **505** := $123 \times 4 + 5 + F(6) = F(F(7)) + 8 \times F(9)$
- **506** := $-1 + (2^3)^{F(4)} - 5 = F(F(6)) \times F(7) + F(-F(8) + F(9))$
- **510** := $(1 + 2) \times (3^4 + F(5 + 6)) = (7 + 8) \times F(9)$
- **511** := $-1 + 2^{3 \times F(4)} = 5 \times (6 + 7) \times 8 - 9$
 $\quad := 1 - 2 + F(3)^{4+5} = 6 + F(F(7)) + 8 \times F(9)$
- **512** := $1 \times 2^{3 \times F(4)} = (56 / (7 + F(8)))^9$
 $\quad := (1 - 2 + 3)^{4+5} = F(6) + 7 \times 8 \times 9$
- **513** := $1 + 2^{3 \times F(4)} = (56 + 7) \times 8 + 9$
 $\quad := 1^2 + F(3)^{4+5} = (-F(F(6)) + 78) \times 9$
- **516** := $12 \times (-F(3) + 45) = 6 + (7 + 8) \times F(9)$
- **518** := $1 + 2^{3 \times F(4)} + 5 = F(6) + (7 + 8) \times F(9)$
- **521** := $F(12) \times F(3) + F(F(F(F(4)) + 5)) = F(F(6) + 7) - 89$
- **525** := $1 + 23^{F(F(4))} - 5 = F(F(6)) + 7 \times 8 \times 9$
- **528** := $-1 + 23^{F(F(4))} = F(-5 + F(6)) \times (F(7) \times F(8) - 9)$
- **529** := $1 \times 23^{F(F(4))} = 5 \times (6 + 7) \times 8 + 9$
- **530** := $1 + 23^{F(F(4))} = -F(5 + 6) + F(7 + 8) + 9$
- **531** := $F(12) \times F(3) + F(4)^5 = (67 - 8) \times 9$
- **534** := $1 \times 23^{F(F(4))} + 5 = 6 \times (F(F(7)) - F(F(8) - 9))$
- **538** := $-F(12) / F(3) + F(F(4) \times 5) = F(F(6) + 7) - 8 \times 9$

- **540** := $12 \times 3 \times F(4) \times 5 = 6 \times (7 \times 8 + F(9))$
- **546** := $(-1 + 2 + F(3) \times 45) \times 6 = F(7) \times (8 + F(9))$
- **555** := $-F(12 - F(3)) + F(F(4) \times 5) = F(F(6) + 7) - F(8) - F(9)$
- **564** := $(F(12) - 3) \times 4 = (5 + 6 \times 7) \times (F(8) - 9)$
- **567** := $(1 + 2)^3 \times F(F(4) + 5) = (6 \times 7 + F(8)) \times 9$
- **568** := $(F(12) - F(3)) \times 4 = 567 - 8 + 9$

- **576** := $12^{F(3)} \times 4 = 56/7 \times 8 \times 9$
 $\quad := 12 \times (-3 + 45 + 6) = F(7 + 8) - F(9)$

- **578** := $F(12 + 3) - F(F(4))^5 = (F(F(6)) + F(7)) \times (8 + 9)$
- **579** := $(F(12) + F(3)) \times 4 - 5 = F(F(6)) \times (7 + F(8)) - 9$
- **584** := $(F(12) + F(3)) \times 4 = 567 + 8 + 9$

- **588** := $(F(12) + 3) \times 4 = (56 - 7) \times (F(8) - 9)$
 $\quad := 1 - 23 + F(F(4) \times 5) = (F(F(6)) - 7) \times (8 + F(9))$

- **590** := $1 - F(2^3) + F(F(4) \times 5) = F(6) \times 78 - F(9)$
- **593** := $(F(12) + 3) \times 4 + 5 = F(F(6) + 7) - 8 - 9$
- **595** := $(123 - 4) \times 5 = -6 + F(7 + 8) - 9$
- **597** := $F(12 + 3) - F(F(F(4)) + 5) = F(F(6) + 7) + F(8) - F(9)$

- **598** := $-12 + F(F(3) + F(F(F(4)) + 5)) = F(F(6) + 7) - F(8) + 9$

- **601** := $F(12 + 3) - 4 - 5 = F(-6 + F(7) + 8) - 9$
 $\quad := (123 - 4) \times 5 + 6 = F(7 + 8) - 9$

- **602** := $F(12 + 3) - F(4) - 5 = -F(F(6)) + 7 \times 89$
- **606** := $F(12 + 3) - 4 = F(5 + 6) \times 7 - 8 - 9$

- **607** := $F(12 + 3) - F(4) = 5 \times 67 + 8 \times F(9)$
 $\quad := (-1 + 2) \times (-3 + F(F(4) \times 5)) = 6 + F(7 + 8) - 9$

- **608** := $F(12 + 3) - F(F(4)) = -5 - 6 + F(7 + 8) + 9$
 $\quad := 1^2 - 3 + F(F(4) \times 5) = F(6) \times (-F(7) + 89)$

- **609** := $-1 + F((2 + 3) \times F(4)) = 567 + 8 + F(9)$
 $\quad := F(12 + 3) + 4 - 5 = F(6) + F(7 + 8) - 9$

- **610** := $F(1 + 2 + 3 \times 4) = (5 + 67) \times 8 + F(9)$
 $\quad := F(1 + 23 - 4 - 5) = F(6 + (-7 + 8) \times 9)$
 $\quad := F(12 + 3) = 4 + 5 \times 6 + F(7 + 8) - F(9)$

- **611** := $1 + F((2 + 3) \times F(4)) = (5 + F(6)) \times (7 \times 8 - 9)$
 $\quad := F(12 + 3) - 4 + 5 = F(F(6) + 7) - 8 + 9$

- **612** := $F(12 + 3) + F(F(4)) = -5 - 6 + 7 \times 89$
 $\quad := F(12 + 3) - F(4) + 5 = 6 \times (F(7) + 89)$

- **613** := $F(12 + 3) + F(4) = 5 + F(6) \times (-F(7) + 89)$
 $\quad := F(12 + 3) - F(F(4)) + 5 = -6 + F(7 + 8) + 9$
- **614** := $F(12 + 3) + 4 = 5 + F(F(6) + 7) + 8 - 9$
- **615** := $F(1 + 2 + 3 \times 4) + 5 = F(6) \times 78 - 9$
- **617** := $F(12 + 3) + F(F(4)) + 5 = -6 + 7 \times 89$
- **619** := $-1 + (2 + 3)^4 - 5 = F(-6 + F(7) + 8) + 9$
 $\quad := 12 - 3 + F(4 + 5 + 6) = F(7 + 8) + 9$
- **622** := $12 + F(F(3) + F(F(F(4)) + 5)) = F(F(6) + 7) + F(8) - 9$
- **623** := $F(12 + 3) + F(F(F(4)) + 5) = (-6 + F(7)) \times 89$
 $\quad := F(12 + 3) + F(F(4)) + 5 + 6 = 7 \times 89$
- **625** := $12 + 3 + F(F(4) \times 5) = 6 + F(7 + 8) + 9$
- **626** := $1 + (2 + 3)^4 = -F(5 + 6) + F(7) \times (F(8) + F(9))$
- **630** := $(12 + F(3)) \times 45 = (-F(6) + 78) \times 9$
- **631** := $1 + (2 + 3)^4 + 5 = F(6) + 7 \times 89$
- **632** := $-1 + 23 + F(F(4) \times 5) = F(6) \times (7 + 8 \times 9)$
- **633** := $1 \times 23 + F(F(4) \times 5) = F(6) \times 78 + 9$
- **636** := $12 \times (-F(3) + F(F(F(4)) \times 5)) = F(F(6) + 7) - 8 + F(9)$
- **640** := $1 \times 2^{3+4} \times 5 = F(F(6) + 7) + F(8) + 9$
- **644** := $F(12 + 3) + F(4 + 5) = 678 - F(9)$
 $\quad := F(12 + 3) + 4 + 5 \times 6 = F(7 + 8) + F(9)$
- **646** := $12 \times 3 + F(F(4) \times 5) = (-F(F(F(6))/7) + F(8)) \times F(9)$
- **648** := $F(12)/F(3) \times (4 + 5) = (-6 + 78) \times 9$
- **656** := $F(12) + F(3)^{4+5} = F(6) \times (-7 + 89)$
- **658** := $F(12)/3 + F(F(4) \times 5) = F(6) \times 78 + F(9)$
- **665** := $F(12) \times 3 + F(F(F(F(4)) + 5)) = F(F(6) + 7) + F(8) + F(9)$
- **672** := $1 \times F(2^3) \times F(F(4))^5 = 6 \times (78 + F(9))$
- **680** := $F(12 - 3) \times 4 \times 5 = F(6) \times (F(7) + 8 \times 9)$
- **682** := $F(12)/F(3) + F(F(4) \times 5) = F(F(6) + 7) + 8 \times 9$
- **687** := $-12 + 3 \times F(F(F(F(4)) + 5)) = 678 + 9$
- **693** := $(1 + 2) \times (-F(3) + F(F(F(F(4)) + 5))) = (F(6) \times 7 + F(8)) \times 9$
- **694** := $(1 + 2) \times F(F(3 + 4)) - 5 = -F(6) + 78 \times 9$
- **695** := $(F(12) - 3 - F(F(4))) \times 5 = -6 - F(7) + F(8) \times F(9)$
- **696** := $-1 - 2 + 3 \times F(F(F(F(4)) + 5)) = F(6) \times (78 + 9)$
- **699** := $(1 + 2) \times F(F(3 + 4)) = 5 - F(6) + 78 \times 9$
 $\quad := (1 + 2) \times F(F(3 \times 4 - 5)) = F(F(6) + 7) + 89$

$$\bullet \mathbf{700} := (12^{F(3)} - 4) \times 5 = -F(F(6)) + 7 + F(8) \times F(9)$$

$$\begin{aligned} \bullet \mathbf{701} &:= 1 \times 2 + 3 \times F(F(F(4)) + 5) &= -6 - 7 + F(8) \times F(9) \\ &:= -F(12) \times F(3) + F(F(4)) + F(-5 + F(F(6))) &= -F(7) + F(8) \times F(9) \end{aligned}$$

$$\bullet \mathbf{705} := (-1 - 2 + F(3 \times 4)) \times 5 = (F(F(6)) + F(7)) \times F(8) - 9$$

$$\bullet \mathbf{707} := 1 \times 2 + 3 \times (F(4)^5 - F(6)) = -7 + F(8) \times F(9)$$

$$\bullet \mathbf{708} := -12 + F(3 \times 4) \times 5 := 6 + 78 \times 9$$

$$\bullet \mathbf{709} := -1 + (-2 + F(3 \times 4)) \times 5 = -6 + F(7) \times (F(8) + F(9))$$

$$\bullet \mathbf{710} := 1 \times (-2 + F(3 \times 4)) \times 5 = F(6) + 78 \times 9$$

$$\bullet \mathbf{711} := 12 + 3 \times F(F(F(4)) + 5) = -F(F(6))/7 + F(8) \times F(9)$$

$$\bullet \mathbf{713} := -1 + F(2^3) \times F(4 + 5) = 6 - 7 + F(8) \times F(9)$$

$$\bullet \mathbf{714} := F(12 - 3) \times F(F(4) + 5) = 6 \times 7 \times (8 + 9)$$

$$:= 12 \times 3 \times 4 \times 5 - 6 = (F(7) + 8) \times F(9)$$

$$:= (12 + 34 + 56) \times 7 = F(8) \times F(9)$$

$$\bullet \mathbf{715} := (F(12) + 3 - 4) \times 5 = (6 + 7) \times (F(8) + F(9))$$

$$:= (1 + 2^{3+F(4)}) \times (5 + 6) = F(7) \times (F(8) + F(9))$$

$$\bullet \mathbf{717} := -12 + 3 \times F(4)^5 = F(F(6))/7 + F(8) \times F(9)$$

$$\bullet \mathbf{719} := 1 - 2 + F(3 \times 4) \times 5 = -F(6) + F(7) + F(8) \times F(9)$$

$$\bullet \mathbf{720} := F(12) \times (3 + F(F(4))) = (5 + 67 + 8) \times 9$$

$$:= 12 \times 3 \times 4 \times 5 = F(6) \times (7 \times 8 + F(9))$$

$$\bullet \mathbf{721} := -1 + 2 + F(3 \times 4) \times 5 = 6 + F(7) \times (F(8) + F(9))$$

$$:= 1 + F(2^3) \times F(4 + 5) + 6 = 7 + F(8) \times F(9)$$

$$\bullet \mathbf{722} := 1 \times 2 + F(3 \times 4) \times 5 = F(6) + (F(7) + 8) \times F(9)$$

$$\bullet \mathbf{723} := 1 + 2 + F(3 \times 4) \times 5 = F(F(6)) + 78 \times 9$$

$$\bullet \mathbf{727} := -1 \times 2 + 3 \times F(4)^5 = 6 + 7 + F(8) \times F(9)$$

$$:= 1^2 + F(3 \times 4) \times 5 + 6 = F(7) + F(8) \times F(9)$$

$$\bullet \mathbf{728} := 1 - 2 + 3 \times F(4)^5 = F(6) \times 7 \times (-F(8) + F(9))$$

$$\bullet \mathbf{729} := (12 - 3)^{F(4)} = 56 \times F(7) - 8 + 9$$

$$:= (-1 + 2) \times 3 \times F(4)^5 = F(6) + 7 + F(8) \times F(9)$$

$$\bullet \mathbf{733} := 123 + F(F(4) \times 5) = 6 + F(7) + F(8) \times F(9)$$

$$\bullet \mathbf{735} := -1 + 23 \times F(F(4))^5 = F(6) + F(7) + F(8) \times F(9)$$

$$\bullet \mathbf{736} := 1 \times 23 \times F(F(4))^5 = F(F(6)) + F(7) \times (F(8) + F(9))$$

$$\bullet \mathbf{748} := (-1 + 23) \times F(4 + 5) = (-6 + 7 + F(8)) \times F(9)$$

$$\bullet \mathbf{754} := F(12 + F(3)) \times F(F(4)) = F(F(6) + 7) + F(F(8) - 9)$$

$$:= 12^{F(3)} + F(F(4) \times 5) = 56 \times F(7) - 8 + F(9)$$

- **756** := $12 \times 3 \times F(F(4) + 5) = (6 + 78) \times 9$
- **760** := $(F(12) + F(3) \times 4) \times 5 = F(6) \times (F(7) \times 8 - 9)$
- **768** := $(1 + 23) \times F(F(4))^5 = F(6) \times (7 + 89)$
- **770** := $(12 + F(3)) \times F(F(F(4))) \times 5 = (F(F(6)) - 7) \times (F(8) + F(9))$
- **781** := $-1 + 23 \times F(4 + 5) = -F(6) + 789$
- **782** := $1 \times 23 \times F(4 + 5) = (F(6) + 7 + 8) \times F(9)$
- **783** := $1 + 23 \times F(4 + 5) = -6 + 789$
- **789** := $1 \times 2 \times 3^4 \times 5 - F(F(6)) = 789$
- **810** := $1 \times 2 \times 3^4 \times 5 = F(F(6)) + 789$
- **816** := $12 \times F(3) \times F(4 + 5) = F(6) \times (F(7) + 89)$
- **825** := $F(12 - F(3)) \times F(4) \times 5 = (F(6) + 7) \times (F(8) + F(9))$
- **843** := $-F(12) + F(F(3)^4) = F(-5 + F(F(6))) - F(F(7) + 8 - 9)$
 $\quad := F(12 + 3) + F(F(F(F(4)) + 5)) = F(F(6) + 7) + F(-F(8) + F(9))$
- **848** := $-F(12) + F(F(3)^4) + 5 = 6 \times 7 \times F(8) + F(9)$
- **861** := $123 \times (F(F(4)) + 5) = F(F(6)) \times 7 + F(8) \times F(9)$
- **864** := $F(12) \times (-3 + 4 + 5) = 6 \times (F(F(7)) - 89)$
 $\quad := F(12) \times (3 + F(4)) = (5 + 67) \times (F(8) - 9)$
- **873** := $6 \times 7 \times F(8) - 9 = F(12) + 3 \times F(4)^5$
- **918** := $(1 + 2)^3 \times F(4 + 5) = (6 + F(7) + 8) \times F(9)$
- **931** := $-1 + (2 + F(3)) \times F(F(F(F(4)) + 5)) = -F(F(6)) + (7 + F(8)) \times F(9)$
- **932** := $F(F(1 + 2 \times 3)) \times 4 = (5 - F(6) + 7) \times F(-F(8) + F(9))$
- **936** := $F(12)/F(3) \times F(F(F(4)) + 5) = (6 + 7) \times 8 \times 9$
 $\quad := 12 \times 3 \times (-4 + 5 \times 6) = F(7) \times 8 \times 9$
- **944** := $-1 + F(2^3) \times 45 = F(6) + F(7) \times 8 \times 9$
- **945** := $1 \times F(2^3) \times 45 = (-F(6) + F(7)) \times F(8) \times 9$
- **946** := $1 + F(2^3) \times 45 = -6 + (7 + F(8)) \times F(9)$
- **947** := $F(1^2 \times F(3)^4) - 5 \times F(6) = F(F(7)) + F(8) \times F(9)$
- **952** := $1 + (2 + F(3)) \times F(4)^5 - F(F(6)) = (7 + F(8)) \times F(9)$
- **96** := $1 \times 2 \times (3 + 45) = -6 + F(7) + 89$
- **960** := $F(12)/3 \times 4 \times 5 = F(6) + (7 + F(8)) \times F(9)$
- **973** := $1 + (2 + F(3)) \times F(4)^5 = F(F(6)) + (7 + F(8)) \times F(9)$
- **975** := $-12 + F(F(3)^4) = F(-5 + F(F(6))) - F(7) - 8 + 9$
- **984** := $-1 - 2 + F(F(3)^4) = (F(5 + 6) - 7) \times (F(8) - 9)$
- **985** := $-1 \times 2 + F(F(3)^4) = -5 + (6 + F(7) \times 8) \times 9$

- **986** := $1 - 2 + F(F(3)^4) = F(-5 + F(6) + F(7)) + 8 - 9$
 $= -1 + F(2^{3-4+5}) = (F(6) + F(7) + 8) \times F(9)$
- **987** := $F(12/3 \times 4) = F(-5 + F(6) + F(7)) \times (-8 + 9)$
 $= F(12 + 3 - 4 + 5) = F(6 - 7 + 8 + 9)$
- **988** := $1 + F((2 + F(3)) \times 4) = (5 + F(6)) \times (-F(7) + 89)$
- **989** := $1 \times 2 + F(F(3)^4) = F(-5 + F(F(6))) + F(F(-F(7) + 8 + 9))$
- **990** := $1 + 2 + F(F(3)^4) = (5 + 6) \times (7 \times 8 + F(9))$
 $= (-1 + 23) \times 45 = (6 + F(7) \times 8) \times 9$
- **999** := $12 + F(F(3)^4) = F(-5 + F(F(6))) + F(7) + 8 - 9$

3.2 Decreasing Order

- **2** := $9 - 8 + (7 - 6)^5 = F(F(4)) + 321 \times 0$
- **3** := $9 - (8 - 7)^6 - 5 = F(4) + 321 \times 0$
- **8** := $(9 - 8)^7 + 6 + 5 - 4 = F(3 \times 2) \times 1$
 $= 9 + (8 - 7 - 6)/5 = F(4) - 3 - 2 + 10$
 $= 9 - (8 - 7)^6 = 5 + F(4) + 321 \times 0$
 $= 9 - 8 + 7 = F(6) + 54321 \times 0$
 $= 9 - 8 - 7 + 6 + 5 + 4 = F(3 \times 2) + 1$
- **11** := $9 + F(F(8)/7) = (65 - 43)/2 \times 1$
 $= 6 + 5 \times 43 - 210$
 $= F(9) - 8 - 7 - F(6) = 5 + 4 + 3 - (2 - 1)$
 $= (5 - 4)^{32} + 10$
- **12** := $(9 - 8) \times 7 + 6 - 5 + 4 = F(F(F(3) + 2)) + 10$
 $= F(9) - 87 + 65 = 4 \times 3 \times (2 - 1)$
 $= 4 \times (3 + 21 \times 0)$
 $= (9 + 87)/F(6) = 54 - F(3) \times 21$
 $= 54 - 32 - 10$
 $= 9 + F(8)/7 = (65 - 43)/2 + 1$
 $= -9 + F(8) = 7 + (6 - 54)/3 + 21$
 $= -F(7) + 6 \times 5 - 4 + 3^2 - 10$
- **13** := $98 - 76 - 5 - 4 = F(3 \times 2 + 1)$
 $= F((9 - 8) \times 7) = -6 + 54/3 + 2 - 1$
 $= F(F(6)) \times 5/F(4) - 32 + 10$
 $= F(9) - F(8) = (76 - 5 - 43)/2 - 1$
 $= F(7) + 654321 \times 0$

$$\bullet \mathbf{14} := 9 \times (8 + 76) / 54 = F(3) + 2 + 10$$

$$\bullet \mathbf{16} := -9 + 87 - F(6) - 54 = 3 \times 2 + 10$$

$$\bullet \mathbf{17} := 98 - 76 - 5 = F(4) \times 3 \times 2 - 1$$

$$= F(4) \times 3 - 2 + 10$$

$$:= 9 + F(8) - F(7) = 6 - 5 \times 4 + 32 - 1$$

$$= 6 + 5 - 4 \times (3 - 2) + 10$$

$$\bullet \mathbf{18} := -9 + 87 - 6 - 54 = -3 + 21$$

$$= F(3 \times 2) + 10$$

$$:= (9 + 87 - 6) / 5 = F(4) \times 3 \times 2 \times 1$$

$$= -4 + 32 - 10$$

$$:= 9 \times F(F(8) / 7) = 6 + 54 - F(3) \times 21$$

$$= -65 - 4 + 32 + F(10)$$

$$\bullet \mathbf{19} := 9 + F(8 + 7) / (65 - 4) = -F(3) + 21$$

$$= 3^2 + 10$$

$$:= (9 - 8) \times F(7) + 6 = 54/3 + 2 - 1$$

$$= 54 / (3 \times 2) + 10$$

$$:= F(9) - 8 - 7 = 65 - 43 - 2 + 1$$

$$= 65 - 4 - 32 - 10$$

$$\bullet \mathbf{20} := 98 - 76 - 5 + F(4) = F(F(3 \times 2)) - 1$$

$$:= 98 - F(7) - 65 = 4 \times (3 \times 2 - 1)$$

$$= 4 + (3 \times 2 + 10)$$

$$:= F(9) - F(8) + 7 = 65 - 43 - 2 \times 1$$

$$\bullet \mathbf{21} := 98 - 76 - 5 + 4 = F(3^2 - 1)$$

$$:= F(98/7 - 6) = 54 - 32 - 1$$

$$:= F(9 - 8 + 7) = (65 - 4^3) \times 21$$

$$= F(6) - 5 - 4 + 32 - 10$$

$$\bullet \mathbf{22} := 98 - 7 - 65 - 4 = F(F(3 \times 2)) + 1$$

$$= 32 - 10$$

$$:= -F(9) + 8 \times 7 = 65 - 4^3 + 21$$

$$= (654/3 + 2) / 10$$

$$\bullet \mathbf{23} := 98 - 76 + 5 - 4 = F(3) + 21$$

$$= 3 + 2 \times 10$$

$$:= 9 + F(8) - 7 \times (6 - 5) = 4 - F(3) + 21$$

$$= 43 - 2 \times 10$$

$$:= (-9 + F(8) \times 7) / 6 = 54 - 32 + 1$$

$$= 5 - 4 + 32 - 10$$

$$:= 9 + F(8) - 7 = 65 - 43 + 2 - 1$$

$$= 6 - 5 + 4 - F(3) + 2 \times 10$$

- 24 := $98 - 76 + 5 - F(4) = 3 + 21$
 $\quad := (9 \times (F(8) - 7) - 6)/5 = 4 \times 3 \times 2 \times 1$
 $\quad \quad \quad = (4 + 3) \times 2 + 10$
 $\quad := 9 + 8 + F(7) - 6 = (5 + 4)/3 + 21$

- 25 := $98/7 + 6 + 5 = 4 \times 3 \times 2 + 1$
 $\quad \quad \quad = F(4) + 32 - 10$
 $\quad := F(9) - 8 - 7 + 6 = 5 - 4 + 3 + 21$
 $\quad \quad \quad = 5 + 4 + 3 \times 2 + 10$
 $\quad := -9 + F(8) + F(7) = 65 - 43 + 2 + 1$
 $\quad \quad \quad = 65 - 4 - 3 \times (2 + 10)$

- 26 := $98 - 7 - 65 = F(4 + 3) \times 2 \times 1$
 $\quad \quad \quad = 4 + 32 - 10$
 $\quad := (9 + F(8) \times 7)/6 = 5 \times (4 - 3) + 21$
 $\quad \quad \quad = 54/3 \times 2 - 10$
 $\quad := F(9) - F(8) + F(7) = 65 \times 4/(3^2 + 1)$
 $\quad \quad \quad = F(6) + 5 \times (4 + 32)/10$
 $\quad := F(9) - 8 = (F(7) + 65) \times (4 + 3)/21$
 $\quad \quad \quad = -7 - F(6) - 5 + 4 + 32 + 10$

- 27 := $98 - 76 + 5 = 4 + F(3) + 21$
 $\quad \quad \quad = 4 + 3 + 2 \times 10$
 $\quad := F(9) - 8 + 7 - 6 = 5 + 43 - 21$
 $\quad \quad \quad = 54 \times (3 + 2)/10$
 $\quad := (9 \times F(8))/7 = -6 + 5 + 4 + 3 + 21$
 $\quad \quad \quad = (6 + 5) \times 4 + 3 - 2 \times 10$

- 28 := $F(9) \times (8 - 7) - 6 = (5 + 4) \times 3 + 2 - 1$
 $\quad \quad \quad = 5 + 43 - 2 \times 10$

- 29 := $9 + 8 + F(7) - 6 + 5 = 4 \times F(3) + 21$
 $\quad := F(9) + 8 - 7 - 6 = 5 + 4 \times 3 \times 2 \times 1$
 $\quad \quad \quad = 5 \times 4 - 3 + 2 + 10$
 $\quad := F(9) + 8 - F(7) = 65 - 4 - 32 \times 1$
 $\quad \quad \quad = 6 + 5 - 4 + 32 - 10$

- 30 := $98 - 7 - 65 + 4 = F(F(3) + 2) \times 10$
 $\quad := (9 - 8)^7 \times 6 \times 5 = F(4) \times 3 + 21$
 $\quad \quad \quad = (4 - 3 + 2) \times 10$
 $\quad := 9 + 8 + F(7) = 65 - 4 - 32 + 1$
 $\quad \quad \quad = 65 - 43 - 2 + 10$
 $\quad := 9 + F(8) = 7 + 65 - 43 + 2 - 1$
 $\quad \quad \quad = (7 + F(6)) \times (54/3 + 2)/10$

- 31 := $9 + F(8) + 7 - 6 = 54 - F(3) - 21$
 $= (54 + 32) - F(10)$
 $:= F(9) - F(8)/7 = (654 - 3)/21$
- 32 := $F(9) - 8 + 7 - 6 + 5 = 4^3/2 \times 1$
 $= 4 \times 3 + 2 \times 10$
 $:= 9 + 8 + 7 + F(6) = (5 - 4) \times 32 \times 1$
 $= 54 - 32 + 10$
 $:= F(9) - F(F(8)/7) = 65 - 4 \times 3 - 21$
 $= F(6) + (-5 + 4 + 3) \times (2 + 10)$
- 33 := $9 \times F(8)/7 + 6 = (5 - 4) \times 32 + 1$
 $:= F(9) - 8 + 7 = 6 + 5 + 43 - 21$
- 34 := $9 + 87 - F(6) - 54 = F(3^2) \times 1$
 $:= F(9) \times (8 - 7)^{65} = F(4) + 32 - 1$
 $= 4 \times 3 \times 2 + 10$
 $:= -F(9) - 8 + 76 = 5 - 4 + 32 + 1$
 $:= F(9) \times (8 - 7) = (6 - 5) \times F(4) + 32 - 1$
 $= 65 - 43 + 2 + 10$
- 35 := $9 + 87 - 65 + 4 = F(3^2) + 1$
 $:= F(9) + (8 - 7)^6 = 54 + F(3) - 21$
 $= 54 - 3^2 - 10$
 $:= F(9) + 8 - 7 = F(6) + 5 + 43 - 21$
- 36 := $F(9) + 8 - 7 + 6 + 5 = 4 + 32 \times 1$
 $:= 9 + 8 + F(7) + 6 = 54 + 3 - 21$
 $:= F(9) + F(F(8)/7) = 65 + 4 - 32 - 1$
 $= 6 \times (-5 - 4 + 3 + 2 + 10)$
- 37 := $F(9) - F(8)/7 + 6 = 54/3 \times 2 + 1$
 $= 54 + 3 - 2 \times 10$
 $:= 9 + F(8) + 7 = 65 + 4 - 32 \times 1$
 $= 6 + 5 + 4 + 32 - 10$
- 38 := $9 - 8 + 7 \times 6 - 5 = -4 + F(3) \times 21$
 $= -4 + 32 + 10$
 $:= 9 + 8 + F(7) + F(6) = 5 + 4 \times 3 + 21$
 $= 54 - 3 \times 2 - 10$
- 39 := $9 \times (8 - 7) + 6 \times 5 = F(4 + 3) \times (2 + 1)$
 $= (4 + 3)^2 - 10$
 $:= 9 + (-8 + F(7)) \times 6 = 54/3 + 21$
 $:= F(9) - 8 + F(7) = 6 + 5 - 4 + 32 \times 1$
 $= 65 - 4 - 32 + 10$

$$\begin{aligned}\bullet 40 &:= 9 + (8 + 7 - F(6)) \times 5 - 4 = (F(3) + 2) \times 10 \\ &:= F(9) \times (8 - 7) + 6 = 5 + 4 + 32 - 1 \\ &\quad = 5 + 43 + 2 - 10\end{aligned}$$

$$\begin{aligned}\bullet 41 &:= -9 + 8 + 7 \times 6 = 5 + 4 + 32 \times 1 \\ &\quad = (5 + 43) \times 2 - F(10)\end{aligned}$$

$$\begin{aligned}\bullet 42 &:= 98 - 76 + 5 \times 4 = F(3) \times 21 \\ &\quad = 32 + 10 \\ &:= 987/F(F(6)) - 5 = 43 - 2 + 1 \\ &:= 98 - 7 \times F(6) = 5 + 4 + 32 + 1 \\ &\quad = (5 - 4) \times 32 + 10 \\ &:= F(9) + F(8) - F(7) = 6 + 54 + 3 - 21 \\ &:= F(9) + 8 = 76 - 5 + 4 - 32 - 1\end{aligned}$$

$$\begin{aligned}\bullet 43 &:= F(9) - 8 \times 7 + 65 = 4^3 - 21 \\ &\quad = 43 + 21 \times 0 \\ &:= 9 + F(8) + F(7) = 65 - 43 + 21\end{aligned}$$

$$\begin{aligned}\bullet 44 &:= 98 + 7 - 65 + 4 = F(3^2) + 10 \\ &:= 9 + 8 \times 7 - F(F(6)) = 5 \times 4 + 3 + 21 \\ &\quad = 54 \times (3 - 2) - 10 \\ &:= -9 \times F(8) + F(F(7)) = 6 + 5 + 4 \times 3 + 21 \\ &\quad = (65 + 43)/2 - 10\end{aligned}$$

$$\begin{aligned}\bullet 45 &:= F(9) \times (8 - 7) + 6 + 5 = 43 + 2 \times 1 \\ &\quad = F(4) + 32 + 10 \\ &:= 9 \times (-8 + F(7)) = 6 + 54/3 + 21\end{aligned}$$

$$\begin{aligned}\bullet 46 &:= -98/7 + 6 + 54 = -3^2 + F(10) \\ &:= 98 + F(7) - 65 = 43 + 2 + 1 \\ &\quad = 4 + 32 + 10 \\ &:= -9 - F(8) + 76 = 5 + 43 - 2 \times 1 \\ &\quad = 54/3 \times 2 + 10\end{aligned}$$

$$\begin{aligned}\bullet 47 &:= 9 + (87 + 65)/4 = -F(3 \times 2) + F(10) \\ &:= (9 - 8) \times (7 \times 6 + 5) = F(4^{F(3)})/21 \\ &\quad = -F(4) + (3 + 2) \times 10 \\ &:= 987/F(F(6)) = 5 + 43 - 2 + 1 \\ &:= -9 + 8 \times 7 = F(F(6) - 5)^4 + 32 - 1 \\ &\quad = 65 \times 4 - 3 - 210\end{aligned}$$

$$\begin{aligned}
 \bullet 48 &:= 9 - 8 + 7 \times 6 + 5 = (4 + 3)^2 - 1 \\
 &\quad = F(4) \times (3 \times 2 + 10) \\
 &:= (9 - 8 + 7) \times 6 = (-6 + 54)/3 \times (2 + 1) \\
 &\quad = 65 \times 4 - F(3) - 210 \\
 &:= F(9) + F(8) - 7 = 54 - 3 - 2 - 1 \\
 &\quad = -54 \times 3 + 210
 \end{aligned}$$

$$\begin{aligned}
 \bullet 49 &:= (9 - 8)^7 - 6 + 54 = -3 \times 2 + F(10) \\
 &:= F(9) - 8 - 7 + 6 \times 5 = (4 + 3)^2 \times 1 \\
 &:= (F(9) + 8) \times 7/6 = 54 - 3 - 2 \times 1 \\
 &\quad = 54 + 3 + 2 - 10 \\
 &:= F(9) + 8 + 7 = 6 + 5 \times 4 + F(3) + 21 \\
 &\quad = 6 \times 5 - F(4) + 32 - 10
 \end{aligned}$$

$$\begin{aligned}
 \bullet 50 &:= -F(9) + 8 + 76 = 5 + 43 + 2 \times 1 \\
 &\quad = 54 + 3 \times 2 - 10
 \end{aligned}$$

$$\begin{aligned}
 \bullet 51 &:= (9 + 8 - 7) \times 6 - 5 - 4 = -F(3) - 2 + F(10) \\
 &:= -98/7 + 65 = -4 + F(3^2 + 1) \\
 &\quad = 43 - 2 + 10 \\
 &:= 9 \times 8 - F(7) - F(6) = 5 + 43 + 2 + 1 \\
 &\quad = 54 - 3 + 21 \times 0
 \end{aligned}$$

$$\begin{aligned}
 \bullet 52 &:= -9 + 8 - 7 + 6 + 54 = -F(F(3) + 2) + F(10) \\
 &:= -F(9) + 87 - 6 + 5 = 4 \times F(3 \times 2 + 1) \\
 &\quad = 4^3 - 2 - 10 \\
 &:= -F(9) + 8 + F(7) \times 6 = 54 - 3 + 2 - 1 \\
 &\quad = 54 - F(3 + 21 \times 0)
 \end{aligned}$$

$$\begin{aligned}
 \bullet 53 &:= 9 \times 8 + 7 - 6 - 5 \times 4 = -F(F(F(3) + 2)) + F(10) \\
 &:= 9 - 8 - F(7) + 65 = F(4)^3 \times 2 - 1 \\
 &\quad = 4 - 3 \times 2 + F(10) \\
 &:= 9 \times 8 - F(7) - 6 = 54 - 3 + 2 \times 1 \\
 &\quad = 54 + 3^2 - 10 \\
 &:= -F(9) + 87 = (65 + 43)/2 - 1
 \end{aligned}$$

$$\begin{aligned}
 \bullet 54 &:= 9 \times (8 - 7 + 6) - 5 - 4 = -3 + 2 + F(10) \\
 &:= (9 + 8) \times 7 - 65 = F(4 + 3 \times 2) - 1 \\
 &\quad = 4 + (3 + 2) \times 10
 \end{aligned}$$

- **55** := $9 - 8 - 7 + 65 - 4 = F(3^2 + 1)$
 $= F((3 - 2) \times 10)$
 $:= (9 + 8 - 7) \times 6 - 5 = F(4 \times 3 - 2 \times 1)$
 $= 43 + 2 + 10$
 $:= F(9) + 8 + 7 + 6 = 54 + 3 - 2 \times 1$
 $= 54 - 3^2 + 10$
 $:= F(9 + 8 - 7) = (65 + 43)/2 + 1$
 $:= F(9) + F(8) = 76 - 54 + 32 + 1$
 $= 76 + 5 - 4 - 32 + 10$

- **56** := $9 - 8 + 7 - 6 + 54 = 3 - 2 + F(10)$
 $:= F(9) + 87 - 65 = F(4 + 3 \times 2) + 1$
 $= 4^3 + 2 - 10$

- **57** := $9 \times (8 - 7) - 6 + 54 = F(F(F(3) + 2)) + F(10)$
 $:= 9 + 8 \times 7 - F(6) = 54 + 3 \times (2 - 1)$
 $= 54 + 3 + 21 \times 0$
 $:= -9 + 8 - 7 + 65 = F(4) \times (-F(3) + 21)$
 $= (4 - 3) \times (2 + F(10))$

- **58** := $(9 + 8) \times 7 - 65 + 4 = F(F(3) + 2) + F(10)$
 $:= (9 - 8) \times (-7 + 65) = F(4) + F(3^2 + 1)$
 $= 4 - 3 + 2 + F(10)$
 $:= 9 \times 8 + 7 - F(F(6)) = 54 + 3 + 2 - 1$
 $= 54 - 3 \times 2 + 10$

- **59** := $(9 + 8) \times 7 - 6 - 54 = F(3) + 2 + F(10)$
 $:= 9 \times 8 - F(7) = 65 - 4 - 3 + 2 - 1$

- **60** := $98/7 - F(6) + 54 = (3 \times 2) \times 10$
 $:= (9 + 87)/F(6) \times 5 = -F(4) + 3 \times 21$
 $= 4 \times 3/2 \times 10$

- **61** := $(9 - 8)^7 \times (65 - 4) = 3 \times 2 + F(10)$
 $:= 98 - 7 - 6 \times 5 = 4^3 - 2 - 1$
 $= 4 \times 3/2 + F(10)$
 $:= F(9 + 8 - 7) + 6 = 54 + 3 \times 2 + 1$
 $= 5 + 4^3 + 2 - 10$

- **62** := $-9/(F(8)/7) + 65 = 4^3 - 2 \times 1$
 $= F(4 \times 3)/2 - 10$
 $:= F(9) + F(8) + F(7) - 6 = 54 + 3^2 - 1$
 $= 5 \times 4 + 32 + 10$
 $:= F(9) + F(8) + 7 = 6 + 54 + 3 - 2 + 1$
 $= -6 + 54 + F(3) + 2 + 10$

$$\begin{aligned}\bullet 63 &:= 98 + F(7) + 6 - 54 = 3 \times 21 \\ &:= 98 - (F(7) - 6) \times 5 = 4^3 - 2 + 1 \\ &\quad = 43 + 2 \times 10\end{aligned}$$

$$\begin{aligned}\bullet 64 &:= F(9) + 8 + 76 - 54 = 3^2 + F(10) \\ &:= 9 - F(8) + 76 = 5 - 4 + 3 \times 21 \\ &\quad = 5 \times 4 \times 32/10\end{aligned}$$

$$\begin{aligned}\bullet 65 &:= 9 \times 8 - F(7) + 6 = 5 - F(4) + 3 \times 21 \\ &\quad = 54 + 3 - 2 + 10\end{aligned}$$

$$\begin{aligned}\bullet 66 &:= (9 - 8)^7 + 65 = 4^3 + 2 \times 1 \\ &\quad = F(4) \times (32 - 10) \\ &:= (9 + F(F(8)/7)) \times 6 = 5 + 4^3 - 2 - 1\end{aligned}$$

$$\bullet 67 := 9 \times 8 - F(7) + F(6) = 5 + 4^3 - 2 \times 1$$

$$\begin{aligned}\bullet 68 &:= 9 \times 8 + 7 - 6 - 5 = F(F(4) \times 3) \times 2 \times 1 \\ &\quad = 4 \times (-3 + 2 \times 10) \\ &:= F(9) - 8 + 7 \times 6 = 5 + 4^3 - 2 + 1 \\ &\quad = 5 + 43 + 2 \times 10 \\ &:= F(9) + F(8) + F(7) = 6 - 5 + 4 + 3 \times 21 \\ &\quad = F(6 + 5) - 4 + 3 - 2 \times 10\end{aligned}$$

$$\begin{aligned}\bullet 69 &:= 9 - F(8) + 76 + 5 = F(4) \times (F(3) + 21) \\ &\quad = (4 + 3) \times 2 + F(10) \\ &:= F(9) + 8 \times 7 - F(F(6)) = 5 + 43 + 21 \\ &\quad = 54 + 3 + 2 + 10\end{aligned}$$

$$\begin{aligned}\bullet 70 &:= 9 \times (8 + 7) - 65 = F(F(4)) \times (F(3^2) + 1) \\ &\quad = (F(4) \times 3 - 2) \times 10 \\ &:= 98 - 7 - F(F(6)) = 5 \times (4 + 3) \times 2 \times 1 \\ &\quad = 54 + 3 \times 2 + 10 \\ &:= -F(9) + 8 \times F(7) = 65 - 4 + 3^2 \times 1 \\ &\quad = 65 - 4 - 3 + 2 - 10\end{aligned}$$

$$\begin{aligned}\bullet 71 &:= (9 - 8) \times (76 - 5) = F(4 \times 3)/2 - 1 \\ &\quad = (F(4) \times 3)^2 - 10\end{aligned}$$

$$\begin{aligned}\bullet 72 &:= 9 \times (F(8) - F(7)) = 6 \times 5 + 43 - 2 + 1 \\ &\quad = 65 - 4 + 3 - 2 + 10\end{aligned}$$

$$\begin{aligned}\bullet 73 &:= 9 - 8 + 7 + 65 = F(4 \times 3)/2 + 1 \\ &\quad = 4 \times 32 - F(10) \\ &:= 9 \times 8 + 7 - 6 = 54 - F(3) + 21\end{aligned}$$

$$\bullet 74 := 9 \times (8 - 7) + 65 = F(F(4)) \times 32 + 10$$

$$:= -F(9) + 87 + F(F(6)) = 5 \times F(4) \times (3 + 2) - 1 \\ = (5 - F(4)) \times 32 + 10$$

$$\bullet 75 := 98 + 7 - 6 \times 5 = 4 \times (3 + 2) + F(10)$$

$$\bullet 76 := 98 - 76 + 54 = F(F(3 \times 2)) + F(10) \\ := 9 \times (8 + 7 - 6) - 5 = 4 \times (-F(3) + 21) \\ = 43 \times 2 - 10$$

$$\bullet 77 := (9 - 8) \times 7 \times (6 + 5) = -F(4) + F(3 \times 2) \times 10$$

$$:= 9 - 8 + 76 = 54 + F(3) + 21 \\ = 54 - 32 + F(10)$$

$$\bullet 78 := 9 - 8 + 7 \times (6 + 5) = F(F(4) \times 3) \times 2 + 10$$

$$:= (9 - 8) \times F(7) \times 6 = 54 + 3 + 21 \\ := -9 + 87 = 65 - 4 \times F(3) + 21$$

$$\bullet 79 := 98/7 + 65 = 4 \times 3 \times 2 + F(10)$$

$$:= 98 - F(7) - 6 = (5 + 4)^{F(3)} - 2 \times 1 \\ = -5 + 4^3 + 2 \times 10$$

$$\bullet 80 := 98 - (7 + 65)/4 = F(3 \times 2) \times 10$$

$$:= 98 - 7 - 6 - 5 = ((F(4) \times 3)^2) - 1 \\ = F(4 \times 3/2) \times 10 \\ := (9 + 8 - 7) \times F(6) = 54 \times 3/2 - 1 \\ = 5 \times 4 + 3 \times 2 \times 10$$

$$\bullet 81 := (9 - 8) \times 76 + 5 = (F(4) \times 3)^2 \times 1$$

$$:= 9^{F(8)/7} = -6 + 54 + 32 + 1 \\ = F(6) \times F(5 + F(4)) - 32 - F(10)$$

$$\bullet 82 := 9 - 8 + 76 + 5 = (F(4) \times 3)^2 + 1$$

$$= F(4 \times 3)/2 + 10 \\ := F(9) - 8 + 7 \times F(6) = 54 \times 3/2 + 1$$

$$\bullet 83 := 9 + 87 - F(6) - 5 = 4 \times F(F(3 \times 2)) - 1$$

$$= -4 + 32 + F(10) \\ := 98 - 7 - F(6) = 5 \times 4 + 3 \times 21 \\ = 5^{F(4)} - 32 - 10$$

$$\bullet 84 := F(9) - 8 - 7 + 65 = 4 \times F(3^2 - 1)$$

$$= (4 + 3) \times (2 + 10) \\ := (-9 + F(8)) \times 7 = (6 + 54 + 3) + 21 \\ = 65 + 4 + 3 + 2 + 10$$

$$\bullet 85 := 98 - F(7) = 65 - 4 + 3 + 21$$

$$\bullet 86 := -9 + 87 + F(6) = 54 + 32 \times 1$$

$$\bullet 87 := 9 \times 8 + 7 + F(6) \times (5 - 4) = 32 + F(10)$$

$$:= 98 - F(7) + F(F(6) - 5) = 43 \times 2 + 1$$

$$:= 9 \times 8 + 7 + F(6) = 54 + 32 + 1$$

$$\bullet 88 := 9 + 8 + 76 - 5 = 4 \times (F(F(3 \times 2)) + 1)$$

$$= 4 \times (32 - 10)$$

$$:= 9 + 87 - F(6) = F(5 + 4 \times 3/2) - 1$$

$$= 54 \times F(3) - 2 \times 10$$

$$\bullet 89 := F(9) \times (8 + 7 + 6) - 5^4 = F(3 - 2 + 10)$$

$$:= 9 + 8 + 7 + 65 = F(4 + 3 \times 2 + 1)$$

$$= (4 \times 3)^2 - F(10)$$

$$:= F(9) - F(8) + 76 = 54 + F(3^2) + 1$$

$$= 5 + 4^3 + 2 \times 10$$

$$:= F(9 + F(F(8)/7)) = 6 + 5 \times 4 + 3 \times 21$$

$$\bullet 90 := 98 - 7 - 6 + 5 = F(F(4 + 3) - 2) + 1$$

$$= (4 + 3 + 2) \times 10$$

$$:= F(9) + 8 \times 7 = (6 + 54) \times 3/2 \times 1$$

$$= 6 \times 5 + 4 + 3 - 2 + F(10)$$

$$\bullet 91 := 98 - 7 \times (6 - 5) = 4 + 32 + F(10)$$

$$:= 98 - F(7) + 6 = 5 + 43 \times 2 \times 1$$

$$= 54 \times 3/2 + 10$$

$$\bullet 92 := 98 - 7 + 6 - 5 = 4 \times (F(3) + 21)$$

$$= 4 \times (3 + 2 \times 10)$$

$$:= (-9 + F(8)) \times 7 + F(6) = 5 + 43 \times 2 + 1$$

$$\bullet 93 := 98 \times (7 - 6) - 5 = F(4) \times (32 - 1)$$

$$= F(4) + 3^2 \times 10$$

$$:= 9 + 8 + 76 = 5^{F(4)} - 32 \times 1$$

$$= -5 \times 4 + 3 + 2 \times F(10)$$

$$\bullet 94 := F(9) \times F(8)/7 - F(6) = 5^{F(4)} - 32 + 1$$

$$= (54 - F(3)) \times 2 - 10$$

$$\bullet 95 := 9 + 87 - 6 + 5 = F(4) \times 32 - 1$$

$$:= -9 + 8 \times F(7) = 65 - F(4) + 32 + 1$$

$$= -6 + 5 + 4 \times 3 \times (-2 + 10)$$

$$\bullet 96 := F(9) + 8 \times 7 + 6 = (5 + 43) \times 2 \times 1$$

$$= 54 + 32 + 10$$

- **97** := $98 - (7 - 6)^5 = F(4) \times 32 + 1$
 $= 98 - 7 + 6 = (5 + 43) \times 2 + 1$
 $= F(5 \times F(F(4))) + 32 + 10$
- **98** := $9 + 8 + 76 + 5 = -4 \times 3 + 2 \times F(10)$
 $= 98 \times (7 - 6) = 5 + F(4) \times (32 - 1)$
 $= -5 - 4 - 3 + 2 \times F(10)$
- **99** := $98 + (7 - 6)^5 = F(4) \times (32 + 1)$
- **100** := $(98/7 + 6) \times 5 = 43 + 2 + F(10)$
 $= 9 \times 8 + 7 + F(F(6)) = 5 \times (-4 + 3 + 21)$
 $= (5 + 4 + 3 - 2) \times 10$
- **101** := $9 + F(8) + 76 - 5 = F(4) \times F(3^2) - 1$
 $= -43 + F(2 + 10)$
 $= -9 + 8 \times F(7) + 6 = (54 - 3) \times 2 - 1$
 $= 5 + 43 \times 2 + 10$
- **102** := $9 + 87 + 6 = (54 - 3) \times (2 \times 1)$
 $= -4 + F(3) \times (-2 + F(10))$
 $= 98 - 7 + 6 + 5 = F(F(4) \times 3) \times (2 + 1)$
 $= -54 \times F(3) + 210$
 $= F(9) \times F(8)/7 = (65 + 4) + 32 + 1$
 $= -65 - 43 + 210$
- **103** := $98 \times (7 - 6) + 5 = F(4) \times F(3^2) + 1$
 $= -4 - 3 + 2 \times F(10)$
 $= 98 + F(7) - F(6) = (54 - 3) \times 2 + 1$
 $= 5^{F(4)} - 32 + 10$
- **104** := $98 + 7 - 6 + 5 = (4 + 3)^2 + F(10)$
 $= 9 + 87 + F(6) = 5 + F(4) \times (32 + 1)$
 $= 54 + (3 + 2) \times 10$
- **105** := $98 + 7 \times (6 - 5) = (F(4) + F(3)) \times 21$
 $= 5 + 43 + 2 + F(10)$
 $= 98 + F(7) - 6 = 5 \times (4 - 3) \times 21$
- **106** := $9 + (8 + 76 \times 5)/4 = F(3) \times (-2 + F(10))$
 $= 98 + 7 + 6 - 5 = F(4) \times 32 + 10$
 $= 9 + F(8) + 76 = 54 \times F(3) - 2 \times 1$
 $= (5 + 43) \times 2 + 10$
- **107** := $9 \times (8 + 7) - F(6) - 5 \times 4 = -3 + 2 \times F(10)$
 $= 9 + 87 + 6 + 5 = -F(4) + F(F(F(3) + 2)) \times F(10)$
 $= 9 + 8 \times F(7) - 6 = 5^{F(4)} + 3 - 21$
 $= 5 \times 4 + 32 + F(10)$

$$\begin{aligned}\bullet \mathbf{108} &:= (98 - 76 + 5) \times 4 = -F(3) + 2 \times F(10) \\ &:= 9 \times F(F(8)/7) \times 6 = 54 \times (3 - 2 + 1) \\ &= 54 - 3 + 2 + F(10)\end{aligned}$$

$$\bullet \mathbf{109} := 9 \times 8 + 7 + 6 \times 5 = -4 + 3 + 2 \times F(10)$$

$$\begin{aligned}\bullet \mathbf{110} &:= 98 + 7 + 6 - 5 + 4 = F(F(F(3) + 2)) \times F(10) \\ &:= (98 - 76) \times 5 = F(F(4)) \times F(3^2 + 1) \\ &= (F(4 + 3) - 2) \times 10 \\ &:= F(9) \times F(8)/7 + F(6) = 5 \times (43 - 21)\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{111} &:= 98 + F(7) \times (6 - 5) = 4 - 3 + 2 \times F(10) \\ &:= 98 + 7 + 6 = 54 \times F(3) + 2 + 1 \\ &= 5 + F(4) \times 32 + 10 \\ &:= 98 + F(7) = 65 + 43 + 2 + 1 \\ &= 65 + 4 + 32 + 10\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{112} &:= 98 + 7 + 6 + 5 - 4 = F(3) + 2 \times F(10) \\ &:= -9 + 8 \times 7 + 65 = 4 - F(3) + 2 \times F(10) \\ &:= 98/7 \times F(6) = (54 + F(3)) \times 2 \times 1 \\ &= -5 + 4 + 3 + 2 \times F(10)\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{113} &:= 9 + 8 + 76 + 5 \times 4 = 3 + 2 \times F(10) \\ &:= F(9) + 8 + 76 - 5 = F(F(F(4)) + F(3)) + 2 \times F(10) \\ &:= 9 + 8 \times F(7) = F(6) \times (5 \times 4 - 3 \times 2) + 1\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{114} &:= (-9 + (87 + 6) \times 5)/4 = F(3) \times (2 + F(10)) \\ &:= F(9) + 8 + 7 + 65 = F(4 + 3)^2 - F(10)\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{115} &:= 98 - F(7) + 6 \times 5 = F(4) + F(3) + 2 \times F(10) \\ &:= F(9) + 87 - 6 = (54 + 3) \times 2 + 1 \\ &= 5 \times (43 - 2 \times 10)\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{116} &:= 98 + 7 + 6 + 5 = 4 + F(3) + 2 \times F(10) \\ &:= -9 + 8 \times F(7) + F(F(6)) = 5^{F(4)} - 3^2 \times 1 \\ &= 5 + 4 - 3 + 2 \times F(10)\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{117} &:= 9 \times (8 \times (7 - 6) + 5) = 4 + 3 + 2 \times F(10) \\ &:= 98 + F(7) + 6 = 54 + 3 \times 21\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{118} &:= 98 + 7 + F(6) + 5 = 4 \times 32 - 10 \\ &:= F(9) + 8 + 76 = (-5 + 4^3) \times 2 \times 1\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{119} &:= 9 \times 8 + 7 \times 6 + 5 = F(4) \times 3 + 2 \times F(10) \\ &:= (9 + 8) \times (F(7) - 6) = -5 + 4 \times (32 - 1) \\ &= (5 - F(4)) \times 32 + F(10)\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{120} &:= F(9 + 8 - 7) + 65 = (4 + F(3)) \times 2 \times 10 \\ &:= 9 \times (F(8) - 7) - 6 = 5 \times 4 \times 3 \times 2 \times 1 \\ &= (-5 \times 4 + 32) \times 10\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{121} &:= 98 - 7 + 6 \times 5 = 4^3 + 2 + F(10) \\ &:= 9 + 8 + F(7) \times F(6) = 5 \times 4 \times 3 \times 2 + 1 \\ &:= F(9) + 87 = F(6 + 5 + 4) / (3 + 2) - 1 \\ &= 65 + (4 + 3) \times (-2 + 10)\end{aligned}$$

$$\bullet \mathbf{122} := 98 + F(7) + 6 + 5 = 4 \times 3 + 2 \times F(10)$$

$$\begin{aligned}\bullet \mathbf{123} &:= F(9) + 8 + 76 + 5 = F(4 \times 3) - 21 \\ &:= F(9 + F(8) / 7) - F(F(6)) = F(5 + 4) \times 3 + 21 \\ &= 5 + 4 \times 32 - 10\end{aligned}$$

$$\bullet \mathbf{124} := F(9) + (8 + 7) \times 6 = 5^4 / (3 + 2) - 1$$

$$\bullet \mathbf{125} := 9 \times (F(8) - 7) - 6 + 5 = (F(4) + F(3))^{2+1}$$

$$\begin{aligned}\bullet \mathbf{126} &:= 9 + 87 + 6 \times 5 = (4 + F(3)) \times 21 \\ &= F(4) \times (32 + 10) \\ &:= 98 + 7 + F(F(6)) = (5 + 4 - 3) \times 21 \\ &:= 9 \times (F(8) - 7) = 65 + 4^3 - 2 - 1 \\ &= 6 \times 5 + 43 \times 2 + 10\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{127} &:= 9 \times (F(8) - 7) + 6 - 5 = 4 \times 32 - 1 \\ &:= F(9) + 87 + 6 = 5^{F(4)} + 3 - 2 + 1 \\ &= -5 + F(4 \times 3) - 2 - 10\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{128} &:= F(9) - 8 + F(7) + F(6 + 5) = 4 \times 32 \times 1 \\ &:= 9 \times 8 + 7 \times F(6) = 5^{F(4)} + 3 \times (2 - 1) \\ &= 54 \times F(3) + 2 \times 10\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{129} &:= F(9) + (8 + 7) \times 6 + 5 = 43 \times (2 + 1) \\ &:= 9 \times (8 + 7) - 6 = 54 \times F(3) + 21\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{130} &:= -9 + F(8) \times 7 - F(6) = 5 \times F(4 + 3) \times 2 \times 1 \\ &= 5 \times 4 \times 3 \times 2 + 10\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{131} &:= 9 \times F(8) + 7 - 65 = -F(4 + 3) + F(2 + 10) \\ &:= F(9) + F(8) + 76 = 5 + (4 + F(3)) \times 21 \\ &= (-5 + 43) \times 2 + F(10) \\ &:= F(-9 + F(8)) - F(7) = 6 \times (54 - 32) - 1\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{132} &:= F(9) + 87 + 6 - 5 = 4 \times (32 + 1) \\ &:= 9 \times (F(8) - 7) + 6 = 5 + 4 \times 32 - 1 \\ &= -5 + F(4)^3 + 2 \times F(10)\end{aligned}$$

$$\bullet \mathbf{133} := 9 \times F(8) - 7 \times F(6) = 5 + 4 \times 32 \times 1$$

$$\bullet \mathbf{134} := 9 \times (F(8) - 7) + F(6) = 5 + 4 \times 32 + 1$$

$$\begin{aligned}\bullet \mathbf{135} &:= 98 + 7 + 6 \times 5 &= 4 \times F(3^2) - 1 \\ &:= 9 + (8 + F(7)) \times 6 &= 5^{F(4)} + 3^2 + 1 \\ &&= 5^4 / (3 + 2) + 10 \\ &:= 9 \times (8 + 7) &= -6 + 54 \times 3 - 21 \\ &&= (-6 + 5 \times F(4)) \times (3 + 2 + 10)\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{136} &:= (98 \times 7 - 6) / 5 &= 4 \times F(3^2) \times 1 \\ &&= F(4 \times 3) + 2 - 10 \\ &:= F(9 + F(8)) / 7 - F(6) &= -5 + F(4 \times 3) - 2 - 1 \\ &&= (5 + 4 \times 3) \times (-2 + 10)\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{137} &:= 9 \times 8 + (7 + 6) \times 5 &= 4 \times F(3^2) + 1 \\ &&= F(4)^3 + 2 \times F(10) \\ &:= F(-9 + F(8)) - F(7) + 6 &= 5 + 4 \times (32 + 1) \\ &:= F(-9 + F(8)) - 7 &= 65 + 4 \times (-3 + 21) \\ &&= 6 - 5 + F(4 \times 3) + 2 - 10\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{138} &:= F(9) + 8 + 7 + F(6 + 5) &= 4 \times 32 + 10 \\ &:= (9 + F(8) - 7) \times 6 &= (5 + 4^3) \times 2 \times 1 \\ &:= -9 + F(8) \times 7 &= (65 + 4) \times (3 - 2 + 1) \\ &&= 6 \times (5 - 4 + 32 - 10)\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{139} &:= -9 + F(8) \times 7 + 6 - 5 &= -F(4) - F(3) + F(2 + 10) \\ &:= F(9) + (-8 + F(7)) \times F(F(6)) &= 5 \times (-4 + 32) - 1\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{140} &:= (-F(9) + 8 \times 7 + 6) \times 5 &= 4 \times (F(3^2) + 1) \\ &&= (4 + 3) \times 2 \times 10\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{141} &:= 9 \times 8 + 7 + 65 - F(4) &= -3 + F(2 + 10) \\ &:= (9 + 87 \times F(6)) / 5 &= F(4 \times 3) - 2 - 1 \\ &&= 43 \times 2 + F(10) \\ &:= 9 \times (8 + 7) + 6 &= 54 \times 3 - 21 \\ &&= 54 + 32 + F(10)\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{142} &:= (9 - 87) \times 6 + F(5 \times F(4)) &= -F(3) + F(2 + 10) \\ &:= -9 + 8 + F(7) \times (6 + 5) &= F(4 \times 3) - 2 \times 1 \\ &:= F(9) + 87 + F(F(6)) &= -5 + (4 + 3) \times 21 \\ &&= 54 \times 3 - 2 \times 10\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{143} &:= 9 \times (8 + 7) + F(6) &= 5^{F(4)} - 3 + 21 \\ &&= 5 + 4 \times 32 + 10\end{aligned}$$

$$\bullet \mathbf{144} := 9 + 87 - 6 + 54 = F(F(F(3) + 2)) + 10$$

$$\begin{aligned} &:= F(9 + F(8)/7) = 6 \times (5 + 43)/2 \times 1 \\ &\quad = (65 + 4 - F(3)) \times 2 + 10 \end{aligned}$$

$$\begin{aligned} &:= F(-9 + F(8)) = (7 - 6) \times (5 + F(4)) \times (-3 + 21) \\ &\quad = (-76 + 54) \times 3 + 210 \end{aligned}$$

$$\bullet \mathbf{145} := 98 + 7 \times 6 + 5 = (4 \times 3)^2 + 1$$

$$\begin{aligned} &\quad = 4 - 3 + F(2 + 10) \end{aligned}$$

$$:= F(-9 + F(8)) - 7 + F(6) = 5 \times (-4 + 32 + 1)$$

$$\bullet \mathbf{146} := 98 + (F(7) - 6 + 5) \times 4 = F(3) + F(2 + 10)$$

$$\begin{aligned} &:= 9 \times (8 + 7) + 6 + 5 = F(4 \times 3) + 2 \times 1 \\ &\quad = -4^3 + 210 \end{aligned}$$

$$\begin{aligned} &:= F(9) + 8 + F(7) \times F(6) = 5 + F(4 \times 3) - 2 - 1 \\ &\quad = 5 + 43 \times 2 + F(10) \end{aligned}$$

$$\bullet \mathbf{147} := 9 + 8 + 76 + 54 = 3 + F(2 + 10)$$

$$:= 98 + 7^{F(F(6)-5)} = (4 + 3) \times 21$$

$$:= 9 \times F(8) - 7 \times 6 = (5 + 4 - F(3)) \times 21$$

$$\bullet \mathbf{148} := 9 \times (8 + 7) + F(6) + 5 = F(F(4)) + F(3) + F(2 + 10)$$

$$\begin{aligned} &:= 9 \times 8 + 76 = 5 + (4 \times 3)^2 - 1 \\ &\quad = 5^{F(4)} - 32 + F(10) \end{aligned}$$

$$\bullet \mathbf{149} := F(9) + 8 \times (7 + F(6)) - 5 = F(F(4)) + 3 + F(2 + 10)$$

$$:= F(9) \times (-8 + F(7)) - F(F(6)) = 5^{F(4)} + 3 + 21$$

$$\bullet \mathbf{150} := 98 - F(7) + 65 = F(4) \times (3 + 2) \times 10$$

$$\begin{aligned} &:= 9 \times 8 + F(7) \times 6 = 5 + (4 \times 3)^2 + 1 \\ &\quad = 54 \times 3 - 2 - 10 \end{aligned}$$

$$\bullet \mathbf{151} := F(9) + 87 + 6 \times 5 = 4 + 3 + F(2 + 10)$$

$$\begin{aligned} &:= F(-9 + F(8)) + F(7) - 6 = 5 + F(4 \times 3) + 2 \times 1 \\ &\quad = 5 - 4^3 + 210 \end{aligned}$$

$$\begin{aligned} &:= F(-9 + F(8)) + 7 = 65 + 43 \times 2 \times 1 \\ &\quad = F(6) + 5 + 4 \times 32 + 10 \end{aligned}$$

$$\bullet \mathbf{152} := (9 - 8) \times (7 \times F(F(6)) + 5) = F(4 \times 3) - 2 + 10$$

$$\begin{aligned} &:= (F(9) - 8 - 7) \times F(6) = (5 + 4 + 3) \times 21 \\ &\quad = (5 + F(4)) \times (3^2 + 10) \end{aligned}$$

$$\bullet \mathbf{153} := 9 \times 8 + 76 + 5 = 43 + 2 \times F(10)$$

$$\begin{aligned} &:= 9 + F(F(F(8)/7) \times 6) = (54 - 3) \times (2 + 1) \\ &\quad = -54 - 3 + 210 \end{aligned}$$

$$\bullet \mathbf{154} := 98 + 7 \times F(6) = 5 \times (-F(4) + F(3^2)) - 1 \\ = 54 \times 3 + 2 - 10$$

$$\bullet \mathbf{155} := F(9) + 8 \times 7 + 65 = -4 + 3 \times (-2 + F(10)) \\ := -9 \times 8 + F(F(7)) - 6 = 5 \times (4 + 3^{2+1}) \\ = 5 \times (43 - 2 - 10)$$

$$\bullet \mathbf{156} := 98 - 7 + 65 = F(4 + 3) \times (2 + 10) \\ := 9 \times 8 \times F(7)/6 = 5^{F(4)} + 32 - 1 \\ = 5 + F(4) \times 32 + F(10) \\ := 9 + F(8) \times 7 = (F(6) + 5) \times 4 \times 3 \times (2 - 1) \\ = 65 + 4 + 32 + F(10)$$

$$\bullet \mathbf{157} := (9 + F(8) \times 7) + 6 - 5 = F(4 + 3) + F(2 + 10) \\ := F(F(9) - F(8)) - 76 = 5^{F(4)} + 32 \times 1 \\ := F(-9 + F(8)) + F(7) = (65 + F(4 + 3)) \times 2 + 1 \\ = 6 + 5 - 4^3 + 210$$

$$\bullet \mathbf{158} := F(-9 + F(8)) - 7 + F(F(6)) = 5^{F(4)} + 32 + 1 \\ = -54 + F(3) + 210$$

$$\bullet \mathbf{159} := 98 + 7 \times F(6) + 5 = F(4 + 3)^2 - 10 \\ := -9 + (F(8) + 7) \times 6 = 54 \times 3 - 2 - 1 \\ = -54 + 3 + 210 \\ := F(9) + 8 \times 7 + 65 + 4 = 3 \times (-2 + F(10))$$

$$\bullet \mathbf{160} := 9 + 8 + F(7) \times (6 + 5) = 4 \times F(3) \times 2 \times 10 \\ := F(9) + (8 + F(7)) \times 6 = 54 \times 3 - 2 \times 1$$

$$\bullet \mathbf{161} := 9 + 87 + 65 = F(F(4)) + 3 \times (-2 + F(10)) \\ := 9 + 8 \times (F(7) + 6) = 54 \times 3 - 2 + 1 \\ := -9 \times 8 + F(F(7)) = 65 + 4 \times (3 + 21) \\ = 65 + 43 \times 2 + 10$$

$$\bullet \mathbf{162} := 9 \times (8 + 7) \times 6/5 = F(4) - 3 \times (2 - F(10)) \\ := 9 + (F(8) \times 7) + 6 = 54 \times 3 \times (2 - 1) \\ = 54 \times 3 + 21 \times 0$$

$$\bullet \mathbf{163} := 98 + (7 + 6) \times 5 = 4 + 3 \times (-2 + F(10)) \\ := (F(9) - F(8)) \times F(7) - 6 = 54 \times 3 + 2 - 1 \\ = -5 + 4 \times (32 + 10)$$

$$\bullet \mathbf{164} := -9 + (F(8) + 7) \times 6 + 5 = F(4 \times 3) + 2 \times 10 \\ := 9 + F(8) \times 7 + F(6) = 54 \times 3 + 2 \times 1$$

$$\bullet \mathbf{165} := 98 + 76 - 5 - 4 = F(F(3) + 2) \times F(10) \\ := F(9) + (8 + F(7)) \times 6 + 5 = F(4 \times 3) + 21 \\ := F(9 + F(8)/7) + F(F(6)) = 5 \times (4 \times 3 + 21)$$

$$\begin{aligned}\bullet \mathbf{167} &:= -9 \times 8 + F(F(7)) + 6 = 5^{F(4)} + F(3) \times 21 \\ &\quad = 5^{F(4)} + 32 + 10 \\ &:= 9 \times 8 + (F(7) + 6) \times 5 = -43 + 210\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{168} &:= 9 \times 8 \times 7 / (F(6) - 5) = 4 \times F(3) \times 21 \\ &\quad = 4 \times (32 + 10) \\ &:= F(9 - 8 + 7) \times F(6) = (-5 + F(4 + 3)) \times 21\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{169} &:= 98 + 76 - 5 = F(4 + 3)^2 \times 1 \\ &:= (F(9) - F(8)) \times (7 + 6) = (5 + 4 \times F(3))^2 \times 1 \\ &\quad = 5^{F(4)} + F(3^2) + 10 \\ &:= (F(9) - F(8)) \times F(7) = F(6) \times 5 + 43 \times (2 + 1) \\ &\quad = (F(6) + 5) \times F(4 + 3 + 21 \times 0)\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{170} &:= 98 + 7 + 65 = F(4 + 3)^2 + 1 \\ &:= 9 \times F(8) - F(7) - 6 = 5 \times (F(4) + 32 - 1) \\ &\quad = 5 \times (4 + 32) - 10 \\ &:= F(9) \times (-8 + F(7)) = 6 + 54 \times 3 + 2 \times 1 \\ &\quad = F(6) - 5 - 43 + 210\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{171} &:= -F(9) - 8 + 7 \times 6 \times 5 + F(4) = 3 \times (2 + F(10)) \\ &:= 9 \times (87 + F(6))/5 = F(4)^3 + F(2 + 10) \\ &:= 9 \times (-F(F(8)/7) + F(F(6))) = (54 + 3) \times (2 + 1) \\ &\quad = (5 - 4) \times 3 \times (2 + F(10))\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{172} &:= -F(9) - F(8) + F(F(7)) - 6 = 5 \times F(F(4) \times 3) + 2 \times 1 \\ &\quad = 5 - 43 + 210\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{173} &:= 98 + (7 + F(6)) \times 5 = F(F(4)) + 3 \times (2 + F(10)) \\ &:= F(9) + F(8) \times 7 - F(6) = 5 + 4 \times F(3) \times 21 \\ &\quad = 5 + 4 \times (32 + 10)\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{174} &:= -F(9) + 8 \times (F(7) + F(6) + 5) = 4^3 + 2 \times F(10) \\ &:= 98 + 76 = 5 \times (F(4) + 32) - 1 \\ &\quad = (54 \times 3) + (2 + 10)\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{175} &:= 98 + 7 \times (6 + 5) = 4 + 3 \times (2 + F(10)) \\ &:= 9 \times F(8) + 7 - F(F(6)) = 5 \times (4 + 32 - 1) \\ &\quad = 5 \times (43 + 2 - 10)\end{aligned}$$

$$\begin{aligned}\bullet \mathbf{176} &:= 98 + F(7) + 65 = 4 \times (F(3^2) + 10) \\ &:= 98 + F(7) \times 6 = 5 \times (F(4) + 32) + 1 \\ &\quad = (5 \times 4 + F(3)) \times (-2 + 10) \\ &:= 9 \times F(8) - F(7) = (6 + 5) \times 4 \times (3 + 2 - 1) \\ &\quad = 6 \times 5 - 4^3 + 210\end{aligned}$$

$$\bullet \mathbf{177} := (9 + 876)/5 = F(4) \times (F(3) + 2 + F(10)) \\ := 9 + (F(8) + 7) \times 6 = (-5 + 4^3) \times (2 + 1)$$

$$\bullet \mathbf{178} := F(9) + F(8 - 7 + 6 + 5) = F(4 + 3^2) - F(10) \\ := -F(9) - F(8) + F(7 + 6) = F(5 + 4 + F(3)) \times 2 \times 1 \\ = -5 + 4 \times 32 + F(10) \\ := -F(9) - F(8) + F(F(7)) = (6 + 54) \times 3 - 2 \times 1 \\ = 6 + 5 - 43 + 210$$

$$\bullet \mathbf{179} := 98 + 76 + 5 = F(4 + 3)^2 + 10$$

$$\bullet \mathbf{180} := 98 - 7 + F(6 + 5) = F(4) \times 3 \times 2 \times 10 \\ := (9 + 8 + F(7)) \times 6 = 5 \times (4 + 32) \times 1$$

$$\bullet \mathbf{181} := 9 \times (8 + F(7)) - F(6) = 543/(2 + 1) \\ := F(9) + F(8) \times 7 = (6 + 54) \times 3 + 2 - 1$$

$$\bullet \mathbf{182} := 9 \times F(8) - F(7) + 6 = 54 \times 3 + 2 \times 10 \\ := (F(9) - 8) \times 7 = (6 + 54) \times 3 + 2 \times 1 \\ = 6 \times 54 + F(3) - F(2 + 10)$$

$$\bullet \mathbf{183} := (F(9) - 8) \times 7 + 6 - 5 = 4 \times 32 + F(10) \\ := 9 \times (8 + F(7)) - 6 = 54 \times 3 + 21$$

$$\bullet \mathbf{184} := (9 + 8) \times 7 + 65 = 4 \times (-3^2 + F(10)) \\ := (9 + F(8) - 7) \times F(6) = -5 + F(4) \times 3 \times 21 \\ = (5 \times 4 + 3) \times (-2 + 10)$$

$$\bullet \mathbf{185} := -F(9) - 8 + F(F(7)) - 6 = 5 \times (4 + 32 + 1) \\ = 5^4 - F(3 \times 2) \times F(10)$$

$$\bullet \mathbf{186} := (F(9) - F(8)/7) \times 6 = F(5 \times F(F(4))) \times 3 + 21 \\ = 5 \times F(4) + 3 \times (2 + F(10))$$

$$\bullet \mathbf{187} := 9 \times (F(8) + 7) - 65 = 43 + F(2 + 10) \\ := F(9) + F(8) \times 7 + 6 = -5 + 4^3 \times (2 + 1) \\ = -5 \times 4 - 3 + 210$$

$$\bullet \mathbf{188} := 9 \times F(8) + (7 - F(6))^5 = F(4)^{3+2} - F(10) \\ := 9 \times F(8) - 7 + 6 = 5^{F(4)} + 3 \times 21$$

$$\bullet \mathbf{189} := 9 \times (8 + 7 + 6) = (5 + 4) \times F(3^2 - 1) \\ := F(9) \times 8 - F(7) \times 6 - 5 = F(4) \times 3 \times 21 \\ := 9 \times (8 + F(7)) = 6 + 54 \times 3 + 21 \\ := 9 \times F(8) = (7 - F(6) \times 5) \times 4 + 321 \\ = (-F(7) + 65) \times 4 - 3^2 - 10$$

- **190** := $9 \times F(8) + (-7 + F(6))^5 = (F(4 \times F(3)) - 2) \times 10$
 $= 9 \times F(8) + 7 - 6 = 5 \times (4 + F(3^2 \times 1)) = 5 \times (4 + 32) + 10$
- **191** := $9 \times (F(8) - 7) + 65 = 4 \times F(3^2) + F(10)$
 $= -F(9) - 8 + F(7 + 6) = 5 \times (4 + F(3^2)) + 1$
 $= -F(9) - 8 + F(F(7)) = 6 \times (5 - 4) \times 32 - 1$
- **192** := $-9 - F(8) + F(F(7)) - 6 - 5 = 4^3 \times (2 + 1)$
 $= (9 + 8 + 7) \times F(6) = (5 + F(4)) \times (3 + 21)$
 $= -54/3 + 210$
- **194** := $F(9) \times 8 - F(7) - 65 = -4^{F(3)} + 210$
 $= F(9) \times 8 - F(7) \times 6 = 5 \times 43 - 21$
- **195** := $9 \times (8 + F(7)) + 6 = 5 \times F(4 + 3) \times (2 + 1)$
 $= 5 \times 43 - 2 \times 10$
- **196** := $(98/7)^{F(F(6)-5)} = 4 \times (-3 \times 2 + F(10))$
 $= F(9) \times 8 - 76 = -5^{F(4)} + 321$
 $= 9 \times F(8) + 7 = 6 + 5 \times (-4 + F(3) \times 21)$
- **197** := $9 \times F(8) + 7 + 6 - 5 = -F(4 + 3) + 210$
 $= 9 \times (8 + F(7)) + F(6) = (5 + F(4)) \times 3^2 + 1$
 $= -5 - 4 \times F(3) + 210$
- **198** := $9 \times (F(8) + 7 - 6) = (5 + 4) \times (F(F(3 \times 2))) + 1$
 $= (5 + 4) \times (32 - 10)$
- **199** := $(987 + F(6))/5 = (4 \times 3)^2 + F(10)$
 $= -F(9) + 8 + F(F(7)) - F(6) = F(F(5 + F(F(4)))) - F(3^2 \times 1)$
 $= 5 - 4^{F(3)} + 210$
- **200** := $F(-9 + F(8)) + 7 \times F(6) = 5 \times (43 - 2 - 1)$
 $= (54/3 + 2) \times 10$
- **201** := $F(9) \times 8 - 76 + 5 = -F(4) \times 3 + 210$
 $= -9 \times 8 + F(7) \times F(F(6)) = 5^{F(F(4))} \times F(3 \times 2) + 1$
 $= 5 + 4 \times (-3 \times 2 + F(10))$
- **202** := $F(-9 + F(8)) - 7 + 65 = -4 \times F(3) + 210$
 $= 98 + F(7) \times F(6) = F(F(5 + F(F(4)))) - 32 + 1$
 $= -5 \times F(F(4)) + F(3) + 210$
 $= 9 \times F(8) + F(7) = 6 \times F(5 + 4) - 3 + 2 - 1$
 $= 65 - 4 - 3 + F(2 + 10)$

$$\begin{aligned}
 \bullet 203 &:= -9 + F(8) \times 7 + 65 = -4 - 3 + 210 \\
 &:= 9 \times F(8) - 7 + F(F(6)) = F(5+4) \times 3 \times 2 - 1 \\
 &\quad = 5 \times 43 - 2 - 10 \\
 &:= -9 - F(8) + F(F(7)) = (6 \times 5 + 4) \times 3 \times 2 - 1 \\
 &\quad = 65 + 4 \times 32 + 10
 \end{aligned}$$

$$\begin{aligned}
 \bullet 204 &:= 9 + F(8)/7 \times 65 = -4 - F(3) + 210 \\
 &:= (9 + F(8)) \times 7 - 6 = 5 \times (43 - 2) - 1 \\
 &\quad = (5 \times 4 - 3) \times (2 + 10)
 \end{aligned}$$

$$\begin{aligned}
 \bullet 205 &:= (9 + 8 - 7) \times F(F(6)) - 5 = -F(4) - F(3) + 210 \\
 &:= F(F(9) - F(8)) - 7 - F(F(6)) = 5 \times (43 - 2) \times 1 \\
 &\quad = -5 + (4 - 3) \times 210
 \end{aligned}$$

$$\bullet 206 := -F(9) + 8 + F(F(7)) - 6 + 5 = -F(F(4)) - F(3) + 210$$

$$\begin{aligned}
 \bullet 207 &:= (98 \times 7 - 65)/F(4) = -3 + 210 \\
 &:= 9 \times (8 + 7 + F(6)) = (5 + 4^3) \times (2 + 1) \\
 &\quad = 5 \times 43 + 2 - 10 \\
 &:= 9 \times F(8) + 7 + 6 + 5 = -F(4) + F(F(3 \times 2)) \times 10 \\
 &:= -F(9) + 8 + F(F(7)) = 6 \times 5 \times (4 + 3) - 2 - 1 \\
 &\quad = 6 + 54 + 3 + F(2 + 10)
 \end{aligned}$$

$$\begin{aligned}
 \bullet 208 &:= 98 + 76 + F(5 + 4) = -F(3) + 210 \\
 &:= -9 \times 8 + 7 \times F(6) \times 5 = 4^3 + F(2 + 10) \\
 &:= 9 \times F(8) + F(7) + 6 = -5^{F(F(4))} + F(F(3 \times 2 + 1)) \\
 &\quad = 5 - 4 - 3 + 210
 \end{aligned}$$

$$\begin{aligned}
 \bullet 209 &:= -9 - F(8) + F(F(7)) + 6 = (5^4 + F(3))/(2 + 1) \\
 &\quad = 5 - F(4) - 3 + 210
 \end{aligned}$$

$$\begin{aligned}
 \bullet 210 &:= (F(9) + 8) \times (-7 - F(6) + 5 \times 4) = F(F(3 \times 2)) \times 10 \\
 &:= (9 + F(8)) \times 7 \times (6 - 5) = (4 - 3) \times 210 \\
 &:= (F(9) + 8 - 7) \times 6 = 5 \times (43 - 2 + 1) \\
 &\quad = (-5 + F(4) + 3) \times 210 \\
 &:= (9 + F(8)) \times 7 = 65 + (4 \times 3)^2 + 1 \\
 &\quad = 654/3 + 2 - 10
 \end{aligned}$$

$$\begin{aligned}
 \bullet 211 &:= -9 - F(8) + F(F(7)) + F(6) = -5 + (4 + F(3))^{2+1} \\
 &\quad = -5 + 4 + F(3) + 210
 \end{aligned}$$

$$\begin{aligned}
 \bullet 212 &:= (9 - F(8) + (7 + 6) \times 5) \times 4 = F(3) + 210 \\
 &:= -F(9) + 8 + F(7 + 6) + 5 = F(F(4 + 3)) - 21 \\
 &\quad = 4 - F(3) + 210 \\
 &:= (9 - 8) \times (F(F(7)) - F(F(6))) = 5 \times 43 - 2 - 1 \\
 &\quad = -5 + 4 + 3 + 210
 \end{aligned}$$

$$\begin{aligned}
 \bullet 213 &:= (9 - 8) \times (76 - 5) \times F(4) = 3 + 210 \\
 &:= -9 - 8 + F(F(7)) - F(6) + 5 = F(4) + F(F(3 \times 2)) \times 10 \\
 &:= 9 + (F(8) + F(7)) \times 6 = 5 \times 43 - 2 \times 1 \\
 &\quad = (5 - 4) \times (3 + 210)
 \end{aligned}$$

$$\begin{aligned}
 \bullet 214 &:= F(9) \times 8 + 7 - 65 = 4 + F(F(3 \times 2)) \times 10 \\
 &:= -F(9) + F(8) + F(F(7)) - 6 = 5 \times 43 - 2 + 1 \\
 &\quad = (5 - 4 + 3) + 210
 \end{aligned}$$

$$\begin{aligned}
 \bullet 215 &:= (9 - 8 + 7 \times 6) \times 5 = F(F(4)) + 3 + 210 \\
 &:= (9 + 8) \times F(7) - 6 = 5 \times 43 \times (2 - 1) \\
 &\quad = 5 \times (43 + 2) - 10
 \end{aligned}$$

$$\begin{aligned}
 \bullet 216 &:= 9 \times 8 \times (7 + F(6))/5 = (4 + F(3))^{2+1} \\
 &\quad = 4 + F(3) + 210 \\
 &:= (9 + F(8)) \times 7 + 6 = 54 \times (3 + 2 - 1) \\
 &\quad = 5 + 4 - 3 + 210 \\
 &:= -9 - 8 + F(F(7)) = 654/3 - 2 \times 1 \\
 &\quad = F(6) + 5 - 4 - 3 + 210
 \end{aligned}$$

$$\begin{aligned}
 \bullet 217 &:= -9 - 8 + F(F(7)) + 6 - 5 = 4 + 3 + 210 \\
 &:= 9 \times F(8) + 7 + F(F(6)) = 5 \times 43 + 2 \times 1 \\
 &\quad = -5 + 4 \times 3 + 210
 \end{aligned}$$

$$\begin{aligned}
 \bullet 218 &:= 9 + 8 \times F(7) + F(F(6)) \times 5 = 4 \times F(3) + 210 \\
 &:= (9 + F(8)) \times 7 + F(6) = 5 \times 43 + 2 + 1 \\
 &\quad = (5 - F(4))^3 + 210
 \end{aligned}$$

$$\begin{aligned}
 \bullet 219 &:= -9 + 8 + F(F(7)) - F(6) - 5 = F(4) \times 3 + 210 \\
 &:= 9 \times 8 + 7 \times F(F(6)) = F(5 \times F(F(4))) \times (F(3) + 2) - 1 \\
 &\quad = 54 \times 3 + 2 + F(10)
 \end{aligned}$$

$$\begin{aligned}
 \bullet 220 &:= (-9 - F(8)) \times (7 + 6) + F(5 \times F(4)) = (F(3) + 2) \times F(10) \\
 &:= (9 + 8) \times F(7) - 6 + 5 = 4 \times F(3^2 + 1) \\
 &\quad = 4 \times (3 - 2) \times F(10) \\
 &:= F(-9 + F(8)) + 76 = 5 \times (43 + 2 - 1) \\
 &\quad = (54 - 32) \times 10 \\
 &:= F(F(9) - F(8)) - F(7) = 6 + 5 \times 43 - 2 + 1 \\
 &\quad = F(6) - 5 + 4 + 3 + 210
 \end{aligned}$$

$$\begin{aligned}
 \bullet 221 &:= 9 + F(8) \times 7 + 65 = F(F(4 + 3)) - 2 - 10 \\
 &:= (9 + 8) \times (7 + 6) = 5 + (4 + F(3))^{2+1} \\
 &\quad = 5 + 4 + F(3) + 210 \\
 &:= (9 + 8) \times F(7) = 654/3 + 2 + 1 \\
 &\quad = 6 + 5 \times (43 + 2) - 10
 \end{aligned}$$

$$\begin{aligned}\bullet 222 &:= (9 + 8) \times F(7) + 6 - 5 = 4 \times 3 + 210 \\ &:= (9 + F(8) + 7) \times 6 = (5 \times F(4))^{F(3)} - 2 - 1 \\ &\quad = 5 + 4 + 3 + 210\end{aligned}$$

$$\begin{aligned}\bullet 223 &:= F(9) - F(8) + 7 \times 6 \times 5 = F(4 + 3) + 210 \\ &:= 9 \times F(8) + F(7) + F(F(6)) = (5 + F(F(4))) \times 32 - 1 \\ &\quad = 5 \times 43 - 2 + 10\end{aligned}$$

$$\begin{aligned}\bullet 224 &:= -9 + F(8 \times (7 - 6) + 5) = 4 \times (3 - 2 + F(10)) \\ &:= -9 + F(F(8 - 7 + 6)) = 5 \times (43 + 2) - 1\end{aligned}$$

$$\begin{aligned}\bullet 225 &:= 9 \times (F(8) - 7 + 6 + 5) = F(F(4 + 3)) + 2 - 10 \\ &:= (9 - 8) \times F(F(7)) - F(6) = 5 \times (43 + 2) \times 1\end{aligned}$$

$$\begin{aligned}\bullet 226 &:= 9 \times F(8) + 7 \times 6 - 5 = 4^{F(3)} + 210 \\ &:= 9 - 8 + F(F(7)) - F(6) = 5 \times (43 + 2) + 1 \\ &\quad = 54 \times (F(3) + 2) + 10 \\ &:= F(F(9) - F(8)) - 7 = F(6) + 5 \times 43 + 2 + 1 \\ &\quad = 654/3 - 2 + 10\end{aligned}$$

$$\begin{aligned}\bullet 227 &:= (9 + 8) \times F(7) + 6 = -5 + F(F(4 + 3)) - 2 + 1 \\ &\quad = 5 + 4 \times 3 + 210\end{aligned}$$

$$\begin{aligned}\bullet 228 &:= 9 + (F(8) + 7) \times F(6) - 5 = (F(F(4)) + F(3)) \times (2 + F(10)) \\ &:= 9 - 8 + F(F(7)) - 6 = (5 \times F(4))^{F(3)} + 2 + 1 \\ &\quad = 54/3 + 210\end{aligned}$$

$$\begin{aligned}\bullet 229 &:= (F(9) + 8) \times 7 - 65 = -4 + F(F(3 \times 2 + 1)) \\ &:= (9 + 8) \times F(7) + F(6) = 5^{F(4)} \times F(3) - 21\end{aligned}$$

$$\begin{aligned}\bullet 230 &:= (-9 - F(8) + 76) \times 5 = F(F(4 + 3)) - 2 - 1 \\ &:= F(9) \times 8 - 7 \times 6 = 5 \times (43 + 2 + 1) \\ &\quad = 5 \times (4 + 32 + 10)\end{aligned}$$

$$\begin{aligned}\bullet 231 &:= -9 + 8 + F(F(7)) - 6 + 5 = F(F(4 + 3)) - 2 \times 1 \\ &\quad = F(4 \times F(3)) + 210 \\ &:= 9 \times F(8) + 7 \times 6 = -5 + 4^{F(3)} \times 21 \\ &\quad = 5 + 4^{F(3)} + 210\end{aligned}$$

$$\begin{aligned}\bullet 232 &:= -9 + 8 + F(F(7)) \times (6 - 5) = F(4 + 3^2) - 1 \\ &\quad = 65 - 43 + 210 \\ &:= -9 + 8 + F(7 + 6) = -5 + 4 + F(F(3 \times 2 + 1)) \\ &\quad = -5 + F(4)^3 + 210 \\ &:= -9 + 8 + F(F(7)) = F(6 - 5 + 4 \times 3) - 2 + 1\end{aligned}$$

$$\bullet 233 := F(98 - 76 - 5 - 4) = F(F(3 \times 2 + 1))$$

$$:= F(-9 + 87 - 65) = F(4 + 3^2 \times 1)$$

$$= F(4)^{3+2} - 10$$

$$:= (9 - 8) \times F(7 + 6) = F(5 + 4 + 3 + 2 - 1)$$

$$= 5 \times 4 + 3 + 210$$

$$:= (9 - 8) \times F(F(7)) = 65 \times 4 - 3^{2+1}$$

$$= (65 + 4)/3 + 210$$

$$:= F(F(9) - F(8)) = (765 - F(4))/3 - 21$$

$$= -7 + 6 \times 5 \times (4 - 3) + 210$$

$$\bullet 234 := 9 \times (8 \times 7 - 6 \times 5) = F(4 + 3^2) + 1$$

$$= F(F(4 + 3)) + 2 - 1$$

$$:= 9 - 8 + F(7 + 6) = 5 - 4 + F(F(3 \times 2 + 1))$$

$$= (5 + F(4)) \times 3 + 210$$

$$:= 9 - 8 + F(F(7)) = 6 \times (54/3 + 21)$$

$$= 6 + 54/3 + 210$$

$$\bullet 235 := F(9) \times 8 - 7 \times 6 + 5 = F(F(4 + 3)) + 2 \times 1$$

$$\bullet 236 := 9 \times F(8) + 7 \times 6 + 5 = F(F(4 + 3)) + 2 + 1$$

$$\bullet 237 := -9 + 8 + F(7 + 6) + 5 = 4 + F(F(3 \times 2 + 1))$$

$$= F(4)^3 + 210$$

$$:= -9 - 8 + F(F(7)) + F(F(6)) = -5 + F(4)^{3+2} - 1$$

$$= (5 + 4) \times 3 + 210$$

$$\bullet 238 := F(9) \times (8 - 7 + 6) = -5 + F(4)^{3+2} \times 1$$

$$= 5 + F(4)^{3+2} - 10$$

$$\bullet 239 := (9 - 8) \times F(F(7)) + 6 = 5 + F(4 + 3^2) + 1$$

$$= 5^{F(4)} + F(3) \times (2 + F(10))$$

$$:= -F(9) + F(8) \times F(7) = 654/3 + 21$$

$$= 6 \times 5 - 4 + 3 + 210$$

$$\bullet 240 := 9 - 8 + F(F(7)) + 6 = 5 \times (F(4)^3 + 21)$$

$$= (5 + 4 + 3) \times 2 \times 10$$

$$:= F(F(9) - F(8)) + 7 = F(6) \times (54 - 3 - 21)$$

$$= 6 \times 5 \times (4 - 3) + 210$$

$$\bullet 241 := 98 + F(7) \times (6 + 5) = F(F(4 + 3)) - 2 + 10$$

$$:= (9 - 8) \times F(F(7)) + F(6) = 5 + F(4) + F(F(3 \times 2 + 1))$$

$$= F(5 + 4) - 3 + 210$$

$$\bullet 242 := 98 + F(F(7) - 6 + 5) = F(4)^{3+2} - 1$$

$$:= 9 + F(F(8 - 7 + 6)) = (5 - F(F(4)))^{3+2} - 1$$

$$= 5 + F(4)^3 + 210$$

- 243 := $F(9) \times (8 - 7 + 6) + 5 = F(4)^{3+2} \times 1$
 $= F(4 + 3^2) + 10$
 $:= 9 \times (8 + F(7) + 6) = (5 + 4)^3 / (2 + 1)$
- 244 := $-9 + F(8) + F(F(7)) - 6 + 5 = F(4)^{3+2} + 1$
 $= 4 \times (3 \times 2 + F(10))$
 $:= 9 + 8 + F(F(7)) - 6 = 5 \times (4 + 3)^2 - 1$
- 245 := $9 + 8 + F(7 + 6) - 5 = F(F(4 + 3)) + 2 + 10$
 $:= 98 + 7 \times F(F(6)) = 5 \times (4 + 3)^2 \times 1$
 $= 5 \times (4 + 3) + 210$
 $:= -9 + F(8) + F(F(7)) = 6 + 5 + F(4 + 3^2) + 1$
 $= 65 \times 4 - 3 - 2 - 10$
- 246 := $F(9) - F(8) + F(F(7)) \times (6 - 5) = 4^{F(3)+2} - 10$
 $:= 9 \times (F(8) + 7) - 6 = 5 \times (4 + 3)^2 + 1$
 $= (5 + F(4)) \times 32 + 10$
 $:= F(9) - F(8) + F(F(7)) = F(F(6) + 5) + 4 + 3^2 \times 1$
 $= 6 \times (-5 + 4 + 32 + 10)$
- 247 := $F(F(9) - F(8)) - 7 + F(F(6)) = -5 + 4 \times 3 \times 21$
 $= F(5 + 4) + 3 + 210$
- 248 := $(F(9) - F(8)/7) \times F(6) = (5 + F(4)) \times (32 - 1)$
 $= -5 + 43 + 210$
- 250 := $98 + 7 \times F(F(6)) + 5 = (F(4)^3 - 2) \times 10$
 $:= 9 + 8 + F(7 + 6) = 5 \times ((4 + 3)^2 + 1)$
 $= 5 \times (4 + 3 - 2) \times 10$
 $:= 9 + 8 + F(F(7)) = 65 \times 4 - 3^2 - 1$
 $= (-F(6) + 5 - 4 + 32) \times 10$
- 251 := $F(9) \times 8 - F(7) - F(6) = -5 + 4^{F(3)\times 2} \times 1$
- 252 := $-9 + 87 \times (F(6) - 5) = 4 \times 3 \times 21$
 $:= F(9) - F(8) + F(F(7)) + 6 = (5 + 4 + 3) \times 21$
 $:= 9 \times (F(8) + 7) = -65 - 4 + 321$
- 253 := $9 \times (F(8) + 7) + 6 - 5 = 43 + 210$
 $:= F(9) \times 8 - F(7) - 6 = 5^{F(4)} \times F(3) + 2 + 1$
- 254 := $F(9) \times 8 - 7 - 6 - 5 = F(F(4 + 3)) + 21$
 $:= F(9) + 8 + F(F(7)) - F(F(6)) = F(F(-5 + 4 \times 3)) + 21$
- 255 := $(98 - F(7)) \times (F(6) - 5) = 4^{F(3)+2} - 1$
 $:= (9 + 8) \times (7 + F(6)) = (5 + F(4)) \times 32 - 1$
 $= 5 \times (43 - 2 + 10)$

$$\bullet 256 := ((98/7 + 6)/5)^4 = F(3)^{-2+10}$$

$$\begin{aligned} &:= 9 \times (8 + F(7) + F(6)) - 5 = 4^{3+2-1} \\ &\quad = 4 \times (3^2 + F(10)) \\ &:= 9 + 8 + F(F(7)) + 6 = (5 + F(4)) \times 32 \times 1 \end{aligned}$$

$$\bullet 257 := 9 + 8 + 7 + F(F(6) + 5) = 4^{F(3)+2} + 1$$

$$:= F(9) \times 8 - 7 - F(6) = 5 + 4 \times 3 \times 21$$

$$\bullet 258 := F(9) \times 8 - F(7) - 6 + 5 = F(F(4)) + F(3)^{-2+10}$$

$$\begin{aligned} &:= 9 \times (F(8) + 7) + 6 = 5^{F(F(4))} + F(F(3 \times 2 + 1)) \\ &\quad = 5 + 43 + 210 \end{aligned}$$

$$\bullet 259 := 9 + (8 \times 7 - 6) \times 5 = F(4) + F(3)^{-2+10}$$

$$\begin{aligned} &:= F(9) \times 8 - 7 - 6 = 5 + F(F(4 + 3)) + 21 \\ &:= F(9) \times 8 - F(7) = -65 + F(4) + 321 \\ &\quad = -65 + 4 + 32 \times 10 \end{aligned}$$

$$\bullet 260 := (F(9) + F(8)/7 \times 6) \times 5 = F(4 + 3) \times 2 \times 10$$

$$\begin{aligned} &:= 9 \times (F(8) + 7) + F(6) = 5 + 4^{F(3)+2} - 1 \\ &\quad = 54 \times (3 + 2) - 10 \end{aligned}$$

$$\bullet 261 := (9 \times 87)/(F(6) - 5) = F(4) \times (32 + F(10))$$

$$\begin{aligned} &:= 9 \times (8 + F(7) + F(6)) = 5 + 4^{3+2-1} \\ &\quad = 54 - 3 + 210 \end{aligned}$$

$$\bullet 263 := 9 + F(8) + F(7 + 6) = 5 \times 4^3 - 2 - F(10)$$

$$\begin{aligned} &:= 9 + F(8) + F(F(7)) = 6 \times 5 + F(4 + 3^2) \times 1 \\ &\quad = 65 - 4 \times 3 + 210 \end{aligned}$$

$$\bullet 264 := -9 + F(8) \times (7 + 6) = (5 + F(4)) \times (32 + 1)$$

$$= (5 + F(4)) + F(3)^{-2+10}$$

$$\begin{aligned} &:= -9 + F(8) \times F(7) = (F(6 + 5) + 43) \times 2 \times 1 \\ &\quad = (65 - 43) \times (2 + 10) \end{aligned}$$

$$\bullet 265 := F(9) \times 8 - 7 \times (6 - 5) = (F(F(4)) + 3) \times (-2 + F(10))$$

$$\begin{aligned} &:= 9 \times F(8) + 76 = 5 \times (F(4)^3 \times 2 - 1) \\ &\quad = 5 \times (4 - 3) \times (-2 + F(10)) \\ &:= F(9) \times 8 - 7 = F(6) + 5 + 4 \times 3 \times 21 \\ &\quad = 65 \times 4 - 3 - 2 + 10 \end{aligned}$$

$$\bullet 266 := 98 + F(F(7)) - 65 = -F(5 \times F(F(4))) + 321$$

$$= -54 + 32 \times 10$$

$$:= F(9) \times (F(8) - F(7)) - 6 = 4^{F(3)+2} + 10$$

$$\begin{aligned}\bullet 267 &:= 9 \times F(8) + F(7) + 65 = F(4) \times F(3 - 2 + 10) \\ &:= F(9) \times 8 - F(7) + F(6) = -54 + 321 \\ &\quad = 54 + 3 + 210\end{aligned}$$

$$\begin{aligned}\bullet 269 &:= 9 + F(8) + F(F(7)) + 6 = 54 \times (3 + 2) - 1 \\ &\quad = -5 + 4^3 + 210\end{aligned}$$

$$\begin{aligned}\bullet 270 &:= 9 \times F(8) + 76 + 5 = F(4) \times 3^2 \times 10 \\ &:= 9 \times (-8 + F(7)) \times 6 = 54 \times (3 + 2) \times 1 \\ &\quad = 5 \times 4 \times 3 + 210\end{aligned}$$

$$\begin{aligned}\bullet 271 &:= -9 \times 8 + 7^{F(6)-5} = -4 + (3 + 2) \times F(10) \\ &:= F(9) \times 8 - 7 + 6 = 54 \times (3 + 2) + 1 \\ &\quad = 54 \times (F(3) + 2) + F(10)\end{aligned}$$

$$\begin{aligned}\bullet 272 &:= (9 + 8) \times (F(7) + F(6) - 5) = F(F(4) \times 3) \times (-2 + 10) \\ &:= F(9) \times 8 \times (7 - 6) = F(5 + 4) \times F(3 \times 2) \times 1 \\ &\quad = 5 \times 43 + 2 + F(10) \\ &:= F(9) \times (F(8) - F(7)) = F(6) \times F(5 + 4) \times 3 / (2 + 1) \\ &\quad = 6 - 54 + 32 \times 10\end{aligned}$$

$$\bullet 272 := F(9) \times 8 = F(F(7)) - 6 + 5 + 43 - 2 - 1 = (-F(7) + 6 \times 5) \times (4 \times 3/2 + 10)$$

$$\begin{aligned}\bullet 273 &:= (98 - 7) \times (F(6) - 5) = F(4 + 3) \times 21 \\ &:= F(9) \times 8 + 7 - 6 = F(-5 + 4 \times 3) \times 21\end{aligned}$$

$$\begin{aligned}\bullet 274 &:= F(9) \times 8 + F(7) - 6 - 5 = 4^3 + 210 \\ &:= 9 + F(8) \times F(7) - F(6) = 5 \times F(4 \times 3 - 2) - 1 \\ &\quad = -5 + 4 + (3 + 2) \times F(10)\end{aligned}$$

$$\begin{aligned}\bullet 275 &:= F(9) \times 8 + 7 - 6 + 5 - F(4) = (3 + 2) \times F(10) \\ &:= (9 + F(8)) \times 7 + 65 = (4 + 3 - 2) \times F(10) \\ &:= F(9) + 8 + F(7 + 6) = 5 \times (F(4)^3 \times 2 + 1) \\ &\quad = 5 \times (43 + 2 + 10) \\ &:= F(9) + 8 + F(F(7)) = F(6) - 54 + 321 \\ &\quad = 6 \times 54 + 3 \times 2 - F(10)\end{aligned}$$

$$\begin{aligned}\bullet 276 &:= 9 + F(8) \times F(7) - 6 = 5 \times F(4 \times 3 - 2) + 1 \\ &\quad = -54 + 3 \times 2 \times F(10)\end{aligned}$$

$$\begin{aligned}\bullet 277 &:= (-9 + 8 \times 7) \times 6 - 5 = F(F(4)) + (3 + 2) \times F(10) \\ &:= F(9) \times 8 + F(7) - F(6) = (-5 + F(4 \times 3)) \times 2 - 1\end{aligned}$$

$$\begin{aligned}\bullet 278 &:= F(9) \times 8 + 7 - 6 + 5 = F(4 \times 3) \times 2 - 10 \\ &:= F(9) \times (F(8) - F(7)) + 6 = (-5 + F(4 \times 3)) \times 2 \times 1 \\ &\quad = (5 + 4) \times 32 - 10\end{aligned}$$

$$\begin{aligned}
 \bullet 279 &:= F(9) \times 8 + 7 \times (6 - 5) = 4 + (3 + 2) \times F(10) \\
 &:= F(9) \times 8 + F(7) - 6 = (5 + 4) \times (32 - 1) \\
 &\quad = 5 + 4^3 + 210 \\
 &:= F(9) \times 8 + 7 = 65 \times 4 - F(3) + 21 \\
 &\quad = F(6) + 5 + (4^{F(3)})^2 + 10
 \end{aligned}$$

$$\bullet 280 := (F(9) + 8 - 7) \times F(6) = (5 + F(4)) \times (F(3^2) + 1) \\
 = 54 \times (3 + 2) + 10$$

$$\bullet 281 := F(9) + 8 + F(F(7)) + 6 = -5 + F(F(4 + 3)) - 2 + F(10)$$

$$\begin{aligned}
 \bullet 282 &:= -98 + 76 \times 5 = -F(F(4)) \times (3 - F(2 + 10)) \\
 &:= (-9 + 8 \times 7) \times 6 = -5 + F(4 \times 3) \times 2 - 1 \\
 &:= 9 + F(8) \times F(7) = 6 \times (5 + 43 - 2 + 1) \\
 &\quad = 6 \times 54 - 32 - 10
 \end{aligned}$$

$$\bullet 283 := F(9) + 8 + F(F(7)) + F(6) = -5 + F(4 \times 3) \times 2 \times 1$$

$$\begin{aligned}
 \bullet 284 &:= 9 + (-F(8) + 76) \times 5 = -4 + F(3) \times F(2 + 10) \\
 &:= 9 + F(8) + F(F(7)) + F(F(6)) = -5 + F(4 \times 3) \times 2 + 1
 \end{aligned}$$

$$\begin{aligned}
 \bullet 285 &:= 9 + F(8) \times F(7) + F(6) - 5 = (F(F(4)) + 3) \times (2 + F(10)) \\
 &:= F(9) \times 8 + 7 + 6 = 5 \times F(4) \times (-F(3) + 21) \\
 &\quad = 5 + (-4 + 32) \times 10 \\
 &:= F(9) \times 8 + F(7) = -F(6) \times 5 + 4 + 321 \\
 &\quad = 6 + 5 + 4^3 + 210
 \end{aligned}$$

$$\begin{aligned}
 \bullet 286 &:= (9 + 8) \times F(7) + 65 = F(F(4 + 3)) - 2 + F(10) \\
 &:= F(9) \times 8 - 7 + F(F(6)) = F(5 + F(F(4))) \times (F(F(3 \times 2)) + 1) \\
 &\quad = -54 + F(3^2) \times 10
 \end{aligned}$$

$$\begin{aligned}
 \bullet 287 &:= (-9 + 8 \times 7) \times 6 + 5 = F(4 \times 3) \times 2 - 1 \\
 &:= F(9) \times 8 + 7 + F(6) = (5 + 4) \times 32 - 1
 \end{aligned}$$

$$\begin{aligned}
 \bullet 288 &:= (9 - 8 + 76 - 5) \times 4 = F(3) \times F(2 + 10) \\
 &:= 9 \times 8 \times (-7 + 6 + 5) = F(4 \times 3) \times 2 \times 1 \\
 &\quad = F(4 + 3^2) + F(10) \\
 &:= (F(9) + 8) \times 7 - 6 = (5 + 4) \times 32 \times 1 \\
 &:= F(9) + F(8) + F(F(7)) = (-6 + 54) \times 3 \times 2 \times 1 \\
 &\quad = 6 \times (5 - 4 + 3) \times (2 + 10)
 \end{aligned}$$

$$\begin{aligned}
 \bullet 289 &:= (9 + 8)^{F(7)-6-5} = F(4 \times 3) \times 2 + 1 \\
 &:= F(F(9) - F(8)) + 7 \times F(6) = (5 + 4) \times 32 + 1
 \end{aligned}$$

$$\begin{aligned}
 \bullet 290 &:= (9 \times 8 + 7 - F(F(6))) \times 5 = (F(4)^3 + 2) \times 10 \\
 &:= 9 + F(8) \times F(7) + F(6) = (5 + 4 \times 3)^2 + 1 \\
 &\quad = ((5 + 4) \times 3 + 2) \times 10
 \end{aligned}$$

- **291** := $98 + F(F(7)) - F(6) \times 5 = F(4) + F(3) \times F(2 + 10)$
 $= F(9) \times 8 + F(7) + 6 = (5 + 4)^{F(3)} + 210$
- **292** := $9 \times 8 + F(F(7)) - F(6) - 5 = F(F(4)) \times (F(3) + F(2 + 10))$
- **293** := $F(9) \times 8 + F(7) + F(6) = 5 + F(4 \times 3) \times 2 \times 1$
 $= 5 + F(4 \times 3) + F(2 + 10)$
- **294** := $98 \times (7 + F(6))/5 = F(F(4)) \times (3 + F(2 + 10))$
 $= (F(9) + 8 + 7) \times 6 = 5 + F(4 \times 3) \times 2 + 1$
 $= (5 + F(F(4))) \times (32 + 10)$
 $= (F(9) + 8) \times 7 = -6 - 5 \times 4 + 32 \times 10 = 6 \times (5 + 43 + 2 - 1)$
- **296** := $(9 + F(8) + 7) \times F(6) = -5^{F(F(4))} + 321$
 $= 5 + F(4) + F(3) \times F(2 + 10)$
- **297** := $9 \times 8 + F(F(7)) - F(6) = (5 + 4) \times (32 + 1)$
 $= F(5 \times F(4))/F(3) + 2 - 10$
- **298** := $9 - F(8) \times (7 - F(F(6)) + 5) = F(4 \times 3) \times 2 + 10$
 $= 9 \times (F(8) + F(7)) - F(6) = (5 + F(4 \times 3)) \times 2 \times 1$
 $= (5 + 4) \times 32 + 10$
- **299** := $9 \times 8 + F(F(7)) - 6 = 5 \times 4^3 - 21$
- **300** := $(9 + 8 - 7) \times 6 \times 5 = (-4 + F(3^2)) \times 10$
 $= (F(9) + 8) \times 7 + 6 = -F(5 + F(4)) + 321$
 $= 5 \times 4^3 - 2 \times 10$
- **301** := $F(9) + F(8) \times F(7) - 6 = -5 \times 4 + 321$
- **302** := $-F(9) + 8 \times 7 \times 6 = F(5 \times F(4))/F(3) - 2 - 1$
- **303** := $9 + F(8) \times (-7 + F(F(6))) = F(5 \times F(4))/F(3) - 2 \times 1$
- **304** := $F(9) - 8 + F(7) \times F(F(6)) + 5 = 4 \times (F(F(3 \times 2)) + F(10))$
- **305** := $9 \times 8 + F(7 + 6) = 5 \times (4^3 - 2 - 1)$
 $= 5^4 - 32 \times 10$
 $= 9 \times 8 + F(F(7)) = (65 - 4) \times (3 \times 2 - 1)$
 $= (6 - 5 + 4)^3 \times 2 + F(10)$
- **306** := $9 \times F(8 + 7 - 6) = -5 \times F(4) + 321$
 $= 9 \times (F(8) + F(7)) = 654/F(3) - 21$
 $= 6 \times (54 - 3 + 21 \times 0)$
- **307** := $F(9) + F(8) \times (7 + 6) = (5 + 4) \times F(3^2) + 1$
 $= 5^{F(4)} \times F(3) + 2 + F(10)$
 $= F(9) + F(8) \times F(7) = 6 - 5 \times 4 + 321$
- **309** := $F(F(9) - F(8)) + 76 = 5 \times (4^3 - 2) - 1$

$$\begin{aligned}\bullet 310 &:= 9 \times 8 + F(7+6) + 5 = (-F(4) + F(3^2)) \times 10 \\ &:= 98 + F(F(7)) - F(F(6)) = 5 \times (4^3 - 2) \times 1 \\ &= (-5 + 4 + 32) \times 10\end{aligned}$$

$$\begin{aligned}\bullet 311 &:= F(9) - F(8) + F(F(7)) + 65 = 4^{F(3)+2} + F(10) \\ &:= 9 \times 8 + F(F(7)) + 6 = 5 \times (4^3 - 2) + 1\end{aligned}$$

$$\begin{aligned}\bullet 312 &:= (F(9) - 8 + F(7)) \times F(6) = -5 - 4 + 321 \\ &= 5 \times 4^3 + 2 - 10\end{aligned}$$

$$\bullet 313 := 9 \times 8 + F(F(7)) + F(6) = -5 - F(4) + 321$$

$$\begin{aligned}\bullet 314 &:= F(9) \times 8 + 7 \times 6 = (5^4 + 3)/2 \times 1 \\ &= 54 \times 3 \times 2 - 10\end{aligned}$$

$$\bullet 315 := 9 \times (8 \times 7 - F(F(6))) = 5 \times (4^3 - 2 + 1)$$

$$\bullet 316 := 9 \times 8 + F(F(7)) + 6 + 5 = -4 + 32 \times 10$$

$$\begin{aligned}\bullet 317 &:= 9 \times (F(8) + 7) + 65 = -4 + 321 \\ &:= (F(9) - 8) \times F(7) - F(F(6)) = 5 \times 4^3 - 2 - 1\end{aligned}$$

$$\begin{aligned}\bullet 318 &:= F(9) + F(8) \times F(7) + 6 + 5 = -F(4) + 321 \\ &:= (-F(9) + 87) \times 6 = 5 \times 4^3 - 2 \times 1 \\ &= 54 \times F(3) + 210\end{aligned}$$

$$\bullet 319 := 9 + (8 \times 7 + 6) \times 5 = -F(F(4)) + 321$$

$$\bullet 320 := 98 + F(F(7)) - 6 - 5 = 4^3/2 \times 10$$

$$\begin{aligned}\bullet 321 &:= -98 - F(7) + F(6) \times 54 = 321 \\ &:= -9 - 8 + F(F(7)) + F(F(6)) \times 5 = F(4) \times (-3 + 2 \times F(10))\end{aligned}$$

$$\begin{aligned}\bullet 322 &:= (F(9) + 8) + 7 \times F(6) \times 5 = F(F(4)) + 32 \times 10 \\ &:= -F(9) + F(F(8) - 7) - F(F(6)) = 5 - 4 + 321\end{aligned}$$

$$\begin{aligned}\bullet 323 &:= (9 + 8) \times (-7 + F(F(6)) + 5) = F(F(4)) + 321 \\ &= F(4) + 32 \times 10 \\ &:= (9 + 8) \times (F(7) + 6) = 5 - F(4) + 321 \\ &= -54 + F(F(3) + 2 + 10)\end{aligned}$$

$$\begin{aligned}\bullet 324 &:= 9 + (F(8) + 7 \times 6) \times 5 = F(4) + 321 \\ &= 4 + 32 \times 10 \\ &:= 9 + F(8) \times (7 + F(6)) = 54 \times (3 + 2 + 1)\end{aligned}$$

$$\begin{aligned}\bullet 325 &:= -F(9) - F(8) + 76 \times 5 = 4 + 321 \\ &:= 98 + F(F(7)) - 6 = 54 \times 3 \times 2 + 1 \\ &= 5 \times 43 + 2 \times F(10)\end{aligned}$$

$$\begin{aligned}\bullet 326 &:= 98 + F(7 + 6) - 5 = -4 + 3 \times 2 \times F(10) \\ &:= 9 \times 8 + F(F(7)) + F(F(6)) = F(5 \times F(4))/F(3) + 21 \\ &= 5 + F(4) \times (-3 + 2 \times F(10))\end{aligned}$$

- **327** := $(F(9) - 8) \times F(7) - 6 - 5 = -F(4) + 3 \times 2 \times F(10)$
 $= -9 + 8 \times 7 \times 6 = 5 + F(F(4)) + 32 \times 10$
- **328** := $9 + F(8) + F(F(7)) - 65 = -F(F(4)) + 3 \times 2 \times F(10)$
 $= F(9) \times 8 + 7 \times F(6) = 5 + F(F(4)) + 321$
 $= 5 \times 4^3 - 2 + 10$
- **329** := $987 / (F(6) - 5) = F(4^{F(3)}) / (2 + 1)$
- **330** = $(98 - (7 - 65) \times 4) = 3 \times 2 \times F(10)$
 $= F(9) \times 8 - 7 + 65 = 4 \times 3/2 \times F(10)$
 $= F(9 + 8 - 7) \times 6 = 5 + 4 + 321$
 $= (5 - 4 + 3) \times 10$
- **331** := $98 + F(7 + 6) = 5 \times F(F(4)) + 321$
 $= 98 + F(F(7)) = 6 \times 54 + 3 \times 2 + 1$
- **332** := $-9 + 8 \times 7 \times 6 - 5 = F(F(4)) + 3 \times 2 \times F(10)$
 $= (F(9) - 8) \times F(7) - 6 = 5 \times 4^3 + 2 + 10$
- **333** := $F(9) \times 8 + 7 \times F(6) + 5 = F(4) + 3 \times 2 \times F(10)$
- **334** := $F(9) \times F(8) - 76 \times 5 = 4 + 3 \times 2 \times F(10)$
- **335** := $-F(9) - 8 + F(-7 + F(F(6))) = 5 \times (4 + 3 \times 21)$
 $= 5 \times F(4) + 32 \times 10$
- **336** := $98 + F(7 + 6) + 5 = 4^{F(3)} \times 21$
 $= 9 \times F(8) + 7 \times F(F(6)) = 5 \times F(4) + 321$
- **337** := $98 + F(F(7)) + 6 = F(5 + F(F(4)))^{F(3)} \times 2 - 1$
 $= 5 + F(F(4)) + 3 \times 2 \times F(10)$
 $= F(9) \times 8 + (7 + 6) \times 5 = -F(4) + F(3^2) \times 10$
- **338** := $-F(9) - 8 + 76 \times 5 = -F(F(4)) + F(3^2) \times 10$
 $= (F(9) - 8) \times (7 + 6) = -5 + (4 + 3)^{2+1}$
 $= 5^{F(4)} + 3 + 210$
 $= (F(9) - 8) \times F(7) = F(6) + 5 + 4 + 321$
 $= 6 \times (-5 + 43) + 2 \times F(10)$
- **339** := $(9 + F(8) + F(7)) \times F(6) - 5 = F(4) \times (3 + 2 \times F(10))$
 $= 98 + F(F(7)) + F(6) = 5 \times F(F(4) \times 3) \times 2 - 1$
 $= -5 + 43 \times (-2 + 10)$
- **340** := $98 + F(7 + 6) + 5 + 4 = F(3^2) \times 10$
 $= 9 + 8 \times 7 \times 6 - 5 = F(4 + 3 + 2) \times 10$
 $= F(9) \times (F(F(8)/7) + F(6)) = 5 \times F(F(4) \times 3) \times 2 \times 1$
 $= 5 \times (4^3 + 2) + 10$

- **342** := $98 + F(F(7)) + 6 + 5 = (4 + F(3)) \times (2 + F(10))$
- **343** := $F(9) \times 8 + 76 - 5 = (4 + 3)^{2+1}$
 $= F(4) + F(3^2) \times 10$
 $:= -F(9) + F(F(8) - F(7) + 6) = (-5 + 4 \times 3)^{2+1}$
 $:= -F(9) + F(F(8) - 7) = 6 \times (54 + 3) + 2 - 1$
 $= (-6 + 5 \times F(4)) \times 32 + F(10)$
- **344** := $9 - 8 + 7^{F(6)-5} = 43 \times (-2 + 10)$
 $:= (F(9) - 8) \times F(7) + 6 = (5 + F(F(4)))^3 + 2 - 1$
 $= (5 \times 4 - 3)^2 + F(10)$
- **345** := $9 + 8 \times 7 \times 6 = 5 \times F(4) \times (F(3) + 21)$
 $= 5 \times (4^{F(3)} - 2 + F(10))$
- **346** := $(F(9) - 8) \times F(7) + F(6) = 5^{F(F(4))} + 321$
 $= F(F(5 + F(F(4)))) + 3 + 2 \times F(10)$
- **347** := $-9 + F(F(8) - 7) - F(F(6)) = 5 + F(F(4)) \times 3 \times (2 + F(10))$
- **348** := $-F(9) + F(F(8) - F(7)) + 6 + 5 = 4 \times (32 + F(10))$
 $:= F(9) \times 8 + 76 = 5 + (4 + 3)^{2+1}$
 $= 5 + F(4 \times 3) \times 2 + F(10)$
- **349** := $-F(9) + F(F(8) - 7) + 6 = 5 + 43 \times (-2 + 10)$
- **350** := $F(9) \times 8 + F(7) + 65 = (F(4) + 32) \times 10$
 $:= F(9) \times 8 + F(7) \times 6 = 5 \times F(F(4)) \times F(3^2 + 1)$
 $= 5^4 - (3 + 2) \times F(10)$
- **351** := $-F(9) + F(F(8) - 7) + F(6) = F(5 + F(F(4))) \times 3^{2+1}$
 $= F(5 + F(4)) + 3 \times 2 \times F(10)$
 $:= 98 + F(F(7)) + F(F(6)) = (5 + F(4)) \times (F(3^2) + 10)$
- **354** := $F(9) \times 8 - 7 + F(6 + 5) = F(4 \times 3) + 210$
 $:= (9 \times 8 - F(7)) \times 6 = 5^{F(4)} \times 3 - 21$
- **356** := $9 + F(F(8) - 7) - 6 \times 5 = 4 \times (F(3^2) + F(10))$
 $:= F(98/7) - F(F(6)) = F(5 + F(4) \times 3) - 21$
 $= F(F(5 + F(F(4)))) \times F(3) - 2 \times F(10)$
- **357** := $(9 + 8) \times (F(7) + F(6)) = (5 + 4 \times 3) \times 21$
- **359** := $(F(9) - 8) \times F(7) + F(F(6)) = 5 \times F(4 \times 3)/2 - 1$
 $= 5 + F(4 \times 3) + 210$
- **360** := $9 \times (F(8) + F(7) + 6) = 5 \times 4 \times (-3 + 21)$
 $= 54/3 \times 2 \times 10$
- **362** := $-9 + F(F(8) - 7) - 6 = (F(5 + F(4)) - F(3))^2 + 1$

- 364 := $(F(9) - F(8)) \times (7 + F(F(6))) = (5 + F(F(4)))^3 + 21$
 $= F(5 + 4) + 3 \times 2 \times F(10)$
- 365 := $9 + F(F(8) - 7) - F(F(6)) = 5 \times (F(4 \times 3)/2 + 1)$
 $= -5 + (F(4) + F(3^2)) \times 10$
- 367 := $-F(9) + F(8) + 76 \times 5 = F((4 + 3) \times 2) - 10$
- 368 := $-9 + F(F(8) - F(7) + 6) = (5 + F(4)) \times (-3^2 + F(10))$
 $= -9 + F(F(8) - 7) = -65 + 432 + 1$
 $= -6 + 54 + 32 \times 10$
- 369 := $F(98/7) - F(6) = (5^{F(4)} - F(3)) \times (2 + 1)$
 $= -5 - F(4) + F(F(3) + 2 + 10)$
- 370 := $F(9) \times 8 - 7 + F(F(6)) \times 5 = (F(4) + F(3^2)) \times 10$
 $= F(9) + 8 \times 7 \times 6 = (5 + 4^3/2) \times 10$
- 371 := $-F(9) + (87 - 6) \times 5 = (4 + 3) \times (-2 + F(10))$
 $= F(98/7) - 6 = -5 + F((4 + 3) \times 2) - 1$
 $= (5 + 4 - F(3)) \times (-2 + F(10))$
- 372 := $(F(9) + F(8) + 7) \times 6 = -5 + F((4 + 3) \times 2) \times 1$
 $= 54 \times 3 + 210$
- 373 := $-9 - 8 + F(7) \times 6 \times 5 = -4 + F(F(3) + 2 + 10)$
- 374 := $F(98/7) - F(6) + 5 = -F(4) + F(F(3) + 2 + 10)$
 $= -9 + F(F(8) - 7) + 6 = 5^{F(4)} \times 3 - 2 + 1$
 $= 54 + 32 \times 10$
- 375 := $(-9 + 8 + 76) \times 5 = -F(F(4)) + F(F(3) + 2 + 10)$
- 376 := $F(98/7) - 6 + 5 = F((4 + 3) \times 2) - 1$
 $= (-9 + 8 \times 7) \times F(6) = 5^{F(4)} \times 3 + 2 - 1$
- 377 := $9 - 8 + 76 \times 5 - 4 = F(F(3) + 2 + 10)$
 $= F(98/7) \times (6 - 5) = F((4 + 3) \times 2) \times 1$
 $= 432 - F(10)$
 $= F(9 - 8 + 7 + 6) = F(5 - 4 \times 3 + 21)$
 $= F(98/7) = F(6 - 5 + 4 \times 3 + 2 - 1)$
 $= F(65 - 43 + 2 - 10)$
- 378 := $98 + 7 \times F(6) \times 5 = F((4 + 3) \times 2) + 1$
 $= 9 + F(F(8) - 7) - F(6) = 54/3 \times 21$
- 379 := $-9 + 8 + 76 \times 5 = F(F(4)) + F(F(3) + 2 + 10)$
 $= (F(9) + F(8)) \times 7 - 6 = (5 \times 4)^{F(3)} - 21$
- 380 := $(9 - 8) \times 76 \times 5 = (4 + F(3^2)) \times 10$
 $= 9 + F(F(8) - 7) - 6 = 5 \times 4 \times (-F(3) + 21)$
 $= 5 \times (43 \times 2 - 10)$

- 381 := $9 - 8 + 76 \times 5 = 4 + F(F(3) + 2 + 10)$
- 382 := $(9 + F(8)) \times F(7) - F(6) = -5 + F((4 + 3) \times 2) \times 1$
- 383 := $F(98/7) + 6 = 5 + F((4 + 3) \times 2) + 1$
- 384 := $(9 + F(8)) \times F(7) - 6 = (5^{F(4)} + 3) \times (2 + 1)$
 $= 54 + 3 \times 2 \times F(10)$
- 385 := $(9 - 8 + 76) \times 5 = (F(4) \times 3 - 2) \times F(10)$
 $= F(98/7) + F(6) = F(5 \times F(F(4))) \times (3 \times 2 + 1)$
 $= (5 - 4 + 3 \times 2) \times F(10)$
 $= (F(9) + F(8)) \times 7 = (6 + 5) \times (4 + 32 - 1)$
 $= (6 + 5) \times (43 + 2 - 10)$
- 386 := $-9 + (87 - F(6)) \times 5 = F(4 \times F(3))^2 - F(10)$
 $= 9 + F(F(8) - F(7) + 6) = -54 + F(3 \times 2) \times F(10)$
 $= 9 + F(F(8) - 7) = F(6) + 54/3 \times 21$
 $= F(-6 + 5 \times 4) - 3 + 2 + 10$
- 387 := $9 + F(8) \times (7 + 6 + 5) = F((4 + 3) \times 2) + 10$
- 389 := $-9 + F(F(8) - 7) + F(F(6)) = F(5 + F(4) \times 3) + 2 + 10$
- 390 := $(9 + 8 \times 7) \times 6 = (5 + F(F(4)) + 32) \times 10$
 $= (9 + F(8)) \times F(7) = 65 + 4 + 321$
- 391 := $(F(9) + F(8)) \times 7 + 6 = (5 + F(4 \times F(3))^2) - F(10)$
- 392 := $(F(9) + 8 + 7) \times F(6) = (5 \times 4)^{F(3)} + 2 - 10$
- 393 := $(F(9) + F(8)) \times 7 + F(6) = (F(5 + F(F(4))))^{F(3)} \times 2 + F(10)$
- 394 := $9 + F(F(8) - 7) + F(6) = 54 + F(3^2) \times 10$
- 396 := $(9 + F(8)) \times F(7) + 6 = 5^{F(4)} \times 3 + 21$
- 398 := $F(98/7) + F(F(6)) = ((5 \times 4)^{F(3)} - 2) \times 1$
 $= -F(5 + 4) + 3 \times F(2 + 10)$
- 399 := $9 \times F(8) + 7 \times 6 \times 5 = (4 + 3) \times (2 + F(10))$
 $= (F(9) - 8 - 7) \times F(F(6)) = (F(5 + F(4)) - F(3)) \times 21$
 $= 543 - F(2 + 10)$
- 401 := $9 \times F(8) + F(F(7)) - F(F(6)) = (5 \times 4)^{F(3)} + 2 - 1$
 $= (-5 + F(F(4 + 3))) \times 2 - F(10)$
- 403 := $F(9) + F(F(8) - 7) - F(6) = (5 \times 4)^{F(3)} + 2 + 1$
 $= F(5 \times F(4)) + 3 - 210$
- 405 := $F(9) + F(F(8) - 7) - 6 = 5 \times F(4) \times 3^{2+1}$
 $= -5 + (43 - 2) \times 10$

- **406** := $(F(9) + F(8)) \times 7 + F(F(6)) = 5 \times (F(4) \times 3)^2 + 1$
 $= -F(5+4) + F(3 \times 2) \times F(10)$
- **407** := $(9 + F(F(8) - 7)) + F(F(6)) = -F(5 + F(F(4))) + F(3) \times 210$
- **408** := $(9 + 8) \times (F(7) + 6 + 5) = F(F(4) \times 3) \times (2 + 10)$
 $:= 9 + F(8) \times (F(7) + 6) = (54 - 3) \times (-2 + 10)$
- **410** := $9 + F(8) + 76 \times 5 = (43 - 2) \times 10$
- **411** := $-9 + (8 + 76) \times 5 = F(F(4 + 3)) \times 2 - F(10)$
 $:= (9 + F(8)) \times F(7) + F(F(6)) = -5 - 4 + F(3) \times 210$
 $:= F(9) + F(F(8) - 7) = 6 + 5 \times F(4) \times 3^{2+1}$
 $= -6 - 5 + 432 - 10$
- **414** := $9 + (87 - 6) \times 5 = F(F(4)) \times (-3 + 210)$
 $:= -F(9) + 8 \times 7 \times F(6) = (5 - F(4)) \times (-3 + 210)$
- **416** := $-F(9) + (8 + 7) \times 6 \times 5 = -4 + F(3) \times 210$
 $:= 9 \times F(8) + F(F(7)) - 6 = F(5 + F(F(4))) \times 32 \times 1$
 $= (54 - F(3)) \times (-2 + 10)$
- **417** := $F(98/7) + F(6) \times 5 = -F(4) + F(3) \times 210$
 $:= F(9) + F(F(8) - 7) + 6 = (-5 + F(4 \times 3)) \times (2 + 1)$
 $= -5 + 432 - 10$
- **419** := $F(9) \times 8 + 7 \times F(F(6)) = 5 \times 4 \times F(F(3 \times 2)) - 1$
 $= -5 + 4 + F(3) \times 210$
- **420** := $9 + 87 + 6 \times 54 = F(3) \times 210$
 $:= 98/7 \times 6 \times 5 = (4 - F(3)) \times 210$
 $:= (-F(9) + 8 \times F(7)) \times 6 = 5 \times F(F(4)) \times F(3) \times 21$
 $= 5 \times 43 \times 2 - 10$
- **421** := $-9 \times F(8) + F(7 + F(6)) = (5 \times 4)^{F(3)} + 21$
- **422** := $F(9) + 8 + 76 \times 5 = 432 - 10$
 $:= 9 \times F(8) + F(7 + 6) = 5 - F(4) + F(3) \times 210$
 $:= 9 \times F(8) + F(F(7)) = -6 - 5 + 432 + 1$
 $= (6 - 5) \times 432 - 10$
- **423** := $9 \times (87 - F(6) \times 5) = F(4) + F(3) \times 210$
- **424** := $9 + (8 \times F(7) - F(F(6))) \times 5 = 4 + F(3) \times 210$
 $:= (-F(9) + 87) \times F(6) = (5 - F(4)) \times (F(3) + 210)$
- **426** := $9 + F(F(8) - 7) + F(6) \times 5 = F(F(4)) \times (3 + 210)$
- **428** := $F(9) + F(8) \times (F(7) + 6) + 5 = 4 \times (-3 + 2 \times F(10))$
 $:= 9 \times F(8) + F(F(7)) + 6 = -5 + 432 + 1$

$$\bullet \mathbf{429} := 9 + (8 + 76) \times 5 = -F(4) + 3 \times F(2 + 10)$$

$$\begin{aligned}\bullet \mathbf{430} &:= -F(9) + 8 \times (-7 + 65) = -F(F(4)) + 3 \times F(2 + 10) \\ &:= 9 \times F(8) + F(F(7)) + F(6) = 5 \times 43 \times 2 \times 1\end{aligned}$$

$$\bullet \mathbf{431} := -F(9) + (87 + 6) \times 5 = 432 - 1$$

$$\begin{aligned}\bullet \mathbf{432} &:= (98/7 - 6) \times 54 = 3 \times F(2 + 10) \\ &:= 9 \times (8 \times 7 - F(6)) = 54 \times (3^2 - 1)\end{aligned}$$

$$\bullet \mathbf{433} := -9 + (F(8) + F(7)) \times (F(6) + 5) = 432 + 1$$

$$\begin{aligned}&:= F(9) + F(8) \times (F(7) + 6) = 54 \times F(3 \times 2) + 1 \\ &= 543 - 2 \times F(10)\end{aligned}$$

$$\bullet \mathbf{434} := -9 + 8 \times 7 \times F(6) - 5 = F(F(4)) + 3 \times F(2 + 10)$$

$$\bullet \mathbf{435} := F(9) + F(8) + 76 \times 5 = F(4) + 3 \times F(2 + 10)$$

$$\bullet \mathbf{436} := 9 \times (F(8) + 7 + F(F(6))) - 5 = 4 + 3 \times F(2 + 10)$$

$$\bullet \mathbf{437} := 9 \times (F(8) - F(7)) \times 6 + 5 = -F(4) + F(3 \times 2) \times F(10)$$

$$\bullet \mathbf{438} := -9 - 8 + 7 \times 65 = -F(F(4)) + F(3 \times 2) \times F(10)$$

$$\begin{aligned}\bullet \mathbf{439} &:= -9 + 8 \times 7 \times F(6) = F(5 \times F(F(4))) \times F(3 \times 2) - 1 \\ &= -5 + 4 + F(3 \times 2) \times F(10)\end{aligned}$$

$$\bullet \mathbf{440} := F(9) - F(8) + 7 \times (65 - 4) = F(3 \times 2) \times F(10)$$

$$\begin{aligned}&:= (9 + 87 - F(6)) \times 5 = F(4 \times F(3))^2 - 1 \\ &:= F(9 + 8 - 7) \times F(6) = 5 \times (F(F(4) \times 3 + 2) - 1) \\ &= 5 \times 43 \times 2 + 10\end{aligned}$$

$$\bullet \mathbf{441} := -F(9) + (87 + F(6)) \times 5 = F(4 \times F(3)) \times 21$$

$$\begin{aligned}&:= F(9 - 8 + 7) \times F(F(6)) = (5 + 4^{F(3)}) \times 21 \\ &= F(4) \times (3 + F(2 + 10))\end{aligned}$$

$$\bullet \mathbf{442} := F(98/7) + 65 = F(4 \times F(3))^2 + 1$$

$$= 432 + 10$$

$$:= F(9) \times F(8 - 7 + 6) = F(5 + 4) \times F(3 \times 2 + 1)$$

$$\bullet \mathbf{443} := 9 - F(8) + 7 \times 65 = F(F(4 + 3)) + 210$$

$$\begin{aligned}&:= 9 \times F(8) + F(F(7)) + F(F(6)) = (F(5 + F(4)))^{F(3)} + 2 \times 1 \\ &= -5 + 4 \times (F(3) + 2 \times F(10))\end{aligned}$$

$$\bullet \mathbf{444} := 9 \times 8 + F(-7 + F(F(6))) - 5 = 4 + F(3 \times 2) \times F(10)$$

$$\begin{aligned}\bullet \mathbf{445} &:= F(F(9) - F(8)) + F(F(7)) - F(F(6)) = 5 \times F(4 \times 3 - 2 + 1) \\ &= 5^{F(4)} + 32 \times 10\end{aligned}$$

$$\bullet \mathbf{448} := -F(9) + F(F(8) - 7) + F(F(6)) \times 5 = 4 \times (F(3) + 2 \times F(10))$$

$$\begin{aligned}\bullet \mathbf{449} &:= 9 \times 8 + F(-7 + F(F(6))) = (5 \times F(4))^{F(3)} \times 2 - 1 \\ &= 5 + 4 + F(3 \times 2) \times F(10)\end{aligned}$$

- 450 := $9 \times (8 + 7 \times 6) = 5^{F(F(4))} \times (-3 + 21) = (54 - 3^2) \times 10$
- 451 := $F(9) + F(F(8) - 7) + F(6) \times 5 = F(4 \times F(3))^2 + 10$
- 452 := $9 \times 8 + 76 \times 5 = 4 \times (3 + 2 \times F(10))$
- 455 := $F(9) \times (F(8) - 7) - F(F(6)) = (-5 + F(F(4 + 3))) \times 2 - 1 = 5 \times (4 + 32 + F(10))$
- 456 := $9 - 8 + 7 \times 65 = 4 \times F(3) \times (2 + F(10))$
- 457 := $(-F(9) + 8 \times 7) \times F(F(6)) - 5 = F(F(4))^{3^2} - F(10) = (-5 + F(F(4 + 3))) \times 2 + 1 = 5 + 4 \times (3 + 2 \times F(10))$
- 458 := $F(F(9) - F(8)) + F(F(7)) - F(6) = F(F(5 + F(F(4)))) \times F(3) + 2 - 10$
- 460 := $F(F(9) - F(8)) + F(F(7)) - 6 = 5 \times 4 \times (F(3) + 21) = (5 + 43 - 2) \times 10$
- 462 := $(-F(9) + 8 \times 7) \times F(F(6)) = (5 \times 4 + F(3)) \times 21$
- 465 := $(9 + 8 + 76) \times 5 = F(F(4 + 3)) \times 2 - 1$
- 466 := $-9 + (87 + F(6)) \times 5 = F(F(4 + 3)) \times 2 \times 1 = F(F(9) - F(8)) + F(7 + 6) = F(5 + 4 \times F(3)) \times 2 \times 1 = (-5 + F(F(4 + 3))) \times 2 + 10 = F(F(9) - F(8)) + F(F(7)) = 6 + 5 \times 4 \times (F(3) + 21) = 6 + (5 + 43 - 2) \times 10$
- 467 := $-9 + F(8) + 7 \times 65 = F(F(4 + 3)) \times 2 + 1$
- 468 := $(-9 + 87) \times 6 = F(F(5 + F(F(4)))) \times F(3) + 2 \times 1 = F(5 + F(F(4))) \times 3 \times (2 + 10)$
- 470 := $F(9) \times (F(8) - 7) - 6 = 5 + F(F(4 + 3)) \times 2 - 1 = 5 \times F(4) \times 32 - 10$
- 472 := $(9 \times 8 - F(7)) \times F(6) = 5 + F(F(4 + 3)) \times 2 + 1 = (5 + F(4)) \times (F(3) + 2 + F(10))$
- 473 := $F(9) \times F(8) - F(F(7)) - F(6) = (F(F(5 + F(F(4)))) + 3) \times 2 + 1$
- 474 := $(9 \times 8 + 7) \times 6 = 54 + F(3) \times 210$
- 475 := $F(9) \times F(8) - F(F(7)) - 6 = 5 \times (F(4) \times 32 - 1)$
- 476 := $(9 + 8) \times (7 + F(F(6))) = (5 + F(F(4 + 3))) \times 2 \times 1 = 54 \times 3^2 - 10 = F(9) \times (8 + 7 - 6 + 5) = F(F(4 + 3)) \times 2 + 10 = F(9) \times (F(8) - 7) = 65 \times (4 + 3) + 21 = -6 - 5 + 432 + F(10)$
- 477 := $F(F(9) - F(8)) + F(F(7)) + 6 - 5 = F(4) \times 3 \times (-2 + F(10))$
- 481 := $F(9) \times F(8) - F(7 + 6) = 5 \times F(4) \times 32 + 1 = F(9) \times F(8) - F(F(7)) = (6 + 5 + 4) \times 32 + 1 = (6 + 5) \times 43 - 2 + 10$

- **482** := $F(9) \times (F(8) - 7) + 6 = -5 + 432 + F(10)$
- **483** := $9 \times 8 \times 7 - F(F(6)) = (5 \times 4 + 3) \times 21$
- **484** := $F(9) \times (F(8) - 7) + F(6) = (5 - F(4)^3)^{F(2+1)}$
- **486** := $9^{F(F(8)/7)} \times 6 = 54 \times 3^2 \times 1$
 $= 543 - 2 - F(10)$

- **487** := $F(9) \times (F(8) - 7) + 6 + 5 = 432 + F(10)$
 $:= F(9) \times F(8) - F(F(7)) + 6 = 54 \times 3^2 + 1$

- **488** := $-F(9) + 87 \times 6 = -5 - F(F(4)) + 3^2 \times F(10)$
- **489** := $F(9) \times (8 + 7) - F(F(6)) = F(F(5 + F(F(4)))) + F(3)^{-2+10}$
- **490** := $98 \times (F(7) - F(6)) = (-5 + F(4^{F(3)}))/2 - 1$
 $= 543 + 2 - F(10)$
- **491** := $9 \times 8 \times 7 - F(6) - 5 = -4 + 3^2 \times F(10)$
- **492** := $F(9) \times 8 + F(F(7)) - F(6) - 5 = -F(4) + 3^2 \times F(10)$
- **493** := $-F(9) \times 8 + 765 = -F(F(4)) + 3^2 \times F(10)$
- **494** := $(F(9) - 8) \times (F(7) + 6) = F(5 \times F(F(4))) \times 3^2 - 1$
 $= (5 \times 4 + F(3))^2 + 10$

- **495** := $F(9) + (87 + 6) \times 5 - 4 = 3^2 \times F(10)$
 $:= (98 + 7 - 6) \times 5 = (4 + 3 + 2) \times F(10)$
 $:= 9 \times (-F(8) + 76) = 5 \times F(4) \times (32 + 1)$
 $= (5 + 4) \times (-F(3) + 2 + F(10))$

- **496** := $9 \times 8 \times 7 - F(6) = F(5 \times F(F(4))) \times 3^2 + 1$
 $= 54 \times 3^2 + 10$
 $:= (F(9) - (1/7) \times F(8)) \times (F(F(6)) - 5) = F(4 \times F(3))^2 + F(10)$

- **497** := $F(9) \times (8 + 7) - F(6) - 5 = F(F(4)) + 3^2 \times F(10)$
 $:= F(9) \times 8 + F(F(7)) - F(6) = (5 + F(4^{F(3)}))/2 + 1$
 $= F(5 \times F(4)) - 3 - 2 \times F(10)$

- **498** := $F(9) + 8 \times (-7 + 65) = F(4) + 3^2 \times F(10)$
 $:= 9 \times 8 \times 7 - 6 = F(5 \times F(4)) - F(3) - 2 \times F(10)$

- **499** := $F(9) + (87 + 6) \times 5 = 4 + 3^2 \times F(10)$
 $:= F(9) \times 8 + F(F(7)) - 6 = 5^{F(4)} \times (F(3) + 2) - 1$

- **502** := $9 \times 8 \times 7 - F(F(6) - 5) = F(F(4))^{3^2} - 10$
 $:= F(9) \times (8 + 7) - F(6) = 5 + F(F(4)) + 3^2 \times F(10)$

- **504** := $9 \times 8 \times 7 = (6 + 54/3) \times 21$
 $= 6 \times (5 - F(4)) \times (32 + 10)$

$$\bullet \mathbf{505} := F(9) \times 8 + F(7+6) = (5 \times F(F(6)) - 4) \times (3 \times 2 - 1) \\ := F(9) \times 8 + F(F(7)) = F(6) \times 5 \times (4+3) \times 2 - F(10)$$

$$\bullet \mathbf{510} := 9 \times 8 \times 7 + 6 = (5 + F(4))^3 - 2 \times 1 \\ = 5 \times F(4) + 3^2 \times F(10) \\ := F(9) \times (8+7) = 6 + (5 + F(4)) \times 3 \times 21 \\ = 6 \times 5 \times F(4) + F(3) \times 210$$

$$\bullet \mathbf{511} := -F(9) + F(8+7) - 65 = F(F(4))^{3^2} - 1 \\ := F(9) \times 8 + F(F(7)) + 6 = 5 \times F(4) \times F(3^2) + 1 \\ = -5 + 43 \times (2+10)$$

$$\bullet \mathbf{512} := -9 + F(8+7) - F(6+5) = (4 \times F(3))^{2+1} \\ = 4^3 \times (-2+10) \\ := 9 \times 8 \times 7 + F(6) = (5 - F(4))^{3^2} \times 1$$

$$\bullet \mathbf{513} := 9 \times (87 - 6 \times 5) = F(F(4))^{3^2} + 1 \\ = F(4) \times 3 \times (2 + F(10)) \\ := -9 + 87 \times 6 = (5 + F(4))^3 + 2 - 1$$

$$\bullet \mathbf{516} := F(9) \times 8 + F(F(7)) + 6 + 5 = 43 \times (2+10) \\ := F(9) \times (8+7) + 6 = 5 + F(F(4))^{3^2} - 1 \\ = F(5 + F(4)) + 3^2 \times F(10)$$

$$\bullet \mathbf{518} := F(9) \times (8+7) + F(6) = 5 + F(F(4))^{3^2} + 1 \\ = 5^4 + 3 - 2 \times F(10)$$

$$\bullet \mathbf{520} := (9 \times 8 - 7) \times F(6) = (5 \times 4 + 32) \times 10$$

$$\bullet \mathbf{521} := F(9) + F(8) + F(F(7)) + F(F(6)+5) = F(F(4+3)) \times 2 + F(10) \\ := F(-9 + F(8)) + F(-7 + F(F(6))) = 5 + 43 \times (2+10)$$

$$\bullet \mathbf{522} := 9 \times (F(8) + 7 \times 6 - 5) = F(F(4))^{3^2} + 10$$

$$\bullet \mathbf{525} := 9 \times 8 \times 7 + F(F(6)) = 5^{4-F(3)} \times 21$$

$$\bullet \mathbf{526} := F(9) \times 8 + F(F(7)) + F(F(6)) = 5^{F(F(4))} \times F(F(3 \times 2)) + 1 \\ = 5 + F(F(4+3)) \times 2 + F(10)$$

$$\bullet \mathbf{534} := F(9 + F(F(8)/7)) \times 6 = F(5 \times F(4)) - F(F(3 \times 2)) - F(10)$$

$$\bullet \mathbf{538} := -9 \times 8 + F(7 + F(6)) = 5^4 - 32 - F(10)$$

$$\bullet \mathbf{540} := 9 \times (-F(8) + 76 + 5) = F(4)^3 \times 2 \times 10 \\ := (F(9) + 8 \times 7) \times 6 = 543 - 2 - 1$$

- **544** := $F(9) \times (8 - F(7) + F(F(6))) = 543 + 2 - 1$
- **545** := $F(9) \times 8 + F(7) \times F(F(6)) = 543 + 2 \times 1$
- **546** := $(F(9) + 8) \times F(7) = 6 + 543 - 2 - 1$
 $= 6 + 54 \times (3 - 2) \times 10$
- **550** := $-F(9) + F(8 + 7) - F(F(6)) - 5 = (4 \times 3 - 2) \times F(10)$
- **552** := $(F(9) + 8) \times F(7) + 6 = F(5 \times F(4)) - F(F(3) + 2) - F(10)$
- **554** := $(F(9) + 8) \times F(7) + F(6) = F(F(5 + F(F(4)))) + 321$
 $= F(5 \times F(4)) - F(3)/2 - F(10)$
- **555** := $(98 + 7 + 6) \times 5 = F(F(4) \times (3 + 2)) - F(10)$
 $\quad := -F(9) + F(8 + 7) - F(F(6)) = F(5 \times F(4)) - F(3^2 + 1)$
 $\quad = 543 + 2 + 10$
- **556** := $F(9) + 87 \times 6 = F(5 \times F(4)) + 3 - 2 - F(10)$
- **558** := $9 \times (8 \times 7 + 6) = F(5 \times F(4)) + F(F(3) + 2) - F(10)$
- **560** := $(-F(9) + 8 \times F(7)) \times F(6) = 5 \times F(F(4)) \times (3 - 2 + F(10))$
- **564** := $(-9 + F(8)) \times (7 \times 6 + 5) = 4 \times (-3 + F(2 + 10))$
- **566** := $9 \times F(8) + F(-7 + F(F(6))) = 5^4 - F(3) - 2 - F(10)$
- **567** := $-9 + 8 \times (7 + 65) = F(4)^3 \times 21$
 $\quad := 9 \times (F(8) + 7 \times 6) = (5 + 4) \times 3 \times 21$
- **568** := $-F(9) - F(8) + 7 \times F(6 + 5) = 4 \times (-F(3) + F(2 + 10))$
 $\quad := -F(9) - 8 + F(7 + F(6)) = F(5 \times F(4)) - F(3) \times 21$
 $\quad = F(5 \times F(4)) - 32 - 10$
- **570** := $(-9 + 8 \times F(7)) \times 6 = 5^4 - F(3^2 + 1)$
 $\quad = (-5 + 4^3 - 2) \times 10$
- **574** := $-F(9) + 8 \times 76 = 5^4 + F(3) + 2 - F(10)$
- **576** := $9 \times (-8 + 7 + 65) = F(F(4)) \times F(3) \times F(2 + 10)$
 $\quad := (9 + 87) \times 6 = F(5 \times F(4)) - F(3^2) \times 1$
 $\quad = -54 + 3 \times 210$
 $\quad := -F(9) + F(8 + 7) = 6 \times (54 + F(3) \times 21)$
 $\quad = 6 \times (54 + 32 + 10)$
- **578** := $(9 + 8) \times (F(7) + F(F(6))) = F(5 \times F(4)) - 32 \times 1$
 $\quad = 5^4 + F(3 \times 2) - F(10)$
- **579** := $-9 + (F(8) + 7) \times F(F(6)) = F(5 \times F(4)) - 32 + 1$
- **580** := $-9 - F(8) + F(7 + F(6)) = (54 + F(3) + 2) \times 10$
- **584** := $F(9) + (8 \times F(7) + 6) \times 5 = 4 \times (F(3) + F(2 + 10))$
 $\quad := -F(9) + 8 + F(7 + F(6)) = (5 \times 4 + 3)^2 + F(10)$

- **588** := $98 \times (7 - 6 + 5) = 4 \times (3 + F(2 + 10))$
 $:= (F(9) + 8) \times (-7 + F(F(6))) = (5^{F(F(4))} + 3) \times 21$
 $= F(5 \times F(4)) - 32 + 10$

- **590** := $-F(9) + 8 \times F(7) \times 6 = 5^4 - F(3^2) + 1$
 $= (54 + 3 + 2) \times 10$

- **593** := $-9 + F(8 + 7) - F(6) = 5^4 - 32 \times 1$

- **594** := $9 \times (87 - F(F(6))) = 5^4 - 32 + 1$
 $= 54 \times (3 - 2 + 10)$

- **595** := $-9 + F(8 + 7) - 6 = 5 \times (F(4)^{F(3)} + 2 \times F(10))$

- **597** := $9 + (F(8) + 7) \times F(F(6)) = F(5 \times F(4)) - F(3 \times 2 + 1)$
 $= F(5 \times F(4)) - F(F(3) \times 2) - 10$

- **598** := $9 - F(8) + F(7 + F(6)) = 5^4 - 3^{2+1}$

- **599** := $-9 + 8 \times 76 = F(5 \times F(4)) - 3 + 2 - 10$

- **600** := $(9 \times (F(8) - 7) - 6) \times 5 = F(F(4) \times (3 + 2)) - 10$

- **601** := $-9 + F(8 + F(7) - 6) = 5^4 - 3 - 21$
 $= 5^4 + 3 \times (2 - 10)$
 $:= -9 + F(8 + 7) = 6 \times 5 \times 4 \times (3 + 2) + 1$

- **605** := $F(9 \times (8 - 7) + 6) - 5 = (F(4 + 3) - 2) \times F(10)$

- **606** := $9 + F(8 + 7) - F(6) - 5 = -4 + F(3 + 2 + 10)$

- **607** := $9 \times (-8 + 76) + 5 = -F(4) + F(3 + 2 + 10)$
 $:= -9 + F(8 + 7) + 6 = 5^4 + 3 - 21$
 $= 5^4 + F(3) - 2 \times 10$

- **608** := $9 + F(8 + 7) - 6 - 5 = -F(F(4)) + F(3 + 2 + 10)$

- **609** := $9 \times 8 \times 7 + F(F(6)) \times 5 = F(F(4) \times (3 + 2)) - 1$
 $:= -9 + 8 + F(7 + F(6)) = (-5 + F(F(4) \times 3)) \times 21$
 $= 5^4 - 3 \times 2 - 10$

- **610** := $(98 + 7) \times 6 - 5 \times 4 = F(3 + 2 + 10)$
 $:= F(9) + 8 \times (7 + 65) = F((4 + 3) \times 2 + 1)$
 $= F(4 + 3 - 2 + 10)$
 $:= F(9 \times (8 - 7) + 6) = F(54/3 - 2 - 1)$
 $= (5 \times 4)^{F(3)} + 210$

- **611** := $(-9 + 8 \times 7) \times (F(6) + 5) = F(F(4) \times (3 + 2)) + 1$
 $:= 9 + F(8 + 7) - F(6) = F(5 \times F(4)) + F(3) - 2 + 1$
 $= 5^4 - F(3) - 2 - 10$

$$\begin{aligned}\bullet 612 &:= 9 + 8 \times 76 - 5 = F(F(4)) + F(3 + 2 + 10) \\ &:= 9 \times (-8 + 76) = 5^4 - F(3 \times 2 + 1) \\ &\quad = (54 - 3) \times (2 + 10)\end{aligned}$$

$$\begin{aligned}\bullet 613 &:= F(F(9) - F(8)) + 76 \times 5 = F(4) + F(3 + 2 + 10) \\ &:= 9 + F(8 + 7) - 6 = F(5 \times F(4)) + 3 \times (2 - 1) \\ &\quad = F(5 \times F(4)) + 3 + 21 \times 0\end{aligned}$$

$$\bullet 614 := F(9) + F(8 + 7) - 6 \times 5 = 4 + F(3 + 2 + 10)$$

$$\begin{aligned}\bullet 615 &:= -9 + 8 \times F(7) \times 6 = 5^4 - 3^2 - 1 \\ &\quad = 5^4 + F(3) - 2 - 10\end{aligned}$$

$$\begin{aligned}\bullet 619 &:= 9 + F(8 + F(7) - 6) = 5^4 - 3 - 2 - 1 \\ &\quad = 5^4 + F(3) + 2 - 10 \\ &:= 9 + F(8 + 7) = -6 + 5^4 - 3 + 2 + 1 \\ &\quad = -6 + 5 \times F(4) + F(3 + 2 + 10)\end{aligned}$$

$$\bullet 620 := 9 + F(8 + 7) + 6 - 5 = (4^3 - 2) \times 10$$

$$\bullet 621 := 98 \times 7 - 65 = F(4) \times (-3 + 210)$$

$$\begin{aligned}\bullet 622 &:= -9 + F(8) + F(7 + F(6)) = 5^4 - 3 \times (2 - 1) \\ &\quad = 5^4 - 3 + 21 \times 0\end{aligned}$$

$$\bullet 623 := F(9) - F(8) + F(7 + F(6)) = 5^4 - 3 + 2 - 1$$

$$\bullet 624 := (-9 + F(8)) \times (-F(7) + 65) = F(4) \times (-F(3) + 210)$$

$$\begin{aligned}&:= (-9 + 87) \times F(6) = 5^4 - 3/(2 + 1) \\ &\quad = 5^4 + 3^2 - 10\end{aligned}$$

$$\begin{aligned}\bullet 625 &:= 9 + F(8 + 7) + 6 = 5^4 - 3 + 2 + 1 \\ &\quad = 5^4 + 321 \times 0\end{aligned}$$

$$\bullet 626 := (F(9) + F(8)) \times F(7) - F(6 + 5) = -4 + 3 \times 210$$

$$\begin{aligned}\bullet 627 &:= -9 + F(8) + F(7 + F(6)) + 5 = -F(4) + 3 \times 210 \\ &:= 9 + 8 + F(7 + F(6)) = 5^4 + 3 - 2 + 1\end{aligned}$$

$$\bullet 628 := 9 + 8 \times F(7) \times 6 + 5 = -F(F(4)) + 3 \times 210$$

$$\begin{aligned}\bullet 630 &:= 9 + F(8 + 7) + 6 + 5 = F(4) \times F(F(3 \times 2)) \times 10 \\ &:= (98 + 7) \times 6 = 5 \times (4 + F(3)) \times 21 \\ &\quad = (5 - 4) \times 3 \times 210\end{aligned}$$

$$\begin{aligned}\bullet 632 &:= 9 + F(8 + 7) + F(6) + 5 = F(F(4)) + 3 \times 210 \\ &:= (9 \times 8 + 7) \times F(6) = 5^4 + 3 \times 2 + 1\end{aligned}$$

$$\begin{aligned}\bullet 633 &:= F(9) + F(8+7) - 6 - 5 = F(4) + 3 \times 210 \\ &:= 9 + 8 \times F(7) \times 6 = 5^4 + 3^2 - 1 \\ &= 5 - F(F(4)) + 3 \times 210\end{aligned}$$

$$\bullet 634 := F(9) + (8+7) \times F(6) \times 5 = 4 + 3 \times 210$$

$$\begin{aligned}\bullet 636 &:= (-9 + F(8)) \times (F(7) + F(6) \times 5) = F(4) \times (F(3) + 210) \\ &:= F(9) - 8 + F(7 + F(6)) = 5^4 + 3 - 2 + 10\end{aligned}$$

$$\begin{aligned}\bullet 638 &:= F(9) \times F(8) - 76 = 5^4 + F(3 \times 2 + 1) \\ &= 5 + F(4) + 3 \times 210\end{aligned}$$

$$\bullet 639 := -9 + 8 \times (76 + 5) = F(4) \times (3 + 210)$$

$$\begin{aligned}\bullet 640 &:= 9 + F(8) + F(7 + F(6)) = 5 \times 4 \times 32 \times 1 \\ &= (5 - F(4)) \times 32 \times 10 \\ &:= 9 + F(8) + F(F(7) + F(F(6) - 5)) = F(F(4)) \times 32 \times 10\end{aligned}$$

$$\begin{aligned}\bullet 642 &:= F(9) \times F(8) - 7 - 65 = F(F(4)) \times 321 \\ &:= F(9) + 8 \times 76 = (5 - F(4)) \times 321 \\ &= 5^4 - 3 + 2 \times 10\end{aligned}$$

$$\begin{aligned}\bullet 644 &:= F(9) + F(8 + F(7) - 6) = 5^4 - F(3) + 21 \\ &= 5^4 + 3^2 + 10 \\ &:= F(9) + F(8 + 7) = 654 - 3^2 - 1 \\ &= 654 \times (3 - 2) - 10\end{aligned}$$

$$\bullet 646 := F(9) \times (-F(F(8)/7) + F(F(6))) = F(5 + 4) \times (-F(3) + 21)$$

$$\begin{aligned}\bullet 648 &:= 9^{F(F(8)/7)} \times F(6) = 5^4 + F(3) + 21 \\ &= 5^4 + 3 + 2 \times 10\end{aligned}$$

$$\begin{aligned}\bullet 649 &:= F(9) \times 8 + F(-7 + F(F(6))) = 5^4 + 3 + 21 \\ &= 5^4 + 3 \times (-2 + 10)\end{aligned}$$

$$\bullet 650 := F(9) + F(8 + 7) + 6 = 5 \times 4 + 3 \times 210$$

$$\begin{aligned}\bullet 651 &:= (F(9) - F(8)/7) \times F(F(6)) = (F(5 + 4) - 3) \times 21 \\ &= F(5 + F(4)) + 3 \times 210\end{aligned}$$

$$\bullet 652 := F(9) + F(8 + 7) + F(6) = 5^4 + 3^{2+1}$$

$$\bullet 658 := F(9) \times F(8) - 7 \times F(6) = 5^4 + 32 + 1$$

$$\bullet 660 := (9 \times (F(8) - 7) + 6) \times 5 = (4^3 + 2) \times 10$$

$$\bullet 662 := -F(9) + 87 \times F(6) = F(5 \times F(4)) - F(F(3) + 2) + F(10)$$

$$\bullet 665 := 9 + 8 \times (-7 + F(6 + 5)) = F(F(4) \times (3 + 2)) + F(10)$$

$$\begin{aligned}&:= 98 \times 7 - F(F(6)) = F(5 \times F(4)) + F(3^2 + 1) \\ &= 5 + (4^3 + 2) \times 10\end{aligned}$$

- **666** := $(98 + F(7)) \times 6 = (5 + F(4 \times F(3)))^2 - 10$
- **672** := $F(9) \times F(8) - 7 \times 6 = (5 + F(4)^3) \times 21 = (54 + F(3)) \times (2 + 10)$
- **674** := $F(9) + F(8 + 7) + 6 \times 5 = F(4)^{3 \times 2} - F(10)$
- **678** := $98 \times 7 - F(6) = F(F(5 + F(F(4)))) \times 3 - 21 = (5^{F(F(4))})^{F(3)} - 2 + F(10)$
- **680** := $(9 + F(8) - F(7)) \times F(6) \times 5 = F(F(4) \times 3) \times 2 \times 10$
 $\quad := 98 \times 7 - 6 = 5 \times 4 \times F(3^2) \times 1 = 5 \times (F(4 \times 3) + 2 - 10)$
- **682** := $9 \times 8 + F(7 + F(6)) = 5^{F(F(4)) \times F(3)} + 2 + F(10)$
- **684** := $9 \times (87 - 6 - 5) = 4 \times 3 \times (2 + F(10))$
- **686** := $98 \times (F(7) - 6) = (5 + F(F(4)))^3 \times 2 \times 1 = 5^4 + 3 \times 2 + F(10)$
- **687** := $(-9 + 87 \times F(6)) = (5 + F(F(4)))^3 \times 2 + 1 = 543 + F(2 + 10)$
- **689** := $98 \times 7 + F(6) - 5 = F(4 + 3) \times (-2 + F(10))$
- **693** := $9 \times (F(8) + 7 \times F(6)) = F(5 + F(4)) \times (32 + 1)$
- **694** := $98 \times 7 + F(6) = -5 + F(F(4 + 3)) \times (2 + 1)$
- **695** := $F(9) \times F(8) - F(7) - 6 = 5 \times 4 \times 32 + F(10)$
- **699** := $9^{F(8)/7} - 6 \times 5 = F(F(4 + 3)) \times (2 + 1)$
 $\quad := F(9) \times F(8) - 7 - F(6) = 5 \times F(4 \times 3) - 21$
- **700** := $F(9) \times F(8) + 7 - F(F(6)) = 5 \times 4 \times (F(3^2) + 1)$
 $\quad = 5 \times (4 + 3) \times 2 \times 10$
- **701** := $F(9) \times F(8) - 7 - 6 = F(F(5 + F(F(4)))) \times 3 + 2 \times 1$
 $\quad = 5^4 + F(F(3 \times 2)) + F(10)$
 $\quad := F(9) \times F(8) - F(7) = (6 + 5) \times 4^3 - 2 - 1$
- **705** := $9 + 87 \times F(6) = 5 \times (F(4 \times 3) - 2 - 1)$
 $\quad = 5 \times (43 \times 2 + F(10))$
- **707** := $98 \times 7 + F(F(6)) = F(F(5 + F(F(4)))) \times 3 - 2 + 10$
 $\quad := F(9) \times F(8) - 7 = (6 + 5) \times 4^3 + 2 + 1$
 $\quad = F(F(F(6)) - 5) + (4 - 32) \times 10$
- **708** := $98 + F(7 + F(6)) = (5 + 4)^3 - 21$
- **709** := $(F(9) + F(8)) \times F(7) - 6 = 5 \times (F(4 \times 3) - 2) - 1$
 $\quad = (5 + 4)^3 - 2 \times 10$
- **711** := $9 \times (87 - F(6)) = 5 \times (F(4 \times 3) - 2) + 1$
- **712** := $F(9 + F(F(8)/7)) \times F(6) = 5 \times F(4 \times 3) + 2 - 10$
- **713** := $F(9) \times F(8) - 7 + 6 = F(5 + 4) \times F(F(3 \times 2)) - 1$

- **714** := $(F(9) + F(8)) \times F(7) - 6 + 5 = F(F(4) \times 3) \times 21$
 $\quad := (9 + 8) \times 7 \times 6 = F(5 + 4) \times F(3^2 - 1)$
 $\quad = 5^4 + F(3 - 2 + 10) = 6 + (5 + 4)^3 - 21$
 $\quad := F(9) \times (8 + F(7)) = 7 \times (6 \times 5 \times 4 + 3 - 21)$
 $\quad := F(9) \times F(8) = (76 - 54) \times 32 + 10$

- **715** := $(9 + 8 \times 7) \times (6 + 5) = (4 + 3^2) \times F(10)$
 $\quad := (F(9) + F(8)) \times F(7) = 65 \times (4 \times 3 - 2 + 1)$
 $\quad = 65 \times (-4 + 3 + 2 + 10)$
 $\quad := F(9) \times F(8) + 7 - 6 = 5 \times ((4 \times 3)^2 - 1)$
 $\quad = 5^4 + 3^2 \times 10$

- **719** := $(9 + 8) \times 7 \times 6 + 5 = F(4)^{3 \times 2} - 10$
 $\quad := F(9) \times F(8) + F(7) - F(6) = 5 \times (4 \times 3)^2 - 1$

- **720** := $9 \times (8 + 7 + 65) = F(4 \times 3)/2 \times 10$
 $\quad := -9 + (F(8)/7)^6 = 5 \times (4 \times 3)^2 \times 1$
 $\quad = 5 \times 4 \times 3 \times (2 + 10)$

- **721** := $9^{F(8)/7} - F(6) = 5 \times (4 \times 3)^2 + 1$
 $\quad = (5 + 4)^3 + 2 - 10$
 $\quad := F(9) \times F(8) + 7 = 6 \times 5 \times 4 \times 3 \times 2 + 1$

- **722** := $F(9) \times (8 + F(7)) + F(6) = 5 \times F(4 \times 3) + 2 \times 1$
 $\quad = F(5 \times F(4)) + F(3) + 2 \times F(10)$

- **723** := $9^{F(8)/7} - 6 = 5 \times F(4 \times 3) + 2 + 1$
 $\quad = F(5 \times F(4)) + 3 + 2 \times F(10)$

- **726** := $(F(9) + 87) \times 6 = (5 + 4)^3 - 2 - 1$

- **727** := $F(9) \times F(8) + 7 + 6 = (5 + 4)^3 - 2 \times 1$
 $\quad := F(9) \times F(8) + F(7) = -F(6) + 5 \times (4 + 3) \times 21$
 $\quad = -F(6) + 5 \times 4 \times F(3^2) + F(10)$

- **728** := $9^{F(8)/7} - 6 + 5 = F(4)^{3 \times 2} - 1$
 $\quad := (98 - 7) \times F(6) = (5 + 4)^3 - 2 + 1$

- **729** := $9^{8 \times (7-6)-5} = F(4)^{3 \times 2} \times 1$
 $\quad := 9^{F(8)/7} = 6 - 5 + F(4)^{3 \times 2} - 1$

- **730** := $(-9 + F(8) \times 7 + F(6)) \times 5 = F(4)^{3 \times 2} + 1$
 $\quad := F(9) + 87 \times F(6) = 5 \times (F(4 \times 3) + 2) \times 1$
 $\quad = 5 \times (-4^3 + 210)$

- **733** := $F(9) \times F(8) + F(7) + 6 = 5 + F(4)^{3 \times 2} - 1 = 5^4 - F(3) + 2 \times F(10)$
- **735** := $9^{F(8)/7} + 6 = 5 \times (4 + 3) \times 21 = -5 \times F(4) \times (3 \times 2 - F(10))$
- **736** := $(F(9) + F(8)) \times F(7) + F(F(6)) = -5 + F(4 + 3) \times (2 + F(10))$
- **737** := $9^{F(8)/7} + F(6) = (5 + 4)^3 - 2 + 10$
- **738** := $9 + (F(8)/7)^6 = 5^4 + 3 + 2 \times F(10)$
- **739** := $-F(9) + 8 + 765 = F(4)^{3 \times 2} + 10$
- **741** := $-F(9) + (8 + 7 \times F(F(6))) \times 5 = F(4 + 3) \times (2 + F(10))$
- **742** := $F(9) \times F(8) + 7 + F(F(6)) = (5 + F(F(4))) \times F(3) \times (-2 + F(10))$
- **748** := $F(9) \times (F(8) + 7 - 6) = F(5 + 4) \times (F(F(3 \times 2)) + 1) = F(5 + 4) \times (32 - 10)$
- **750** := $9^{F(8)/7} + F(F(6)) = (5 + 4)^3 + 21$
- **754** := $F(98/7) \times F(F(6) - 5) = F(F(4)) \times F(F(3) + 2 + 10)$
 $= F(-9 + F(8)) + F(7 + F(6)) = F(5 + F(4) \times 3) \times 2 \times 1$
- **756** := $9 \times (8 + 76) = (F(5 + 4) + F(3)) \times 21 = 54 \times (F(3) + 2 + 10)$
- **760** := $(-9 + 8 \times F(7)) \times F(6) = (-5 + 43) \times 2 \times 10$
- **763** := $F(9) + (F(8)/7)^6 = -5 + 4^3 \times (2 + 10)$
- **768** := $-9 + F(8) \times (7 + 6 \times 5) = 4^3 \times (2 + 10)$
 $= (9 + 87) \times F(6) = (5 - F(F(4))) \times F(3)^{-2+10}$
- **770** := $9 \times 87 - F(6) - 5 = (4 + 3) \times 2 \times F(10)$
 $= F(9) \times F(8) + 7 \times F(6) = (-5 + 4 \times 3) \times 2 \times F(10)$
- **774** := $9 \times (8 + F(7) \times 6) = (5^{F(F(4))} + 3)^2 - 10$
- **775** := $9 \times 87 - F(6) = 5^{F(F(4))} \times (32 - 1)$
 $= 5 + (4 + 3) \times 2 \times F(10)$
- **777** := $-9 + F(8) + 765 = F(4^{F(3)}) - 210$
 $= 9 \times 87 - 6 = (F(5 + 4) + 3) \times 21$
 $= 5 \times F(4 \times 3) + 2 + F(10)$
- **782** := $F(9) \times (8 + 7 + F(6)) = F(5 + 4) \times (F(3) + 21)$
- **783** := $9 \times 87 = 6 \times 5^{F(4)} + 32 + 1$
 $= F(6) \times (5 + 43 \times 2) + F(10)$
- **784** := $9 \times 87 + 6 - 5 = F(4)^{3 \times 2} + F(10)$
 $= 98 \times (-F(7) + F(F(6))) = (5^{F(F(4))} + 3)^2 \times 1$
 $= (5 + F(F(4))) \times (F(3) + 2 \times F(10))$

- **786** := $(F(-9 + F(8)) - F(7)) \times 6 = (5 + 4)^3 + 2 + F(10)$
- **789** := $9 \times 87 + 6 = 5 + F(4)^{3 \times 2} + F(10)$
- **790** := $F(9) \times F(8) + 76 = 5^{F(F(4))} \times 32 - 10$
- **791** := $9 \times 87 + F(6) = (5 + F(F(4))) \times (3 + 2 \times F(10))$
- **798** := $(F(9) + 8) \times (F(7) + 6) = (-5 + 43) \times 21$
- **799** := $9 \times F(8) + F(7 + F(6)) = 5^{F(F(4))} \times 32 - 1.$

- **801** := $9 \times F(-8 + F(7) + 6) = 5^{F(F(4))} \times 32 + 1$
 $= (5 + 4) \times F(3 - 2 + 10)$
- **810** := $9 \times (87 + F(6) - 5) = (F(4) \times 3)^2 \times 10$

- **816** := $F(9) \times F(8) / 7 \times F(6) = F(5 + 4) \times (3 + 21)$
 $= F(5 + 4) \times 3 \times (-2 + 10)$
- **818** := $F(9) \times F(8) + F(7) \times F(6) = F(5 \times F(4)) - F(3) + 210$
- **819** := $(F(9) \times 8 - F(F(7))) \times F(F(6)) = F(5 + F(F(4))) \times 3 \times 21$
- **822** := $(F(-9 + F(8)) - 7) \times 6 = F(5 \times F(4)) + F(3) + 210$
- **823** := $-9 + 8 \times F(7) \times F(6) = -5 + 4 \times (-3 + 210)$

- **825** := $(F(9) + F(8)) \times (7 + F(6)) = 5 \times (F(4 \times 3) + 21)$
 $= F(5 \times F(F(4))) \times (3 + 2 + 10)$
 $\quad := 9 + 8 \times (F(7) + F(6 + 5)) = F(4) \times (3 + 2) \times F(10)$

- **828** := $-9 - 8 + F(7) \times 65 = 4 \times (-3 + 210)$
 $\quad := (-9 + F(8) \times 7) \times 6 = (5 + 4^3) \times (2 + 10)$
- **832** := $9 \times (87 + 6) - 5 = 4 \times (-F(3) + 210)$
- **837** := $9 \times (87 + 6) = 5^4 + F(3) + 210$
- **840** := $(9 - 8 + 7) \times F(F(6)) \times 5 = 4 \times F(F(3 \times 2)) \times 10$
 $\quad := (98 + 7) \times F(6) = 5 \times 4 \times F(3) \times 21$
 $\quad = 5 \times 4 \times (32 + 10)$

- **841** := $9 + 8 \times F(7) \times F(6) = (-5 + F(F(4) \times 3))^2 \times 1$
- **842** := $-F(9) + 876 = (5 - F(F(4) \times 3))^2 + 1$

- **843** := $-F(9) + F(8) \times 7 \times 6 - 5 = F(4^{F(3)}) - F(2 + 10)$
 $\quad := F(F(9) - F(8)) + F(7 + F(6)) = F(5 \times F(4)) + F(F(3 \times 2 + 1))$
 $\quad = -5 + 4 \times (F(3) + 210)$

- **848** := $9 \times 87 + 65$
 $= -F(9) + F(8) \times 7 \times 6$
 $= 4 \times (F(3) + 210)$
 $= (F(5 + F(F(4))) + 3) \times (-2 + F(10))$
- **852** := $(-9 + F(8)) \times (76 - 5)$
 $= 4 \times (3 + 210)$
- **855** := $9 \times (87 + F(6))$
 $= -5 + 43 \times 2 \times 10$
- **860** := $9 \times (87 + F(6)) + 5$
 $= 43 \times 2 \times 10$
- **864** := $9 \times 8 \times (F(7) - 6 + 5)$
 $= F(F(4)) \times 3 \times F(2 + 10)$
 $\quad := F(9 + F(8)/7) \times 6$
 $= 54 \times (3 \times 2 + 10)$
- **866** := $F(9) + 8 \times F(7) \times F(6)$
 $= F(5 \times F(4)) + F(3)^{-2+10}$
- **873** := $9 \times (F(8) + 76)$
 $= (5 + 4)^3 + F(2 + 10)$
- **877** := $F(9) \times 8 + F(7 + F(6)) - 5 = F(4^{F(3)}) - 2 \times F(10)$
- **880** := $9 + 876 - 5$
 $= 4 \times F(3) \times 2 \times F(10)$
- **882** := $9 \times (8 \times F(7) - 6)$
 $= F(5 + F(4)) \times F(3) \times 21$
 $= F(5 + F(4)) \times (32 + 10)$
- **885** := $9 + 876$
 $= 5 \times F(4) \times (F(3) + 2 + F(10))$
- **890** := $9 + 876 + 5$
 $= F(F(4 + 3) - 2) \times 10$
- **903** := $(9 - F(8)) \times 7 + F(F(F(6))) - 5 = 43 \times 21$
- **904** := $(9 + 8 \times F(7)) \times F(6)$
 $= (5 + F(4)) \times (3 + 2 \times F(10))$
- **906** := $(F(-9 + F(8)) + 7) \times 6$
 $= (F(5 + 4) - 3)^2 - F(10)$
- **910** := $F(9) + 876$
 $= (5 + 43 \times 2) \times 10$
- **912** := $(-9 + F(8)) \times 76$
 $= (5 + F(4)) \times F(3) \times (2 + F(10))$
 $\quad := (9 - F(8)) \times (F(7) - F(6 + 5))$
 $= 4^{F(3)} \times (2 + F(10))$
- **915** := $9 \times 8 \times F(7) - F(F(6))$
 $= F(5 \times F(4))/F(3) \times (2 + 1)$
- **918** := $F(9) \times (8 + F(7) + 6)$
 $= F(5 + 4) \times 3^{2+1}$
 $= 54 \times (-3 + 2 \times 10)$
- **924** := $(-9 \times F(8) + F(F(7))) \times F(F(6)) = F(5 + F(4)) \times (F(3^2) + 10)$
- **930** := $(F(-9 + F(8)) + 7 \times 6) \times 5 = F(4^{F(3)}) - 2 - F(10)$
 $\quad := 9 \times 8 \times F(7) - 6$
 $= (5^{F(4)} - 32) \times 10$
- **931** := $F(9) \times (F(8) + 7) - F(F(6))$
 $= F(5 \times F(4)) + 321$
- **932** := $-F(9) - 8 - F(7) + F(F(F(6))) - 5 = 4 \times F(F(3 \times 2 + 1))$
- **934** := $F(9) \times F(8) + F(F(7)) - F(6) - 5$
 $= (F((4^{F(3)})) + 2) - F(10)$
- **935** := $(98 - F(7)) \times (6 + 5)$
 $= (F((F(4) \times 3))/2) \times F(10)$
- **936** := $9 \times 8 \times F(7)$
 $= 6 \times (54 - F(3)) \times (2 + 1)$
 $= (6 + 5) \times 43 \times 2 - 10$
- **939** := $F(9) \times F(8) + F(F(7)) - F(6) = (5 + 4)^3 + 210$
- **942** := $9 \times 8 \times F(7) + 6$
 $= F(F(5 + F(F(4)))) \times F(3) \times 2 + 10$
- **945** := $9 \times (-8 + F(7)) \times F(F(6))$
 $= 5 \times F(4) \times 3 \times 21$
 $= 5^4 + 32 \times 10$
- **946** := $F(9) \times (F(8) + 7) - 6$
 $= 5^4 + 321$

- **947** := $F(9) \times F(8) + F(F(7))$ = $-F(F(6)) + 5 + F(4) \times 321$
- **952** := $F(9) \times (F(8) + 7)$ = $6 + 5^4 + 321$
 $= 6 \times 54 \times 3 - 2 \times 10$
- **953** := $F(9) \times F(8) + F(F(7)) + 6$ = $-F(5 + 4) + F(3 \times 2 + 10)$
- **955** := $F(9) \times F(8) + F(F(7)) + F(6)$ = $-5 + F(4) \times 32 \times 10$
- **958** := $F(9) \times (F(8) + 7) + 6$ = $-5 + F(4) \times 321$
- **960** := $(9 + 8 + 7) \times F(6) \times 5$ = $F(4) \times (32 \times 10)$
 \vdots := $F(9) \times (F(8) + 7) + F(6) = 5 \times 4^3 \times (2 + 1)$
 $= (5 + 43) \times 2 \times 10$
- **963** := $-9 - 8 - 7 + F(F(F(6)) - 5) = F(4) \times 321$
- **966** := $9 + 87 \times (6 + 5) = F(4^{F(3)}) - 21$
 \vdots := $987 - F(F(6)) = F((5 + F(4)) \times F(3)) - 21$
- **967** := $9 \times (87 + F(F(6))) - 5$ = $F(4^{F(3)}) - 2 \times 10$
- **968** := $(F(9) + 87) \times F(6)$ = $5 + F(4) \times 321$
- **972** := $9 \times (87 + F(F(6)))$ = $54 \times (-3 + 21)$
- **975** := $(-9 - F(8) + F(F(7)) - F(6)) \times 5 = F(4^{F(3)}) - 2 - 10$
- **977** := $F(9) \times F(8) + F(F(7)) + 6 \times 5$ = $F(4 \times (F(3) + 2)) - 10$
- **978** := $-9 + F(F(8) - F(7) + F(6))$ = $-5 - 4 + F(3 \times 2 + 10)$
- **979** := $F(9) + F(8) \times (F(F(7)) - F(6))/5 = F(4^{F(3)}) + 2 - 10$
 \vdots := $987 - F(6) = -5 + F(4^{F(3)}) - 2 - 1$
- **981** := $987 - 6$ = $-5 + F(4^{F(3)}) - 2 + 1$
- **983** := $(F(9) - F(8)) \times 76 - 5 = -4 + F(3 \times 2 + 10)$
- **984** := $987 - F(6) + 5$ = $F(4^{F(3)}) - 2 - 1$
- **985** := $987 - F(F(6) - 5)$ = $F(4^{F(3)}) - 2 \times 1$
- **986** := $987 - 6 + 5$ = $F(4^{F(3)}) - 2 + 1$
 \vdots := $F(9) \times (8 + F(7) + F(6)) = F(54/3 - 2) - 1$
- **987** := $987 \times (6 - 5)^4 = F(3 \times 2 + 10)$
 \vdots := $987 \times (6 - 5) = F(4 \times (3 + 2 - 1))$
 $= F(4 \times 3/2 + 10)$
 \vdots := $F((9 + 87)/6) = F((5 + 43)/(2 + 1))$
- **988** := $987 + 6 - 5$ = $F(4^{F(3)}) + 2 - 1$
 \vdots := $(F(9) - F(8)) \times 76 = F(54/3 - 2) + 1$
- **989** := $987 + F(F(6) - 5) = F(4^{F(3)}) + 2 \times 1$

- **990** := $987 + F(6) - 5 = F(4^{F(3)}) + 2 + 1 = F(4) \times 3 \times 2 \times F(10)$
 $= 9 \times (8 \times F(7) + 6) = 5 + F(4^{F(3)}) - 2 \times 1 = -5 \times (4 \times 3 - 210)$
- **991** := $F(9) + 87 \times (6 + 5) = 4 + F(3 \times 2 + 10)$
- **993** := $987 + 6 = 5 + F(4^{F(3)}) + 2 - 1$
- **995** := $9 \times (8 \times F(7) + 6) + 5 = F(4^{F(3)}) - 2 + 10$
 $= 987 + F(6) = 5 + F(4^{F(3)}) + 2 + 1$
- **996** := $9 + F(F(8) - F(7) + F(6)) = 5 + 4 + F(3 \times 2 + 10)$
- **997** := $9 + 8 - 7 + F(F(F(6)) - 5) = F(4 \times (F(3) + 2)) + 10$
- **999** := $9 + F(8)/7 + F(F(F(6)) - 5) = F(4^{F(3)}) + 2 + 10$

Acknowledgement

The author is thankful to T.J. Eckman, Georgia, USA (email: jeek@jeek.net) in programming the script to develop these representations.

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