

Factorial-Power Selfie Expressions – II

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Abstract

*This paper brings numbers in such a way that both sides of the expressions are with same digits. One side is digits with factorial and other side are with same digits with same powers but with different permutations. These types of expressions, we call as **selfie expressions**. This we have done with two ways. One having only positive sign and second with positive and negative signs. In both the cases operation of multiplication and composite relation are used. In case of positive sign, the results are up to five terms expressions*

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1 Selfie Expressions

Selfie expressions are very much similar to **selfie numbers** [4]. Selfie numbers are represented by its own digits by use of some operations, while **selfie expressions** are the expressions where both sides have same digits, not necessarily same operations on both sides, i.e., **same digits equality expressions**. Below are different ways of expressing equalities with same digits on both sides:

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- **Multiplicative Equalities**

$$abcd\dots \times efgh\dots = cbad\dots \times gfhe\dots \quad \forall a, b, c, d, e, \dots \in \mathbb{N}_+. \quad (1)$$

- **Power and Addition**

$$a^b + c^d + \dots = ab + cd + \dots, \quad \forall a, b, c, d, \dots \in \mathbb{N}. \quad (2)$$

- **Factorial and Power**

$$a! \times b! + (c! + d!) \times e! + \dots = a^a + b^b - c^c \times (d^d - e^e) + \dots, \quad \forall a, b, c, d, e, \dots \in \mathbb{N}_+, \text{ etc.} \quad (3)$$

$$a! \times b! + (c! + d!) \times e! + \dots = a^c + (b^d - c^a) \times d^e - e^b + \dots, \quad \forall a, b, c, d, e, \dots \in \mathbb{N}_+, \text{ etc.} \quad (4)$$

Let us explain one by one, the idea of above four **selfie expressions**, i.e., (1)–(4). This is done separately in each subsection.

1.1 Multiplicative Selfie Equalities

This subsection brings results based on the expression (1). By **multiplicative selfie equalities**, we understand that there are equalities, where each side is separated by operation of multiplications having same digits on both sides, not necessarily in same order. There are many ways of writing these kind of numbers explained in following subsections.

1.1.1 First Type

In this case, we have multiplicative equalities with equal number of digits on both sides and also in each multiplicative factor. The operation of multiplications is with number and its reverse forming a palindromic-type expression. For example, Based on idea of expressions are written in such a way that numbers formed by same digits multiplied by its reverse are equal to another group of multiplicative factors with same digits but of different numbers. See below some examples:

- | | |
|---|---|
| <ul style="list-style-type: none"> ◊ $37468 \times 86473 = 47386 \times 68374.$ ◊ $37596 \times 69573 = 39756 \times 65793.$ ◊ $39648 \times 84693 = 48396 \times 69384.$ ◊ $45495 \times 59454 = 49545 \times 54594.$ ◊ $46069 \times 96064 = 64096 \times 69046.$ | <ul style="list-style-type: none"> ◊ $120024 \times 420021 = 210042 \times 240012.$ ◊ $102204 \times 402201 = 201402 \times 204102.$ ◊ $130026 \times 620031 = 260013 \times 310062.$ ◊ $120036 \times 630021 = 210063 \times 360012.$ ◊ $102306 \times 603201 = 201603 \times 306102.$ |
|---|---|

1.1.2 Second Type

The second case is similar to first one, having the same number of digits in each multiplicative factor but not forming a palindromic-type expression. For example,

- | | |
|---|--|
| <ul style="list-style-type: none"> ◊ $2017 \times 3404 = 1702 \times 4034$ ◊ $2017 \times 6808 = 1702 \times 8068.$ ◊ $1729 \times 3584 = 1792 \times 3458.$ ◊ $1729 \times 3854 = 1927 \times 3458.$ | <ul style="list-style-type: none"> ◊ $1729 \times 4358 = 2179 \times 3458.$ ◊ $1729 \times 4732 = 2197 \times 3724.$ ◊ $1729 \times 5438 = 2719 \times 3458.$ ◊ $1729 \times 5781 = 1927 \times 5187.$ |
|---|--|

1.1.3 Third Type

The third case is similar to second one, but there is no rule with order of digits. Only thing is that on both sides of the equality sign, there are same digits. There are many numbers, but we have written only those with more than one equality sign. See below examples,

$$\diamond 162 \times 8064 = 216 \times 6048 = 648 \times 2016.$$

$$\diamond 162 \times 8073 = 207 \times 6318 = 702 \times 1863.$$

$$\diamond 17 \times 35945 = 35 \times 17459 = 395 \times 1547.$$

$$\diamond 176 \times 7469 = 194 \times 6776 = 776 \times 1694.$$

$$\diamond 18 \times 39879 = 189 \times 3798 = 378 \times 1899.$$

$$\diamond 18 \times 41553 = 54 \times 13851 = 513 \times 1458.$$

$$\diamond 1782 \times 43956 = 2178 \times 35964 = 3564 \times 21978 = 4356 \times 17982.$$

$$\diamond 18 \times 2830464 = 486 \times 104832 = 1404 \times 36288 = 3024 \times 16848.$$

$$\diamond 18 \times 5204736 = 162 \times 578304 = 3456 \times 27108 = 4518 \times 20736.$$

$$\diamond 198 \times 179982 = 297 \times 119988 = 1188 \times 29997 = 1782 \times 19998.$$

$$\diamond 198 \times 339966 = 396 \times 169983 = 1683 \times 39996 = 3366 \times 19998.$$

$$\diamond 2 \times 12089121 = 11 \times 2198022 = 222 \times 108911 = 1221 \times 19802.$$

Due to large quantity of numbers, we worked only with double or higher equality signs. Some times these expressions with single equality are famous as **vamp numbers**.

1.2 Power and Addition

Following the idea of expression (2) the author wrote the numbers **2017** [5] and **1729** [6] as:

$$\begin{aligned} 2017 &:= 4^4 + 41^2 + 77^0 + 79^1 &= 44 + 412 + 770 + 791. \\ &:= 1^4 + 44^2 + 77^0 + 79^1 &= 14 + 442 + 770 + 791. \\ &:= 2^4 + 2^8 + 4^2 + 12^3 + 180^0 &= 24 + 28 + 42 + 123 + 1800. \\ &:= 1^1 + 3^6 + 5^4 + 5^4 + 6^2 + 180^0 &= 11 + 36 + 54 + 54 + 62 + 1800. \end{aligned}$$

$$\begin{aligned} 1729 &:= 2^7 + 40^2 + 130^0 &= 27 + 402 + 1300. \\ &:= 2^6 + 40^2 + 64^1 + 66^0 &= 26 + 402 + 641 + 660. \\ &:= 1^6 + 41^2 + 46^1 + 84^0 &= 16 + 412 + 461 + 840. \end{aligned}$$

Below are more examples,

$$81 := 2^3 + 2^6 + 3^2 = 23 + 26 + 32.$$

$$\begin{aligned} 246 &:= 5^2 + 5^2 + 14^2 = 52 + 52 + 142. \\ 266 &:= 4^2 + 9^2 + 13^2 = 42 + 92 + 132. \\ 286 &:= 6^2 + 9^2 + 13^2 = 62 + 92 + 132. \\ 306 &:= 8^2 + 11^2 + 11^2 = 82 + 112 + 112. \\ &:= 9^2 + 9^2 + 12^2 = 92 + 92 + 122. \end{aligned}$$

$$99 := 2^3 + 3^3 + 4^3 = 23 + 33 + 43.$$

$$121 := 2^3 + 2^6 + 7^2 = 23 + 26 + 72.$$

$$170 := 2^6 + 5^2 + 9^2 = 26 + 52 + 92.$$

$$246 := 2^2 + 11^2 + 11^2 = 22 + 112 + 112.$$

In the above examples, the equality expressions are formed by three terms on both sides, while the numbers 2017 and 1729 are with **different terms expressions**. More detailed study can be seen at author's work [9, 10]. In these works, instead of using only positive sign, both positive and negative signs are used. For more study on numbers refer historical work [1, 2, 3].

1.3 Factorial and Power

Recently, author [11] worked on results arising due to (3). This we have done in two different ways. One without any repetition of digits. The second we have done with repetition of digits. In both the case the power in the right side of the equality is same as of the base. Both sides of the equality are with the operations as, positive, negative, multiplication, and composition relation. See below some examples in each case:

1.3.1 Different Digits

$$\begin{aligned}
 144 &:= (2! - 1!) \times 3! \times 4! = -2^2 \times (1^1 + 3^3) + 4^4. \\
 147 &:= 1! + 2! + 3! \times 4! = -1^1 - 2^2 \times 3^3 + 4^4. \\
 148 &:= (1! + 4!) \times 3! - 2! = 1^1 \times 4^4 - 3^3 \times 2^2. \\
 152 &:= 2! + 3! \times (1! + 4!) = 2^2 \times (-3^3 + 1^1) + 4^4. \\
 286 &:= (-1! + 3! \times 4!) \times 2! = -1^1 + 3^3 + 4^4 + 2^2. \\
 287 &:= -1! + 2! \times 3! \times 4! = 1^1 \times 2^2 + 3^3 + 4^4. \\
 288 &:= 1! \times 2! \times 3! \times 4! = 1^1 + 2^2 + 3^3 + 4^4.
 \end{aligned}$$

1.3.2 Repetition of Digits

$$\begin{aligned}
 108 &:= 2! \times (3! + 4! + 4!) = 2^2 \times 3^3 + 4^4 - 4^4 \\
 &:= 3! \times (3! + 3! \times 2!) = (3^3 + 3^3 - 3^3) \times 2^2 \\
 &:= -5! + 2! \times (5! - 3!) = (5^5 + 2^2 - 5^5) \times 3^3 \\
 &:= (-3! + 5!) \times 2! - 5! = 3^3 \times (5^5 + 2^2 - 5^5) \\
 &:= (2! \times 3! + 3!) \times 3! \times 1! = (2^2 + 3^3 - 3^3) \times 3^3 \times 1^1 \\
 &:= (1! \times 1! + 2!) \times 3! \times 3! = (-1^1 - 1^1 + 2^2) \times (3^3 + 3^3) \\
 &:= (1! \times 3! + 3! + 3!) \times 3! = 1^1 \times 3^3 + 3^3 + 3^3 \\
 &:= (4! + 3! \times 1! + 4!) \times 2! = (4^4 + 3^3 \times 1^1 - 4^4) \times 2^2 \\
 &:= (-3! + 5! \times 1!) \times 2! - 5! = (5^5 \times 1^1 + 3^3 - 5^5) \times 2^2.
 \end{aligned}$$

$$\begin{aligned}
 1008 &:= ((4! - 2!) \times 4! - 4!) \times 2! = (4^4 - 2^2 - 4^4 + 4^4) \times 2^2 \\
 &:= (2! + 2! + 4!) \times 3! \times 3! = 2^2 \times (-2^2 + 4^4) - 3^3 + 3^3 \\
 &:= (2! - 1! + 3!) \times 3! \times 4! = -2^2 + (1^1 + 3^3) \times 3^3 + 4^4 \\
 &:= 2! \times (2! \times (5! + 5!) + 4!) = 2^2 \times (-2^2 - 5^5 + 5^5 + 4^4).
 \end{aligned}$$

We observe that the (4) is different from the (3) in right side of the expression. In case (3), the power of digits is same as of bases. This is what we have given examples above. In case of (4), it is not necessary that the power is

same as of digits, but is a permutation of same digits as of bases. See below more general way.

$$(a!, b!, c!, \dots) = (a^a, b^b, c^c, \dots)$$

$$(a!, b!, c!, \dots) = (a, b, c, \dots)^{(a,b,c,\dots)}.$$

The first expression is simplified form of (3) and the second expression is similar to (4). The aim of this work is bring numbers based on (4).

2 Factorial-Power Selfie Expressions: Permutable Power

In this paper, our aim is to work with examples based on the expression given in (4), where the expressions are separated by equality sign with **factorial** and **powers** on each side. The powers are the same as of bases but with different permutations. Moreover, the digits follow the same order on both sides, with no rule on operations. The operation used are multiplication, addition, subtraction, and composition. Due to high quantity of numbers, the results are limited up to five terms for positive sign, and up to four terms for positive and negative signs. Results for five terms expressions with positive and negative signs are given in next work [12].

2.1 Positive Sign: Up to Four Terms Expressions

2.1.1 Up to Four Terms Expressions

Below are examples of numbers following the expression (4) with positive sign up to four terms.

$$1 := 1! = 1^1.$$

$$2 := 1! \times 2! = 1^2 \times 2^1.$$

$$3 := 1! + 2! = 1^2 + 2^1.$$

$$8 := 1! \times 2! + 3! = 1^3 + 2^2 + 3^1.$$

$$12 := 1! \times 2! \times 3! = 1^2 + 2^3 + 3^1.$$

$$= 1^3 \times 2^2 \times 3^1.$$

$$= 1^3 + 2^1 + 3^2.$$

$$13 := 1! + 2! \times 3! = 1^3 + 2^2 \times 3^1.$$

$$18 := (1! + 2!) \times 3! = 1^1 + 2^3 + 3^2.$$

$$= 1^3 \times 2^1 \times 3^2.$$

$$31 := 1! + 3! + 4! = 1^4 \times 3^3 + 4^1.$$

$$48 := 1! \times 2! \times 4! = (1^4 + 2^1) \times 4^2.$$

$$145 := 4! \times 3! + 1! = 4^3 + 3^4 \times 1^1.$$

$$36 := 1! \times 2! \times 3! + 4! = 1^3 + 2^4 + 3^1 + 4^2.$$

$$= 1^4 + 2^2 + 3^3 + 4^1.$$

$$56 := 2! \times (1! + 4!) + 3! = 2^3 \times 1^4 + 4^2 \times 3^1.$$

$$:= 3! + (1! + 4!) \times 2! = (3^2 + 1^3) \times 4^1 + 2^4.$$

$$60 := (1! \times 2!) \times (3! + 4!) = 1^1 + 2^4 + 3^3 + 4^2.$$

$$:= (1! \times 2!) \times (4! + 3!) = 1^4 + 2^1 \times 4^2 + 3^3.$$

$$61 := 1! + (4! + 3!) \times 2! = (1^3 + 4^1) \times 3^2 + 2^4.$$

$$90 := (1! + 2!) \times (3! + 4!) = 1^1 + 2^4 + 3^2 + 4^3.$$

$$= 1^3 + 2^2 + 3^4 + 4^1.$$

$$128 := (1! \times 2!) + 3! + 5! = 1^5 \times 2^2 \times (3^3 + 5^1).$$

$$129 := (1! + 2!) + 3! + 5! = 1^5 + 2^2 \times (3^3 + 5^1).$$

$$132 := (1! \times 2!) \times 3! + 5! = 1^5 \times 2^2 + 3^1 + 5^3.$$

$$:= (2! \times 3!) \times 1! + 5! = 2^5 + (3^1 + 1^3) \times 5^2.$$

$$133 := 1! + 2! \times 3! + 5! = 1^5 + 2^2 + 3^1 + 5^3.$$

$$138 := (1! + 2!) \times 3! + 5! = 1^5 + 2^2 \times 3^1 + 5^3.$$

$$146 := (1! \times 2!) + (3! \times 4!) = 1^4 \times 2^1 \times (3^2 + 4^3).$$

$$\begin{aligned} \mathbf{147} &:= (1! + 2!) + (3! \times 4!) = 1^2 \times 2^1 + 3^4 + 4^3. \\ &\quad = 1^4 + 2^1 \times (3^2 + 4^3). \\ &:= (1! + 2!) + (4! \times 3!) = 1^2 \times 2^1 + 4^3 + 3^4. \\ &\quad = (1^4 + 2^3) \times 4^2 + 3^1. \end{aligned}$$

$$\mathbf{150} := 1! \times 3! + 4! + 5! = 1^5 \times 3^4 + 4^3 + 5^1.$$

$$\mathbf{151} := 1! + 3! + 4! + 5! = 1^5 + 3^4 + 4^3 + 5^1.$$

$$\mathbf{152} := (1! + 4!) \times 3! + 2! = (1^4 \times 4^2 + 3^1) \times 2^3.$$

$$\mathbf{168} := 1! \times 5! + 2! \times 4! = (1^5 + 5^2 + 2^4) \times 4^1.$$

$$\begin{aligned} \mathbf{192} &:= (1! \times 2! + 3!) \times 4! = (1^4 + 2^3 + 3^1) \times 4^2. \\ &:= 5! + (1! + 2!) \times 4! = (5^1 + 1^5) \times (2^4 + 4^2). \end{aligned}$$

$$\mathbf{216} := (1! + 3! + 2!) \times 4! = 1^4 \times 3^3 \times (2^2 + 4^1).$$

$$\mathbf{246} := 1! \times 5! \times 2! + 3! = (1^3 + 5^1) \times (2^5 + 3^2).$$

$$\begin{aligned} \mathbf{252} &:= (1! \times 2!) \times (3! + 5!) = 1^3 \times 2^2 + 3^5 + 5^1. \\ &\quad = (1^5 + 2^3) \times (3^1 + 5^2). \end{aligned}$$

$$\mathbf{265} := 1! + 2! \times 5! + 4! = 1^5 \times 2^2 + 5^1 + 4^4.$$

$$\mathbf{266} := (1! + 5!) \times 2! + 4! = 1^5 + 5^1 + 2^2 + 4^4.$$

$$\begin{aligned} \mathbf{288} &:= 1! \times 2! \times 3! \times 4! = 1^1 + 2^2 + 3^3 + 4^4. \\ &\quad = 1^4 \times 2^3 \times 3^2 \times 4^1. \end{aligned}$$

$$\begin{aligned} \mathbf{289} &:= 1! + 2! \times 3! \times 4! = 1^4 + 2^3 \times 3^2 \times 4^1. \\ \mathbf{290} &:= (1! + 3! \times 4!) \times 2! = (1^2 \times 3^4 + 4^3) \times 2^1. \\ \mathbf{312} &:= (1! + 3! \times 2!) \times 4! = (1^2 + 3^3) \times 2^1 + 4^4. \\ \mathbf{336} &:= (1! + 3!) \times 2! \times 4! = (1^1 + 3^2) \times 2^3 + 4^4. \\ \mathbf{432} &:= (1! + 2!) \times 3! \times 4! = 1^4 \times 2^2 \times 3^3 \times 4^1. \end{aligned}$$

$$\begin{aligned} \mathbf{732} &:= (2! + 5!) \times 1! \times 3! = 2^5 + 5^2 \times (1^1 + 3^3). \\ \mathbf{738} &:= (2! + 1! + 5!) \times 3! = 2^1 \times (1^2 + 5^3 + 3^5). \\ \mathbf{744} &:= 1! \times 3! \times 5! + 4! = 1^4 + 3^5 + 5^3 \times 4^1. \\ \mathbf{854} &:= (3! + 1!) \times (2! + 5!) = 3^5 \times (1^2 + 2^1) + 5^3. \\ \mathbf{870} &:= (1! + 4!) \times 3! + 6! = (1^6 \times 4^3 + 3^4) \times 6^1. \end{aligned}$$

$$\begin{aligned} \mathbf{1440} &:= 1! \times 2! \times 3! \times 5! = 1^3 \times 2^5 \times 3^2 \times 5^1. \\ \mathbf{1441} &:= 1! + 2! \times 3! \times 5! = 1^3 + 2^5 \times 3^2 \times 5^1. \\ \mathbf{1728} &:= 2! \times 3! \times (5! + 4!) = 2^2 \times (3^5 + 5^3) + 4^4. \\ \mathbf{2520} &:= (1! + 2!) \times (5! + 6!) = (1^5 + 2^6 + 5^1) \times 6^2. \\ \mathbf{3146} &:= (1! + 5!) \times (2! + 4!) = 1^2 + 5^5 + 2^4 + 4^1. \\ \mathbf{3168} &:= (2! \times 3! + 5!) \times 4! = 2^4 \times (3^2 + 5^3) + 4^5. \\ \mathbf{5904} &:= (2! \times 5! + 3!) \times 4! = 2^4 \times (5^3 + 3^5) + 4^2. \end{aligned}$$

$$\mathbf{207360} := 2! \times 3! \times 4! \times 6! = 2^2 \times (3^4 \times 4^3 + 6^6).$$

2.1.2 Five Terms Expressions

Below are five terms positive sign examples according to the expression (4).

$$\begin{aligned} \mathbf{153} &:= 4! + 1! + 3! + 2! + 5! = 4^1 \times (1^5 + 3^3) + 2^4 + 5^2. \\ &\quad = 4^3 \times 1^5 + 3^2 + 2^4 \times 5^1. \\ &\quad = 4^3 + (1^5 + 3^1) \times 2^4 + 5^2. \end{aligned}$$

$$\mathbf{156} := 1! \times 2! \times 3! + 5! + 4! = 1^5 + 2^4 + 3^1 \times 5^2 + 4^3.$$

$$\begin{aligned} \mathbf{158} &:= 4! + 5! + (1! + 3!) \times 2! = 4^3 + (5^2 + 1^5) \times 3^1 + 2^4. \\ &:= 4! + 5! + 2! \times (1! + 3!) = 4^3 + 5^1 \times (2^4 + 1^5) + 3^2. \end{aligned}$$

$$\begin{aligned} \mathbf{174} &:= 2! \times 4! \times 1! + 5! + 3! = 2^3 + (4^2 + 1^5) \times 5^1 + 3^4. \\ &\quad = 2^5 + 4^3 + (1^4 + 5^2) \times 3^1. \end{aligned}$$

$$\begin{aligned}
 176 &:= 3! + (1! + 4!) \times 2! + 5! = 3^3 \times (1^5 + 4^1) + 2^4 + 5^2. \\
 &:= 3! + (4! + 1!) \times 2! + 5! = (3^1 + 4^2) \times 1^4 + 2^5 + 5^3. \\
 &\quad = 3^3 \times (4^1 + 1^5) + 2^4 + 5^2.
 \end{aligned}$$

$$180 := (1! \times 3! + 4!) \times 2! + 5! = 1^4 \times 3^3 + 4^1 \times 2^5 + 5^2.$$

$$\begin{aligned}
 181 &:= 1! + (3! + 4!) \times 2! + 5! = (1^5 + 3^2) \times 4^1 + 2^4 + 5^3. \\
 &\quad = 1^4 + 3^3 + 4^1 \times 2^5 + 5^2.
 \end{aligned}$$

$$182 := (1! + 3! + 4!) \times 2! + 5! = 1^2 \times 3^4 + 4^3 + 2^5 + 5^1.$$

$$\begin{aligned}
 198 &:= 3! + (2! + 1!) \times 4! + 5! = 3^2 + 2^4 \times 1^5 \times 4^1 + 5^3. \\
 &\quad = 3^4 + 2^5 + (1^3 + 4^2) \times 5^1.
 \end{aligned}$$

$$\begin{aligned}
 266 &:= 3! \times 1! \times 4! + 2! + 5! = 3^4 + (1^3 + 4^1) \times 2^5 + 5^2. \\
 &:= 3! \times 4! \times 1! + 2! + 5! = 3^2 + 4^1 \times (1^4 + 2^5) + 5^3. \\
 &:= 3! \times 4! + 2! \times 1! + 5! = 3^1 \times (4^3 + 2^4) + 1^5 + 5^2.
 \end{aligned}$$

$$\begin{aligned}
 270 &:= 3! \times 1! + 2! \times 5! + 4! = 3^4 + (1^5 + 2^3) \times (5^1 + 4^2). \\
 &:= 3! + 2! \times 5! \times 1! + 4! = (3^2 + 2^5) \times 5^1 + 1^4 + 4^3.
 \end{aligned}$$

$$\begin{aligned}
 272 &:= (1! + 4!) \times 3! + 2! + 5! = (1^5 \times 4^1) \times (3^3 + 2^4 + 5^2). \\
 &\quad = 1^4 \times 4^2 + 3^5 + 2^3 + 5^1. \\
 &:= 2! + (1! + 4!) \times 3! + 5! = (2^5 + 1^4 + 4^2) \times 3^1 + 5^3.
 \end{aligned}$$

$$\begin{aligned}
 276 &:= 2! \times 1! \times (3! + 5!) + 4! = 2^1 \times 1^5 \times (3^4 + 5^2) + 4^3. \\
 &:= 2! \times 1! \times (5! + 3!) + 4! = (2^4 + 1^5 + 5^2 + 3^3) \times 4^1. \\
 &:= 2! \times 1! \times (5! + 3!) + 4! = 2^1 \times 1^5 \times (5^2 + 3^4) + 4^3.
 \end{aligned}$$

$$277 := 1! + 2! \times (3! + 5!) + 4! = 1^5 + 2^1 \times (3^4 + 5^2) + 4^3.$$

$$\begin{aligned}
 278 &:= (1! + 3! + 5!) \times 2! + 4! = (1^5 + 3^4 + 5^2) \times 2^1 + 4^3. \\
 &\quad = 1^5 \times 3^2 + 5^1 + 2^3 + 4^4. \\
 &:= (1! + 5! + 3!) \times 2! + 4! = (1^5 + 5^2 + 3^4) \times 2^1 + 4^3.
 \end{aligned}$$

$$282 := 3! \times (2! + 1! + 4!) + 5! = 3^2 \times (2^4 + 1^5) + 4^1 + 5^3.$$

$$290 := (1! + 3!) \times 4! + 5! + 2! = 1^5 + 3^4 + 4^2 \times (5^1 + 2^3).$$

$$294 := 2! \times (4! \times 1! + 5!) + 3! = 2^5 \times (4^1 + 1^4) + 5^3 + 3^2.$$

$$295 := 1! + 3! + 2! \times (4! + 5!) = (1^5 \times 3^3 + 2^4 + 4^2) \times 5^1.$$

$$296 := (1! + 5! + 4!) \times 2! + 3! = 1^5 + 5^1 \times (4^2 + 2^4 + 3^3).$$

$$\begin{aligned} \mathbf{300} &:= 1! \times 2! \times (3! + 4! + 5!) = (1^5 + 2^4 + 3^3 + 4^2) \times 5^1. \\ &\quad = 1^4 + 2^5 + 3^1 \times (4^3 + 5^2). \end{aligned}$$

$$\begin{aligned} \mathbf{302} &:= (3! + 1! + 4! + 5!) \times 2! = 3^1 \times (1^4 + 4^3 + 5^2) + 2^5. \\ &\quad = 3^2 \times 1^3 + 4^4 + 5^1 + 2^5. \\ &\quad = 3^4 + (1^5 + 4^2) \times (5^1 + 2^3). \end{aligned}$$

$$\mathbf{312} := 1! \times 4! \times (2! + 3!) + 5! = 1^4 + 4^2 + (2^5 + 3^3) \times 5^1.$$

$$\begin{aligned} \mathbf{313} &:= 1! + (3! + 2!) \times 4! + 5! = (1^5 + 3^1) \times 2^3 + 4^4 + 5^2. \\ &\quad = 1^4 \times 3^1 \times (2^5 + 4^3) + 5^2. \\ &\quad = 1^5 \times 3^4 + 2^3 \times (4^1 + 5^2). \end{aligned}$$

$$\begin{aligned} \mathbf{320} &:= (1! + 4!) \times (2! + 3!) + 5! = 1^2 \times 4^4 + 2^5 + 3^3 + 5^1. \\ &\quad := (1! + 4!) \times (3! + 2!) + 5! = (1^4 + 4^1) \times (3^3 + 2^5) + 5^2. \\ &\quad \quad = 1^5 + (4^2 + 3^4) \times 2^1 + 5^3. \end{aligned}$$

$$\begin{aligned} \mathbf{336} &:= (3! + 2! + 1!) \times 4! + 5! = 3^3 \times 2^1 + 1^5 + 4^4 + 5^2. \\ &\quad = 3^5 + (2^4 + 1^3) \times 4^1 + 5^2. \\ &\quad = 3^5 + 2^3 + (1^4 + 4^2) \times 5^1. \end{aligned}$$

$$\begin{aligned} \mathbf{384} &:= 3! \times 1! \times 4! + 2! \times 5! = 3^1 \times 1^5 + 4^2 \times 2^4 + 5^3. \\ &\quad = 3^3 + (1^5 + 4^2) \times (2^4 + 5^1). \\ &\quad = 3^5 \times 1^4 + 4^1 \times 2^2 + 5^3. \\ &\quad = 3^5 + (1^4 + 4^2) \times 2^3 + 5^1. \end{aligned}$$

$$\begin{aligned} \mathbf{385} &:= 1! + 3! \times 4! + 2! \times 5! = (1^3 + 3^4) \times 4^1 + 2^5 + 5^2. \\ &\quad = 1^4 + 3^5 + 4^1 \times 2^2 + 5^3. \\ &\quad = 1^5 + 3^1 + 4^2 \times 2^4 + 5^3. \end{aligned}$$

$$\begin{aligned} \mathbf{386} &:= 2! \times (5! + 1!) + 3! \times 4! = (2^1 + 5^3) \times 1^4 + 3^5 + 4^2. \\ &\quad = (2^3 + 5^1) \times (1^5 + 3^2) + 4^4. \\ &\quad = 2^4 + 5^1 \times (1^5 + 3^2 + 4^3). \end{aligned}$$

$$\mathbf{402} := (3! + 5!) \times (2! + 1!) + 4! = 3^5 + 5^3 + 2^1 \times (1^4 + 4^2).$$

$$\begin{aligned} \mathbf{408} &:= 4! \times 2! \times 1! \times 3! + 5! = 4^2 + 2^4 + 1^5 + 3^1 \times 5^3. \\ &\quad = 4^3 + 2^2 \times 1^5 \times (3^4 + 5^1). \\ &\quad = 4^4 + (2^1 + 1^5) \times 3^2 + 5^3. \end{aligned}$$

$$\begin{aligned}
 409 &:= 1! + 3! \times 2! \times 4! + 5! = (1^3 + 3^1) \times 2^5 + 4^4 + 5^2. \\
 &= (1^4 + 3^1) \times (2^5 + 4^3) + 5^2. \\
 &= 1^5 \times 3^2 + (2^4 + 4^3) \times 5^1.
 \end{aligned}$$

$$\begin{aligned}
 410 &:= (1! + 3! \times 4!) \times 2! + 5! = 1^5 + 3^2 + (4^3 + 2^4) \times 5^1. \\
 &:= 2! \times (3! \times 4! + 1!) + 5! = 2^2 + 3^4 + (4^3 + 1^5) \times 5^1. \\
 &:= 2! \times (4! \times 3! + 1!) + 5! = 2^4 + 4^2 + 3^1 \times (1^5 + 5^3).
 \end{aligned}$$

$$\begin{aligned}
 414 &:= 3! \times (2! \times 4! + 1!) + 5! = 3^2 + (2^4 + 4^3 + 1^5) \times 5^1. \\
 420 &:= (1! + 4!) \times 2! \times 3! + 5! = (1^4 + 4^1) \times (2^5 + 3^3 + 5^2).
 \end{aligned}$$

$$\begin{aligned}
 432 &:= (3! \times 2! + 1!) \times 4! + 5! = 3^5 + (2^3 + 1^4) \times (4^2 + 5^1). \\
 &= 3^5 + 2^4 \times 1^2 \times 4^1 + 5^3.
 \end{aligned}$$

$$438 := 3! + (2! + 1!) \times (4! + 5!) = 3^4 + 2^5 + (1^2 + 4^3) \times 5^1.$$

$$\begin{aligned}
 450 &:= (1! + 2!) \times (4! + 3! + 5!) = (1^5 + 2^4 + 4^3 + 3^2) \times 5^1. \\
 &= 1^4 + (2^5 + 4^1) \times 3^2 + 5^3.
 \end{aligned}$$

$$\begin{aligned}
 456 &:= 4! \times (3! + 1!) \times 2! + 5! = 4^1 \times (3^4 \times 1^5 + 2^3 + 5^2). \\
 &= 4^1 + 3^3 + (1^5 + 2^4) \times 5^2.
 \end{aligned}$$

$$\begin{aligned}
 504 &:= 3! \times 4! + 5! \times (1! + 2!) = 3^4 + (4^2 + 5^3) \times (1^5 + 2^1). \\
 &= 3^5 + (4^1 + 5^2) \times (1^4 + 2^3). \\
 &:= 5! \times (1! + 2!) + 4! \times 3! = 5^1 \times 1^3 + 2^4 \times 4^2 + 3^5. \\
 &= 5^1 \times 1^4 + 2^2 \times 4^3 + 3^5.
 \end{aligned}$$

$$\begin{aligned}
 528 &:= (4! \times 3! \times 1! + 5!) \times 2! = 4^1 \times (3^4 + 1^5) + 5^2 \times 2^3. \\
 &= 4^2 \times 3^3 + (1^5 + 5^1) \times 2^4. \\
 &= 4^3 + (3^1 + 1^5 + 5^2) \times 2^4.
 \end{aligned}$$

$$529 := 1! + (5! + 3! \times 4!) \times 2! = 1^5 + (5^1 + 3^3) \times 4^2 + 2^4.$$

$$\begin{aligned}
 530 &:= 2! \times (1! + 3! \times 4! + 5!) = (2^3 + 1^5 + 3^4 + 4^2) \times 5^1. \\
 &= (2^5 + 1^4 + 3^2 + 4^3) \times 5^1.
 \end{aligned}$$

$$540 := ((1! + 4!) \times 3! + 5!) \times 2! = 1^2 + 4^4 + 3^5 + 5^1 \times 2^3.$$

$$\begin{aligned} 552 &:= (1! + 2!) \times 4! \times 3! + 5! = (1^5 + 2^4) \times (4^1 + 3^3) + 5^2. \\ &\quad = 1^5 \times 2^4 + 4^1 \times (3^2 + 5^3). \end{aligned}$$

$$576 := 2! \times (4! \times (1! + 3!) + 5!) = 2^5 \times (4^2 + 1^4) + 3^3 + 5^1.$$

$$746 := 1! \times 5! \times 3! + 2! + 4! = 1^5 + 5^1 \times (3^4 + 2^2 + 4^3).$$

$$747 := 1! + 2! + 3! \times 5! + 4! = 1^4 \times 2^2 + 3^5 + 5^3 \times 4^1.$$

$$752 := 1! \times 3! + 2! + 4! + 6! = (1^6 + 3^4) \times 2^3 + 4^2 \times 6^1.$$

$$756 := 3! \times 1! \times (2! + 5!) + 4! = (3^4 + 1^5) \times 2^3 + 5^2 \times 4^1.$$

$$\begin{aligned} &:= 3! \times 1! \times (5! + 2!) + 4! = (3^1 + 1^5) \times 5^3 + 2^4 \times 4^2. \\ &\quad = 3^1 \times 1^5 + 5^4 + 2^3 \times 4^2. \end{aligned}$$

$$757 := 1! + (2! + 5!) \times 3! + 4! = 1^2 \times 2^5 + 5^1 \times (3^4 + 4^3).$$

$$762 := 4! + (1! + 2! + 5!) \times 3! = 4^1 \times 1^3 \times 2^5 + 5^4 + 3^2.$$

$$= 4^3 \times 1^5 \times 2^1 + 5^4 + 3^2.$$

$$:= 4! + 3! \times (1! + 5! + 2!) = (4^3 + 3^4 + 1^2) \times 5^1 + 2^5.$$

$$768 := 1! \times 4! \times 2! + 3! \times 5! = 1^3 + 4^4 + 2^1 \times 3^5 + 5^2.$$

$$= 1^5 \times 4^2 \times (2^4 + 3^3 + 5^1).$$

$$= 1^5 \times 4^4 + 2^2 \times (3^1 + 5^3).$$

$$769 := 1! + 2! \times 4! + 3! \times 5! = (1^3 \times 2^5 + 4^2) \times 3^1 + 5^4.$$

$$= 1^4 + 2^1 \times (4^2 + 3^5 + 5^3).$$

$$= 1^5 + 2^4 \times (4^2 + 3^3 + 5^1).$$

$$770 := 5! \times 3! + (4! + 1!) \times 2! = (5^3 + 3^5 + 4^2 + 1^4) \times 2^1.$$

$$:= 5! \times 3! + 2! \times (4! + 1!) = 5^4 + 3^1 \times (2^5 + 4^2) + 1^3.$$

$$774 := (1! \times 2!) \times 4! + 6! + 3! = (1^6 \times 2^4 + 4^3 + 6^1) \times 3^2.$$

$$:= (1! + 5!) \times 3! + 2! \times 4! = (1^3 + 5^1) \times (3^4 + 2^5 + 4^2).$$

$$= 1^5 + 5^3 + 3^4 \times (2^2 + 4^1).$$

$$775 := 1! + 2! \times 4! + 6! + 3! = 1^6 + (2^4 + 4^3 + 6^1) \times 3^2.$$

$$782 := (1! + 3! + 4!) \times 2! + 6! = (1^6 \times 3^4 + 4^2) \times 2^3 + 6^1.$$

$$\begin{aligned} 792 &:= (1! + 2!) \times (5! + 3! \times 4!) = 1^3 \times 2^1 \times (5^2 + 3^5) + 4^4. \\ &\quad = 1^5 + 2^4 + 5^2 \times (3^3 + 4^1). \end{aligned}$$

$$\mathbf{798} := (1! + 2!) \times 4! + 3! + 6! = 1^4 + 2^3 \times 4^1 + 3^6 + 6^2.$$

$$\mathbf{858} := (1! + 2!) \times 3! + 6! + 5! = 1^6 + 2^5 + (3^3 + 6^1) \times 5^2.$$

$$\mathbf{866} := 1! \times 3! \times 4! + 2! + 6! = 1^4 + 3^6 + 4^3 + 2^1 \times 6^2.$$

$$:= 2! + (5! + 4! \times 1!) \times 3! = (2^5 + 5^3) \times (4^1 + 1^2) + 3^4.$$

$$\mathbf{867} := 1! + 2! + (5! + 4!) \times 3! = (1^5 \times 2^3 + 5^2 + 4^4) \times 3^1.$$

$$= 1^4 \times 2^5 \times 5^2 + 4^3 + 3^1.$$

$$:= 1! + 6! + 2! + 3! \times 4! = (1^4 + 6^2) \times 2^1 + 3^6 + 4^3.$$

$$\mathbf{872} := (1! + 4! + 5!) \times 3! + 2! = (1^4 + 4^1) \times 5^3 + 3^5 + 2^2.$$

$$:= 2! + (4! + 1!) \times 3! + 6! = (2^2 + 4^1) \times (1^6 + 3^4) + 6^3.$$

$$\mathbf{876} := (1! \times 2! + 4! + 5!) \times 3! = 1^3 \times 2^2 + 4^1 + 5^4 + 3^5.$$

$$= 1^3 + 2^5 + (4^4 + 5^2) \times 3^1.$$

$$\mathbf{877} := 1! + (2! + 4! + 5!) \times 3! = 1^3 + 2^2 + 4^1 + 5^4 + 3^5.$$

$$\mathbf{878} := 4! + (3! + 1!) \times (2! + 5!) = (4^2 + 3^4) \times (1^5 + 2^3) + 5^1.$$

$$\mathbf{882} := (1! + 4! + 2! + 5!) \times 3! = (1^2 + 4^4) \times 2^1 + 5^3 + 3^5.$$

$$= 1^5 + 4^1 \times 2^3 \times 5^2 + 3^4.$$

$$:= 3! \times (1! + 2! + 4!) + 6! = 3^6 + 1^4 + 2^3 + 4^1 \times 6^2.$$

$$\mathbf{888} := 2! \times 4! + (1! + 3!) \times 5! = 2^2 \times (4^1 + 1^3) + 3^5 + 5^4.$$

$$= 2^2 \times (4^3 + 1^5) + 3^1 + 5^4.$$

$$= 2^3 \times (4^1 + 1^5 + 3^4 + 5^2).$$

$$= 2^5 \times 4^2 + 1^4 + 3^1 \times 5^3.$$

$$\mathbf{890} := (1! + 3!) \times 4! + 6! + 2! = 1^2 + 3^6 + 4^3 + 6^1 \times 2^4.$$

$$= 1^3 + 3^6 + 4^1 \times 6^2 + 2^4.$$

$$= 1^6 + 3^2 + 4^1 \times 6^3 + 2^4.$$

$$\mathbf{902} := (1! + 3!) \times (2! + 4!) + 6! = (1^3 + 3^2) \times 2^6 + 4^4 + 6^1.$$

$$= (1^6 + 3^3) \times (2^4 + 4^2) + 6^1.$$

$$\mathbf{913} := 1! + 6! + 4! \times (2! + 3!) = (1^4 + 6^1 + 4^2) \times 2^3 + 3^6.$$

$$\mathbf{920} := (1! + 4!) \times (2! + 3!) + 6! = (1^6 + 4^2) \times 2^4 + 3^1 \times 6^3.$$

$$\mathbf{936} := (2! + 3! + 1!) \times 4! + 6! = 2^4 \times 3^2 \times (1^6 + 4^1) + 6^3.$$

$$\begin{aligned} \mathbf{966} &:= 1! \times 2! \times 5! + 3! + 6! = 1^5 + 2^2 \times 5^1 + 3^6 + 6^3. \\ &:= 1! \times 2! \times 5! + 6! + 3! = (1^6 + 2^1) \times (5^2 + 6^3) + 3^5. \end{aligned}$$

$$\mathbf{972} := 1! \times 2! \times (3! + 5!) + 6! = 1^5 \times 2^1 + 3^6 + 5^2 + 6^3.$$

$$\mathbf{973} := 1! + 2! \times (3! + 5!) + 6! = 1^5 + 2^1 + 3^6 + 5^2 + 6^3.$$

$$\mathbf{984} := (3! \times 1! + 2!) \times 5! + 4! = 3^3 + (1^4 + 2^5) \times (5^2 + 4^1).$$

$$\begin{aligned} \mathbf{985} &:= 1! + 4! + (3! + 2!) \times 5! = (1^5 + 4^1) \times 3^2 \times 2^3 + 5^4. \\ &= 1^5 \times 4^4 + 3^3 \times (2^1 + 5^2). \end{aligned}$$

$$\begin{aligned} \mathbf{992} &:= (2! + 3!) \times (1! + 5!) + 4! = 2^1 \times (3^5 \times 1^2 + 5^3) + 4^4. \\ &= 2^5 \times (3^1 + 1^4 + 5^2) + 4^3. \\ &= 2^5 + (3^2 + 1^4 + 5^1) \times 4^3. \end{aligned}$$

$$\begin{aligned} \mathbf{1008} &:= 1! \times 3! \times 2! \times 4! + 6! = 1^6 \times 3^2 \times 2^4 + 4^1 \times 6^3. \\ &= 1^6 \times 3^4 \times (2^3 + 4^1) + 6^2. \\ &:= 3! \times (2! \times 4! \times 1! + 5!) = (3^3 + 2^5) \times (4^2 + 1^4) + 5^1. \end{aligned}$$

$$\begin{aligned} \mathbf{1009} &:= 1! + 3! \times (2! \times 4! + 5!) = (1^1 + 3^2) \times 2^5 + 4^3 + 5^4. \\ &= (1^2 + 3^1) \times (2^5 + 4^3) + 5^4. \\ &= (1^5 + 3^4) \times (2^3 + 4^1) + 5^2. \\ &= 1^3 \times 3^4 + 2^5 \times (4^1 + 5^2). \\ &= 1^5 \times 3^1 \times 2^3 \times 4^2 + 5^4. \\ &:= 1! + 3! \times 2! \times 4! + 6! = 1^2 \times 3^4 + 2^6 + 4^1 \times 6^3. \\ &= 1^2 \times 3^6 + 2^4 \times 4^1 + 6^3. \\ &= 1^4 \times 3^6 + 2^2 \times (4^3 + 6^1). \\ &= 1^6 + 3^2 \times 2^4 + 4^1 \times 6^3. \\ &= 1^6 + 3^4 \times (2^3 + 4^1) + 6^2. \end{aligned}$$

$$\begin{aligned} \mathbf{1010} &:= (1! + 3!) \times (4! + 5!) + 2! = (1^4 + 3^2) \times (4^3 + 5^1 + 2^5). \\ &= 1^3 + 3^4 + (4^1 + 5^2) \times 2^5. \\ &:= (1! + 3! \times 4!) \times 2! + 6! = 1^2 + 3^6 + 4^1 \times 2^4 + 6^3. \\ &= 1^3 + 3^6 + 4^4 + 2^2 \times 6^1. \end{aligned}$$

$$\mathbf{1020} := 2! \times (4! + 1!) \times 3! + 6! = (2^3 + 4^1) \times (1^6 + 3^4) + 6^2.$$

$$\begin{aligned} \mathbf{1032} &:= (2! \times 3! + 1!) \times 4! + 6! = 2^4 \times 3^1 \times (1^6 + 4^2) + 6^3. \\ &:= (2! + 3!) \times 4! + 5! + 6! = 2^6 + 3^5 + 4^3 + 5^4 + 6^2. \end{aligned}$$

$$\begin{aligned} \mathbf{1056} &:= (1! + 3!) \times 4! \times 2! + 6! = 1^6 \times 3^1 \times 4^4 + 2^3 \times 6^2. \\ \mathbf{1086} &:= 3! + 5! \times (1! + 2!) + 6! = 3^3 \times (5^2 + 1^5) + 2^6 \times 6^1. \end{aligned}$$

$$\begin{aligned} \mathbf{1104} &:= (1! + 2! + 3!) \times 5! + 4! = (1^4 \times 2^3 + 3^5 + 5^2) \times 4^1. \\ &\quad = (1^5 + 2^4 + 3^3) \times 5^2 + 4^1. \\ &\quad = 1^4 + 2^1 \times 3^3 + 5^2 + 4^5. \end{aligned}$$

$$\begin{aligned} \mathbf{1152} &:= (4! + 5!) \times (3! \times 1! + 2!) = (4^2 + 5^3 + 3^5) \times (1^4 + 2^1). \\ &\quad = (4^4 + 5^1 + 3^3) \times 1^5 \times 2^2. \\ &\quad = 4^4 + (5^2 + 3^1) \times 1^3 \times 2^5. \\ &\quad = 4^4 + 5^1 + 3^3 \times (1^2 + 2^5). \\ &\quad = 4^5 + (5^1 + 3^3) \times 1^4 \times 2^2. \end{aligned}$$

$$\begin{aligned} \mathbf{1152} &:= 3! \times (5! + (1! + 2!) \times 4!) = (3^1 + 5^2) \times 1^3 \times 2^5 + 4^4. \\ &\quad = (3^1 + 5^3) \times 1^5 + 2^2 \times 4^4. \\ &\quad = (3^3 + 5^1) \times 1^4 \times 2^2 + 4^5. \end{aligned}$$

$$\begin{aligned} \mathbf{1153} &:= 1! + (2! + 3!) \times (5! + 4!) = 1^3 + 2^5 \times (3^1 + 5^2) + 4^4. \\ &\quad = 1^4 + 2^2 \times (3^3 + 5^1) + 4^5. \\ &\quad = 1^5 + 2^2 \times (3^3 + 5^1 + 4^4). \end{aligned}$$

$$\mathbf{1160} := (1! + 4! + 5!) \times (2! + 3!) = 1^4 \times 4^5 + 5^3 + 2^1 + 3^2.$$

$$\begin{aligned} \mathbf{1176} &:= (1! + 3!) \times (2! \times 4! + 5!) = 1^2 + 3^5 \times 2^1 + 4^3 + 5^4. \\ &\quad = 1^5 + (3^3 + 2^4 + 4^1) \times 5^2. \\ &:= (1! + 3!) \times (4! \times 2! + 5!) = (1^4 + 3^5) \times 4^1 + 2^3 \times 5^2. \end{aligned}$$

$$\begin{aligned} \mathbf{1296} &:= (2! + 1! + 3!) \times (5! + 4!) = 2^2 \times (1^4 + 3^5) + 5^1 \times 4^3. \\ &\quad = 2^3 \times (1^5 + 3^4 + 5^1 \times 4^2). \\ &\quad = 2^4 + 1^2 + 3^5 \times 5^1 + 4^3. \end{aligned}$$

$$\begin{aligned} \mathbf{1442} &:= 1! \times 3! \times 5! + 2! + 6! = (1^6 + 3^2) \times 5^3 + 2^5 \times 6^1. \\ \mathbf{1443} &:= 1! + 3! \times 5! + 2! + 6! = 1^6 \times 3^5 + 5^2 \times 2^3 \times 6^1. \\ \mathbf{1448} &:= 2! + (1! + 5!) \times 3! + 6! = 2^5 \times 1^6 \times 5^2 + 3^1 \times 6^3. \end{aligned}$$

$$\begin{aligned} \mathbf{1452} &:= (1! \times 2! + 5!) \times 3! + 6! = (1^6 + 2^1) \times (5^2 + 3^5 + 6^3). \\ &\quad := 3! \times (2! + 5!) \times 1! + 6! = (3^5 + 2^2) \times 5^1 + 1^6 + 6^3. \\ &\quad := 3! \times 1! \times (2! + 5!) + 6! = 3^6 + (1^5 + 2^1) \times (5^2 + 6^3). \end{aligned}$$

$$\mathbf{1470} := (1! + 5! \times 2!) \times 3! + 4! = 1^2 + 5^1 \times (2^3 + 3^4) + 4^5.$$

$$\begin{aligned}\mathbf{1472} &:= (1! + 6!) \times 2! + 3! + 4! = 1^6 \times 6^4 + (2^3 + 3^1) \times 4^2. \\ &:= 2! \times (6! + 1!) + 3! + 4! = 2^6 + (6^1 + 1^3 + 3^4) \times 4^2. \\ &= 2^6 + 6^4 + (1^2 + 3^3) \times 4^1.\end{aligned}$$

$$\begin{aligned}\mathbf{1476} &:= 1! \times 2! \times (3! + 6!) + 4! = ((1^6 + 2^4) \times 3^2 + 6^3) \times 4^1. \\ &:= 1! \times 2! \times (6! + 3!) + 4! = (1^6 \times 2^3 \times 6^2 + 3^4) \times 4^1. \\ &:= 3! \times (1! + 5!) \times 2! + 4! = (3^5 \times 1^4 + 5^3) \times 2^2 + 4^1. \\ &= (3^5 + 1^3) \times 5^1 + 2^4 \times 4^2. \\ &= (3^5 + 1^4) \times 5^1 + 2^2 \times 4^3. \\ &:= 3! \times (5! + 1!) \times 2! + 4! = 3^3 + 5^2 \times (1^1 + 2^4) + 4^5. \\ &= 3^5 \times 5^1 + 1^3 + 2^2 + 4^4.\end{aligned}$$

$$\begin{aligned}\mathbf{1477} &:= 1! + 2! \times (6! + 3!) + 4! = 1^6 + (2^3 \times 6^2 + 3^4) \times 4^1. \\ \mathbf{1478} &:= 4! + 2! \times (1! + 3! + 6!) = 4^2 \times (2^6 + 1^4 + 3^3) + 6^1.\end{aligned}$$

$$\begin{aligned}\mathbf{1488} &:= (4! + 3! \times 5! \times 1!) \times 2! = (4^1 + 3^5 + 5^3) \times 1^4 \times 2^2. \\ &= (4^3 + 3^1 + 5^2 + 1^5) \times 2^4. \\ &= 4^1 \times (3^5 + 5^3) \times 1^2 + 2^4. \\ &= 4^2 \times 3^4 + (5^1 + 1^3) \times 2^5. \\ &= 4^5 + (3^1 + 5^2 + 1^3) \times 2^4.\end{aligned}$$

$$\begin{aligned}\mathbf{1489} &:= 1! + 2! \times (4! + 3! \times 5!) = (1^1 \times 2^5 + 4^3) \times 3^2 + 5^4. \\ &= 1^2 + 2^4 + 4^1 \times (3^5 + 5^3). \\ &= 1^5 \times 2^1 \times 4^2 \times 3^3 + 5^4.\end{aligned}$$

$$\begin{aligned}\mathbf{1490} &:= (1! + 5! \times 3! + 4!) \times 2! = (1^3 + 5^1) \times 3^5 + 4^2 + 2^4. \\ &= 1^1 + 5^4 + 3^2 \times (4^3 + 2^5). \\ &= 1^5 + 5^4 + 3^3 \times 4^2 \times 2^1.\end{aligned}$$

$$\mathbf{1494} := 1! \times 2! \times (6! + 4!) + 3! = ((1^6 + 2^4) \times 6^1 + 4^3) \times 3^2.$$

$$\begin{aligned}\mathbf{1495} &:= 2! \times (6! + 4!) + 1! + 3! = 2^2 + 6^4 + (4^3 + 1^6) \times 3^1. \\ &= 2^6 + 6^4 + (4^1 + 1^2) \times 3^3.\end{aligned}$$

$$\begin{aligned}\mathbf{1500} &:= 1! \times 2! \times (4! + 3! + 6!) = (1^6 \times 2^2 + 4^3) \times 3^1 + 6^4. \\ &:= 2! \times ((1! + 5!) \times 3! + 4!) = (2^4 + 1^3) \times (5^2 + 3^1) + 4^5.\end{aligned}$$

$$\mathbf{1501} := 1! + 2! \times (4! + 3! + 6!) = 1^6 + (2^2 + 4^3) \times 3^1 + 6^4.$$

$$\mathbf{1566} := 1! \times 6! \times 2! + 5! + 3! = (1^2 + 6^1) \times (2^6 + 5^3) + 3^5.$$

$$\mathbf{1567} := 1! + 5! + 2! \times 6! + 3! = (1^3 + 5^2) \times 2^5 + 6^1 + 3^6.$$

$$\begin{aligned}\mathbf{1572} := 1! \times 5! + 2! \times (3! + 6!) &= (1^6 + 5^2 + 2^5) \times 3^3 + 6^1. \\ &= 1^3 + 5^1 \times (2^6 + 3^5) + 6^2.\end{aligned}$$

$$\begin{aligned}\mathbf{1584} := 1! \times 6! \times 2! + 4! \times 3! &= ((1^6 + 6^1) \times 2^4 + 4^3) \times 3^2. \\ &= 1^6 \times 6^4 + 2^3 \times 4^1 \times 3^2. \\ &:= 1! \times 6! + (5! + 4!) \times 3! = (1^6 + 6^3) \times 5^1 + 4^4 + 3^5. \\ &:= 4! + (2! \times 3! + 1!) \times 5! = (4^2 + 2^1) \times 3^4 + 1^5 + 5^3. \\ &= (4^2 + 2^5) \times (3^3 + 1^4 + 5^1). \\ &= 4^5 + 2^2 \times (3^3 + 1^4) \times 5^1.\end{aligned}$$

$$\begin{aligned}\mathbf{1585} := 1! + 3! \times (4! + 2! \times 5!) &= (1^1 + 3^2) \times (4^3 + 2^5) + 5^4. \\ &:= 1! + 3! \times 4! + 2! \times 6! = 1^6 + (3^2 \times 4^1) \times 2^3 + 6^4.\end{aligned}$$

$$\mathbf{1596} := 3! \times (2! \times (1! + 5!) + 4!) = 3^5 \times (2^2 + 1^1) + 5^3 + 4^4.$$

$$\mathbf{1608} := (1! + 3!) \times 4! + 2! \times 6! = 1^2 \times 3^1 \times (4^4 + 2^6 + 6^3).$$

$$\begin{aligned}\mathbf{1688} := (2! + 3!) \times (5! + 1!) + 6! &= 2^5 \times (3^2 \times 5^1 + 1^6) + 6^3. \\ &:= 2! \times (6! + 1! + 5!) + 3! = (2^3 \times 6^2 + 1^6) \times 5^1 + 3^5.\end{aligned}$$

$$\begin{aligned}\mathbf{1704} := (1! + 3!) \times 2! \times 5! + 4! &= (1^5 + 3^4) \times 2^2 \times 5^1 + 4^3. \\ &= 1^2 + 3^3 \times 2^1 + 5^4 + 4^5.\end{aligned}$$

$$\begin{aligned}\mathbf{1728} := 2! \times (3! \times 4! \times 1! + 6!) &= (2^2 \times 3^3) \times 4^1 \times 1^6 + 6^4. \\ &= (2^2 + 3^3 + 4^4 + 1^6) \times 6^1. \\ &= (2^4 + 3^3 + 4^1 + 1^6) \times 6^2. \\ &:= 2! \times (6! \times 1! + 3! \times 4!) = 2^1 \times 6^3 \times 1^6 + 3^4 \times 4^2. \\ &:= 2! \times 3! \times 1! \times (5! + 4!) = 2^1 + 3^3 \times (1^4 + 5^2) + 4^5. \\ &= 2^2 \times (3^5 \times 1^1 + 5^3) + 4^4. \\ &= 2^4 \times (3^3 + 1^5 + 5^1 \times 4^2). \\ &= 2^5 \times (3^1 + 1^4) + 5^2 \times 4^3.\end{aligned}$$

$$\mathbf{1729} := 1! + (4! \times 3! + 6!) \times 2! = 1^6 + 4^2 \times 3^4 + 6^3 \times 2^1.$$

$$:= 1! + (6! + 3! \times 4!) \times 2! = 1^6 + 6^4 + 3^3 \times 4^1 \times 2^2.$$

$$:= 1! + 2! \times 3! \times (5! + 4!) = 1^1 + 2^2 \times (3^5 + 5^3) + 4^4.$$

$$:= 1! + 3! \times 2! \times (4! + 5!) = (1^1 + 3^2) \times 2^3 + 4^5 + 5^4.$$

$$\begin{aligned}
 \mathbf{1730} &:= (3! \times 4! + 1! + 6!) \times 2! = 3^3 \times 4^2 \times 1^6 + 6^4 + 2^1. \\
 &\quad = 3^4 \times 4^2 + (1^6 + 6^3) \times 2^1. \\
 &:= 2! \times (1! + 3! \times (4! + 5!)) = (2^1 + 1^2) \times 3^3 + 4^5 + 5^4. \\
 &\quad = (2^3 + 1^1) \times 3^2 + 4^5 + 5^4. \\
 &= 2^3 + (1^5 + 3^4) \times (4^2 + 5^1).
 \end{aligned}$$

$$\mathbf{1734} := (1! + 2! \times (4! + 5!)) \times 3! = 1^3 + 2^5 + (4^2 + 5^1) \times 3^4.$$

$$\begin{aligned}
 \mathbf{1740} &:= 2! \times ((1! + 4!) \times 3! + 6!) = (2^1 + 1^6) \times 4^4 + 3^3 \times 6^2. \\
 &:= 2! \times 3! \times (1! + 5! + 4!) = (2^5 + 3^3 + 1^4) \times (5^2 + 4^1). \\
 &= 2^4 + (3^3 + 1^1) \times 5^2 + 4^5.
 \end{aligned}$$

$$\mathbf{1776} := 2! \times ((1! + 3!) \times 4! + 6!) = (2^1 + 1^6 + 3^3) \times 4^2 + 6^4.$$

$$\mathbf{1848} := (1! + 3!) \times (5! \times 2! + 4!) = (1^1 \times 3^4 + 5^3) \times 2^2 + 4^5.$$

$$\begin{aligned}
 \mathbf{1872} &:= (1! + 2! \times 3!) \times (5! + 4!) = (1^2 + 2^1) \times (3^5 + 5^3 + 4^4). \\
 &= 1^1 \times 2^3 \times (3^4 + 5^2) + 4^5.
 \end{aligned}$$

$$\begin{aligned}
 \mathbf{2016} &:= (1! + 3!) \times (4! + 5!) \times 2! = (1^3 \times 3^5 + 4^4 + 5^1) \times 2^2. \\
 &= 1^4 \times 3^2 \times (4^3 + 5^1 \times 2^5).
 \end{aligned}$$

$$\mathbf{2160} := 2! \times 3! \times 1! \times 5! + 6! = 2^3 \times 3^5 + (1^6 + 5^1) \times 6^2.$$

$$\begin{aligned}
 \mathbf{2184} &:= (2! + 1!) \times 3! \times 5! + 4! = 2^3 \times (1^4 + 3^5 + 5^2 + 4^1). \\
 &:= 3! \times 5! \times (2! + 1!) + 4! = 3^2 + 5^3 + 2^1 \times (1^4 + 4^5). \\
 &:= 5! \times (1! + 2!) \times 3! + 4! = (5^1 + 1^5) \times (2^2 \times 3^3 + 4^4).
 \end{aligned}$$

$$\mathbf{2190} := 4! + 3! + (2! + 1!) \times 6! = (4^4 + 3^3 \times 2^2 + 1^6) \times 6^1.$$

$$\begin{aligned}
 \mathbf{2202} &:= (2! + 1!) \times (3! + 6!) + 4! = 2^1 \times (1^6 + 3^3 \times 6^2) + 4^4. \\
 &= 2^1 \times 1^6 + 3^2 \times 6^3 + 4^4.
 \end{aligned}$$

$$\begin{aligned}
 \mathbf{2280} &:= (1! + 3!) \times 5! + 6! \times 2! = (1^6 + 3^5 + 5^1 + 6^2) \times 2^3. \\
 &:= (1! + 2!) \times 6! + 5! + 3! = (1^6 + 2^5 + 6^3 + 5^1) \times 3^2.
 \end{aligned}$$

$$\begin{aligned}
 \mathbf{2304} &:= ((2! + 1!) \times 5! + 4!) \times 3! = (2^5 \times (1^4 + 5^1) + 4^3) \times 3^2. \\
 &= 2^4 \times 1^5 \times (5^3 + 4^2 + 3^1). \\
 &:= (1! + 2!) \times 6! + 3! \times 4! = 1^6 \times 2^4 \times (6^2 + 3^3 \times 4^1). \\
 &:= (1! + 2!) \times 6! + 4! \times 3! = 1^6 \times 2^4 \times (6^2 + 4^1 \times 3^3). \\
 &:= (2! + 1!) \times 6! + 5! + 4! = 2^6 \times (1^5 + 6^1 + 5^2) + 4^4. \\
 &:= (4! + (1! + 2!) \times 5!) \times 3! = (4^4 + 1^2) \times 2^3 + 5^1 + 3^5.
 \end{aligned}$$

$$\mathbf{2538} := (1! + 2!) \times (3! + 6! + 5!) = 1^5 + (2^6 + 3^1) \times 6^2 + 5^3.$$

$$\begin{aligned}\mathbf{2592} &:= (1! + 2!) \times (3! \times 4! + 6!) = (1^6 + 2^1) \times 3^3 \times 4^2 + 6^4. \\ &:= (2! + 1!) \times (5! + 4!) \times 3! = ((2^5 \times 1^4) \times 5^2 + 4^3) \times 3^1. \\ &= (2^3 + 1^2) \times (5^1 + 4^4) + 3^5. \\ &= (2^4 \times 1^5 \times 5^1 + 4^2) \times 3^3. \\ &= 2^3 \times (1^4 + 5^1 \times 4^2 + 3^5). \\ &= 2^4 \times (1^5 + 5^3 + 4^1 \times 3^2).\end{aligned}$$

$$\mathbf{2889} := (1! + 4! \times 5! + 2!) + 3! = 1^1 \times 4^3 + 5^2 \times (2^5 + 3^4).$$

$$\mathbf{2898} := (1! + 2!) \times 3! + 4! \times 5! = (1^4 + 2^5 + 3^2) \times (4^3 + 5^1).$$

$$\begin{aligned}\mathbf{2912} &:= (1! + 5!) \times 4! + 3! + 2! = (1^5 + 5^2) \times (4^3 + 3^1 \times 2^4). \\ &= 1^2 \times 5^1 \times 4^3 + 3^4 \times 2^5. \\ &= 1^4 \times 5^1 \times 4^3 \times 3^2 + 2^5.\end{aligned}$$

$$\mathbf{2928} := 2! \times (6! + 3! \times 5! + 4!) = 2^6 \times 6^2 + 3^5 + 5^3 + 4^4.$$

$$\begin{aligned}\mathbf{3008} &:= 3! + 2! + 5! \times (1! + 4!) = (3^2 + 2^5 + 5^1 + 1^4) \times 4^3. \\ &= (3^3 + 2^5 \times 5^1 + 1^4) \times 4^2.\end{aligned}$$

$$\mathbf{3027} := 1! + 2! + (5! + 3!) \times 4! = (1^2 \times 2^4) \times 5^3 + 3^1 + 4^5.$$

$$\mathbf{3050} := 2! + (5! + 1! + 3!) \times 4! = (2^5 + 5^1) \times (1^3 + 3^4) + 4^2.$$

$$\begin{aligned}\mathbf{3072} &:= (1! \times 2! + 5! + 3!) \times 4! = ((1^4 + 2^5) \times 5^1 + 3^3) \times 4^2. \\ &= 1^2 \times 2^4 \times (5^3 + 3^1) + 4^5.\end{aligned}$$

$$\mathbf{3073} := 1! + (2! + 3! + 5!) \times 4! = 1^2 + 2^4 \times (3^1 + 5^3) + 4^5.$$

$$\mathbf{3096} := (2! + 3! + 1! + 5!) \times 4! = 2^5 \times 3^4 + (1^2 + 5^3) \times 4^1.$$

$$\begin{aligned}\mathbf{3152} &:= 3! + (4! + 2!) \times (1! + 5!) = (3^1 + 4^2 + 2^3) \times 1^4 + 5^5. \\ &= 3^1 + 4^5 + (2^4 + 1^2) \times 5^3.\end{aligned}$$

$$\begin{aligned}\mathbf{3168} &:= ((1! \times 2!) \times 3! + 5!) \times 4! = (1^4 + 2^3) \times 3^1 + 5^5 + 4^2. \\ &:= (1! \times 2! \times 3! + 5!) \times 4! = 1^1 \times 2^4 \times (3^2 + 5^3) + 4^5. \\ &:= (1! \times 3! \times 2! + 5!) \times 4! = 1^3 \times 3^1 \times (2^5 \times 5^2 + 4^4). \\ &= 1^4 \times 3^2 \times (2^5 + 5^1 \times 4^3).\end{aligned}$$

$$\begin{aligned} \mathbf{3169} &:= 1! + (3! \times 2! + 5!) \times 4! = 1^3 + 3^1 \times (2^5 \times 5^2 + 4^4). \\ &\quad = 1^4 + 3^2 \times (2^5 + 5^1 \times 4^3). \end{aligned}$$

$$\begin{aligned} \mathbf{3192} &:= (3! \times 2! + 1! + 5!) \times 4! = 3^1 \times (2^4 + 1^3) + 5^5 + 4^2. \\ &\quad = 3^1 + (2^2 + 1^5) \times 5^4 + 4^3. \end{aligned}$$

$$\begin{aligned} \mathbf{3200} &:= (4! + 1!) \times (2! + 3! + 5!) = (4^2 + 1^4 + 2^3) \times 3^1 + 5^5. \\ &\quad = 4^2 \times (1^4 + 2^1) + 3^3 + 5^5. \\ &\quad = 4^3 \times 1^4 + 2^1 + 3^2 + 5^5. \\ &\quad = 4^5 + (1^2 + 2^4) \times (3^1 + 5^3). \end{aligned}$$

$$\begin{aligned} \mathbf{3216} &:= (5! + (3! + 1!) \times 2!) \times 4! = (5^2 + 3^5) \times 1^4 \times (2^3 + 4^1). \\ &\quad = (5^5 + 3^3) \times 1^2 + 2^4 \times 4^1. \\ &\quad = 5^5 + 3^2 \times (1^4 + 2^1) + 4^3. \end{aligned}$$

$$\begin{aligned} \mathbf{3246} &:= 3! + (2! + 4! + 1!) \times 5! = 3^1 \times (2^4 + 4^5) + 1^2 + 5^3. \\ &\quad = 3^4 + 2^3 \times (4^1 + 1^2) + 5^5. \end{aligned}$$

$$\begin{aligned} \mathbf{3276} &:= (5! + 3!) \times 1! \times (2! + 4!) = (5^3 \times 3^2 + 1^4) \times 2^1 + 4^5. \\ &\quad := (5! + 3!) \times 1! \times (4! + 2!) = 5^5 + 3^3 \times (1^2 + 4^1) + 2^4. \end{aligned}$$

$$\begin{aligned} \mathbf{3277} &:= 1! + (2! + 4!) \times (3! + 5!) = 1^4 \times 2^3 \times (4^2 + 3^1) + 5^5. \\ \mathbf{3300} &:= (1! + 4!) \times (5! + 3! \times 2!) = (1^5 + 4^1 \times (5^3 + 3^4)) \times 2^2. \end{aligned}$$

$$\begin{aligned} \mathbf{3302} &:= (4! + 2!) \times (1! + 5! + 3!) = 4^5 + (2^4 + 1^1) \times (5^3 + 3^2). \\ &\quad := (4! + 2!) \times (3! + 1! + 5!) = 4^2 \times (2^3 + 3^1) + 1^4 + 5^5. \end{aligned}$$

$$\begin{aligned} \mathbf{3312} &:= (5! + 3! \times (1! + 2!)) \times 4! = (5^3 + 3^4 + 1^5) \times 2^2 \times 4^1. \\ &\quad = (5^3 + 3^5) \times (1^4 + 2^2 + 4^1). \\ &\quad := (5! + 3! \times (2! + 1!)) \times 4! = 5^5 + (3^1 + 2^3) \times (1^4 + 4^2). \end{aligned}$$

$$\begin{aligned} \mathbf{3603} &:= 1! + 2! + (3! + 4!) \times 5! = (1^5 + 2^1) \times (3^2 \times 4^3 + 5^4). \\ \mathbf{3607} &:= 1! + 3! + 4! \times 5! + 6! = 1^6 \times 3^5 + 4^1 \times (5^4 + 6^3). \\ \mathbf{3632} &:= 2! + (1! + 5!) \times (3! + 4!) = 2^2 \times 1^1 \times (5^4 + 3^3) + 4^5. \end{aligned}$$

$$\begin{aligned} \mathbf{3648} &:= 1! \times 6! + (2! + 5!) \times 4! = (1^5 + 6^2) \times 2^6 + 5^1 \times 4^4. \\ &\quad := 1! \times 6! + (5! + 2!) \times 4! = (1^4 \times 6^2 + 5^1) \times 2^6 + 4^5. \end{aligned}$$

$$\mathbf{3649} := 1! + 4! \times (2! + 5!) + 6! = 1^4 + 4^5 + 2^6 \times (5^1 + 6^2).$$

$$\mathbf{3661} := 1! + (2! + 5!) \times (3! + 4!) = (1^5 + 2^3) \times 5^1 \times 3^4 + 4^2.$$

$$\mathbf{3690} := (1! + 2! + 5!) \times (3! + 4!) = (1^2 + 2^1) \times (5^3 + 3^4 + 4^5).$$

$$\mathbf{3722} := 2! + (4! + 3! + 1!) \times 5! = (2^3 + 4^5) \times 3^1 + 1^2 + 5^4.$$

$$\mathbf{3744} := (1! \times 3! + 5!) \times 4! + 6! = (1^6 \times 3^5 + 5^3 + 4^4) \times 6^1.$$

$$\mathbf{3745} := 1! + (3! + 5!) \times 4! + 6! = 1^6 + (3^5 + 5^3 + 4^4) \times 6^1.$$

$$\mathbf{3840} := (1! \times 4! + 2! + 3!) \times 5! = (1^4 + 4^3) \times (2^1 + 3^2) + 5^5. \\ = 1^4 \times 4^3 \times (2^5 + 3^1 + 5^2).$$

$$:= 1! \times 5! \times (4! + 2!) + 6! = (1^5 + 5^1) \times 4^4 + 2^6 \times 6^2.$$

$$\mathbf{3841} := 1! + (4! + 2! + 3!) \times 5! = 1^4 + 4^3 \times (2^5 + 3^1 + 5^2).$$

$$\mathbf{3872} := (1! + 5!) \times (2! + 3! + 4!) = (1^3 + 5^1 \times 2^5 + 3^4) \times 4^2. \\ := (1! + 5!) \times (3! + 4! + 2!) = (1^3 + 5^1 + 3^2) \times 4^4 + 2^5.$$

$$\mathbf{3960} := (2! + 4! + 1! + 3!) \times 5! = (2^3 + 4^4) \times (1^5 + 3^2 + 5^1).$$

$$\mathbf{4320} := (4! + 2! \times 3! \times 1!) \times 5! = (4^2 + 2^4) \times 3^3 \times 1^5 \times 5^1. \\ = (4^3 + 2^4) \times 3^2 \times (1^5 + 5^1). \\ = (4^3 + 2^5) \times 3^2 \times 1^4 \times 5^1. \\ = (4^4 + 2^5) \times (3^2 + 1^3 + 5^1).$$

$$\mathbf{4321} := 1! + (3! \times 2! + 4!) \times 5! = 1^4 + 3^2 \times (2^5 + 4^3) \times 5^1. \\ = 1^5 + 3^3 \times (2^4 + 4^2) \times 5^1.$$

$$\mathbf{4326} := 3! + 5! \times 4! + 2! \times 6! = 3^6 + 5^5 + 4^2 \times 2^4 + 6^3.$$

$$\mathbf{4344} := 2! \times 6! + (1! + 5!) \times 4! = 2^5 + 6^2 \times (1^4 + 5^1) + 4^6.$$

$$\mathbf{4347} := 1! + 2! + 4! + 6! \times 3! = (1^4 + 2^6 + 4^1) \times (6^2 + 3^3). \\ = (1^4 + 2^6 + 4^2 \times 6^1) \times 3^3. \\ = (1^6 + 2^4 + 4^1 \times 6^2) \times 3^3.$$

$$\mathbf{4352} := (1! + 6!) \times 3! + 2! + 4! = (1^1 + 6^2 + 3^3) \times 2^6 + 4^4. \\ = (1^3 + 6^1 + 3^2) \times 2^4 + 4^6. \\ = (1^4 + 6^2 + 3^3) \times (2^6 + 4^1).$$

$$\mathbf{4368} := 1! \times 2! \times 4! + 3! \times 6! = 1^3 \times 2^6 \times 4^2 \times 3^1 + 6^4.$$

$$\mathbf{4369} := 1! + 2! \times 4! + 3! \times 6! = 1^3 + 2^6 \times 4^2 \times 3^1 + 6^4.$$

$$\mathbf{4374} := 2! \times 4! + (1! + 6!) \times 3! = (2^4 + 4^3 + 1^6) \times 6^1 \times 3^2.$$

$$\mathbf{4440} := (1! + 4!) \times 5! + 2! \times 6! = 1^6 + 4^2 + 5^5 + 2^1 + 6^4.$$

$$:= (1! + 4! + 2! \times 3!) \times 5! = 1^5 + 4^3 + (2^2 + 3^1) \times 5^4.$$

$$\mathbf{4442} := 1! \times 5! + 3! \times 6! + 2! = (1^3 + 5^1) \times 3^6 + 6^2 + 2^5.$$

$$\mathbf{4448} := (1! + 6!) \times 3! + 2! + 5! = 1^5 + 6^1 \times (3^6 + 2^3) + 5^2.$$

$$\mathbf{4453} := 1! + 3! \times (2! + 6!) + 5! = (1^5 + 3^6 + 2^3) \times 6^1 + 5^2.$$

$$\mathbf{4466} := 1! \times 2! + (6! + 4!) \times 3! = 1^1 + 2^3 \times 6^2 + 4^6 + 3^4.$$

$$\mathbf{4470} := (1! + 6!) \times 3! + 4! + 5! = 1^4 \times 6^1 + 3^5 + 4^6 + 5^3.$$

$$\mathbf{4472} := 2! + 3! \times (1! + 4! + 6!) = 2^2 \times (3^6 + 1^1 + 4^3) + 6^4.$$

$$= 2^4 \times (3^2 + 1^1) + 4^6 + 6^3.$$

$$\mathbf{4476} := (3! \times 1!) \times (2! + 6! + 4!) = (3^4 + 1^2) \times 2^1 + 6^3 + 4^6.$$

$$:= (3! \times 1!) \times (4! + 6! + 2!) = (3^6 + (1^4 + 4^3) \times 6^1) \times 2^2.$$

$$\mathbf{4482} := (1! + 4! + 6! + 2!) \times 3! = ((1^4 + 4^2) \times 6^1 + 2^6) \times 3^3.$$

$$\mathbf{4560} := (4! + 2! \times (1! + 3!)) \times 5! = (4^2 + 2^5 \times (1^4 + 3^3)) \times 5^1.$$

$$= 4^1 + (2^4 + 1^3) \times (3^5 + 5^2).$$

$$\mathbf{4562} := 2! \times (1! + 5!) + 3! \times 6! = 2^5 + (1^3 + 5^2 + 3^6) \times 6^1.$$

$$\mathbf{4596} := (2! + 4! + 6!) \times 3! + 5! = 2^4 + 4^6 + 6^3 + 3^5 + 5^2.$$

$$\mathbf{4608} := 1! \times 3! \times (2! \times 4! + 6!) = ((1^6 + 3^1) \times 2^4 + 4^3) \times 6^2.$$

$$:= 1! \times 3! \times (4! \times 2! + 6!) = ((1^6 + 3^3) \times 4^1 + 2^4) \times 6^2.$$

$$\mathbf{4609} := 1! + 3! \times (4! \times 2! + 6!) = 1^2 \times 3^4 + 4^6 + 2^1 \times 6^3.$$

$$\mathbf{4614} := 3! \times (1! + 2! \times 4! + 6!) = (3^2 + 1^6 + 2^3) \times 4^4 + 6^1.$$

$$\mathbf{4752} := (4! \times (2! + 1!) + 6!) \times 3! = (4^1 \times 2^2) \times 1^6 \times (6^3 + 3^4).$$

$$:= (6! + (1! + 2!) \times 4!) \times 3! = 6^2 \times (1^4 + 2^6 + 4^3 + 3^1).$$

$$\begin{aligned}
 5040 &:= 2! \times 6! + (3! + 4!) \times 5! = 2^4 \times 6^2 + 3^5 + 4^6 + 5^3. \\
 &:= 5! \times ((2! + 1!) \times 3! + 4!) = 5^4 \times 2^3 + (1^5 + 3^2) \times 4^1. \\
 &:= 5! \times (3! \times (2! + 1!) + 4!) = (5^4 + 3^1) \times 2^3 \times 1^5 + 4^2.
 \end{aligned}$$

$$\begin{aligned}
 5052 &:= (1! \times 2! + 5! + 6!) \times 3! = (1^2 + 2^5) \times (5^3 + 6^1) + 3^6. \\
 5053 &:= 1! + (5! + 6! + 2!) \times 3! = (1^5 + 5^1 \times 6^3) \times 2^2 + 3^6. \\
 5064 &:= 1! \times 4! + 3! \times (6! + 5!) = 1^5 + 4^3 + 3^6 \times 6^1 + 5^4. \\
 5072 &:= 1! \times 2! + 3! + 7! + 4! = (1^4 \times 2^7 + 3^3 \times 7^1) \times 4^2. \\
 5073 &:= 1! + 2! + 3! + 7! + 4! = 1^4 + (2^7 + 3^3 \times 7^1) \times 4^2.
 \end{aligned}$$

$$\begin{aligned}
 5076 &:= 1! \times 2! \times 3! + 7! + 4! = 1^4 \times 2^1 \times (3^7 + 7^3) + 4^2. \\
 5077 &:= 1! + 2! \times 3! + 7! + 4! = 1^4 + 2^1 \times (3^7 + 7^3) + 4^2. \\
 5078 &:= 2! \times (1! + 3!) + 7! + 4! = 2^1 \times (1^4 + 3^7 + 7^3) + 4^2. \\
 5094 &:= 1! \times 3! + 7! + 4! \times 2! = (1^4 + 3^7 + 7^3 + 4^2) \times 2^1. \\
 5162 &:= 2! + 5! + (1! + 3!) \times 6! = 2^5 + (5^3 + 1^2 + 3^6) \times 6^1.
 \end{aligned}$$

$$\begin{aligned}
 5173 &:= 1! + 5! + 2! \times 3! + 7! = (1^7 + 5^3) \times (2^5 + 3^2) + 7^1. \\
 &= 1^3 \times 5^5 + 2^7 \times (3^2 + 7^1).
 \end{aligned}$$

$$\begin{aligned}
 5174 &:= (1! + 3!) \times (6! + 2!) + 5! = 1^3 \times 3^6 \times 6^1 + 2^5 \times 5^2. \\
 5186 &:= 1! \times 2! + 4! + 5! + 7! = 1^7 + 2^4 + 4^5 \times 5^1 + 7^2. \\
 5196 &:= (1! \times 2! + 4!) \times 3! + 7! = 1^7 + 2^2 + 4^3 \times 3^4 + 7^1. \\
 5222 &:= (1! + 3!) \times (4! + 2! + 6!) = 1^6 \times 3^4 \times 4^3 + 2^1 + 6^2. \\
 5280 &:= (1! + 3!) \times 6! + 5! \times 2! = (1^6 + 3^1 + 6^2 + 5^3) \times 2^5. \\
 5340 &:= 2! \times 3! \times (1! + 4!) + 7! = 2^4 + 3^7 + 1^1 + 4^3 \times 7^2.
 \end{aligned}$$

$$\begin{aligned}
 5376 &:= (1! + 3!) \times (2! \times 4! + 6!) = ((1^3 + 3^2) \times 2^6 + 4^4) \times 6^1. \\
 &= (1^6 + 3^3) \times (2^4 + 4^2) \times 6^1. \\
 &:= (1! + 3!) \times (4! \times 2! + 6!) = (1^6 \times 3^1) \times 4^3 + 2^2 \times 6^4. \\
 &:= 2! \times (1! + 3!) \times 4! + 7! = (2^7 + (1^4 + 3^2) \times 4^3) \times 7^1.
 \end{aligned}$$

$$\begin{aligned}
 5376 &:= 2! \times (1! + 3!) \times 4! + 7! = 2^7 \times (1^2 + 3^3) + 4^4 \times 7^1. \\
 5472 &:= 7! + 4! \times (1! + 2!) \times 3! = (7^2 + 4^3 + 1^7) \times 2^4 \times 3^1. \\
 5760 &:= 1! \times 3! \times (2! \times 5! + 6!) = (1^6 \times 3^1 + 2^5 + 5^3) \times 6^2. \\
 5761 &:= 1! + 3! \times (2! \times 5! + 6!) = 1^6 + (3^1 + 2^5 + 5^3) \times 6^2. \\
 5768 &:= (1! + 4! \times 5!) \times 2! + 3! = 1^2 \times 4^5 \times 5^1 + 2^3 \times 3^4.
 \end{aligned}$$

$$\begin{aligned}
 5772 &:= 1! \times 2! \times (4! \times 5! + 3!) = (1^1 + 2^2) \times 4^5 + 5^4 + 3^3. \\
 &= (1^5 + 2^3) \times (4^2 + 5^4) + 3^1. \\
 &:= 7! + 3! \times (2! \times 1! + 5!) = (7^2 \times 3^3) \times 2^1 + 1^7 + 5^5.
 \end{aligned}$$

$$\begin{aligned} \mathbf{5773} &:= 1! + (4! \times 5! + 3!) \times 2! = (1^2 + 4^5) \times 5^1 + 3^4 \times 2^3. \\ &:= 1! + 7! + 3! \times (2! + 5!) = 1^7 + (7^2 \times 3^3) \times 2^1 + 5^5. \end{aligned}$$

$$\begin{aligned} \mathbf{5778} &:= 3! \times (2! + 1! + 5!) + 7! = 3^3 \times ((2^5 + 1^7) \times 5^1 + 7^2). \\ &= 3^3 \times (2^5 + (1^7 + 5^2) \times 7^1). \end{aligned}$$

$$\mathbf{5792} := (1! + 6!) \times (2! + 3!) + 4! = (1^1 + 6^3 + 2^6 + 3^4) \times 4^2.$$

$$\begin{aligned} \mathbf{5881} &:= 1! + (3! + 2!) \times 6! + 5! = (1^5 + 3^6) \times 2^3 + 6^2 + 5^1. \\ &= 1^1 \times 3^6 + 2^5 \times (6^2 + 5^3). \end{aligned}$$

$$\mathbf{5882} := (1! + 3!) \times (5! + 6!) + 2! = 1^1 + 3^6 + (5^3 + 6^2) \times 2^5.$$

$$\mathbf{5888} := (2! + 3!) \times (1! + 6!) + 5! = 2^1 \times (3^5 + 1^6) + 6^3 \times 5^2.$$

$$\begin{aligned} \mathbf{5904} &:= (2! \times 5! \times 1! + 3!) \times 4! = 2^2 \times (5^1 \times (1^3 + 3^5) + 4^4). \\ &= 2^2 \times (5^3 + 1^4 + 3^5) \times 4^1. \\ &= 2^4 \times 5^3 + (1^1 + 3^5) \times 4^2. \end{aligned}$$

$$\begin{aligned} \mathbf{5905} &:= 1! + (2! \times 5! + 3!) \times 4! = 1^1 + 2^4 + (5^3 + 3^5) \times 4^2. \\ &:= 1! + 7! + 6! + 3! \times 4! = (1^7 + 7^1) \times 6^3 + 3^4 + 4^6. \end{aligned}$$

$$\begin{aligned} \mathbf{5952} &:= (1! \times 2! + 3!) \times (4! + 6!) = 1^6 \times 2^2 \times (3^1 \times 4^3 + 6^4). \\ &:= (2! \times (1! + 5!) + 3!) \times 4! = 2^4 \times 1^2 \times (5^3 + 3^5 + 4^1). \end{aligned}$$

$$\begin{aligned} \mathbf{5953} &:= 1! + (2! + 3!) \times (4! + 6!) = 1^6 + 2^2 \times (3^1 \times 4^3 + 6^4). \\ \mathbf{5960} &:= (1! + 4! + 6!) \times (3! + 2!) = (1^6 \times 4^3 + 6^2 \times 3^4) \times 2^1. \end{aligned}$$

$$\begin{aligned} \mathbf{6000} &:= 7! \times 1! + (2! + 3!) \times 5! = (7^1 \times 1^7 + 2^5 + 3^2) \times 5^3. \\ &= (7^3 + 1^2) \times 2^1 + 3^7 + 5^5. \end{aligned}$$

$$\begin{aligned} \mathbf{6001} &:= 1! + 5! \times (2! + 3!) + 7! = 1^7 + 5^3 \times (2^5 + 3^2 + 7^1). \\ \mathbf{6012} &:= 2! \times ((1! + 4!) \times 5! + 3!) = (2^3 + 1^1) \times (4^2 + 5^4) + 3^5. \end{aligned}$$

$$\begin{aligned} \mathbf{6048} &:= 2! \times (5! + 3!) \times 1! \times 4! = 2^3 \times (5^4 + 3^1) \times 1^2 + 4^5. \\ &= 2^5 \times 5^2 + (3^4 + 1^1) \times 4^3. \\ &= 2^5 + (5^3 \times 3^1 + 1^4) \times 4^2. \end{aligned}$$

$$\begin{aligned} \mathbf{6049} &:= 1! + (3! + 5!) \times 2! \times 4! = 1^2 + (3^1 + 5^4) \times 2^3 + 4^5. \\ &\quad = 1^5 + 3^1 \times (5^3 \times 2^4 + 4^2). \end{aligned}$$

$$\begin{aligned} \mathbf{6096} &:= (1! + 3! + 5!) \times 4! \times 2! = ((1^4 + 3^1) \times 5^3 + 4^5) \times 2^2. \\ &\quad = (1^3 + 3^5 + 5^1 \times 4^4) \times 2^2. \\ &\quad = (1^5 + 3^1) \times (5^3 + 4^4) \times 2^2. \\ &\quad = 1^3 + 3^5 \times 5^2 + 4^1 + 2^4. \\ &\quad = 1^4 \times 3^1 \times (5^3 \times 4^2 + 2^5). \end{aligned}$$

$$\begin{aligned} \mathbf{6480} &:= (1! \times 4! \times 2! + 3!) \times 5! = (1^4 \times 4^2 + 2^5) \times 3^3 \times 5^1. \\ &\quad = 1^3 + 4^1 + (2^4 + 3^5) \times 5^2. \\ &:= 1! \times 4! \times 5! \times 2! + 6! = (1^5 + 4^2 \times 5^1) \times 2^6 + 6^4. \\ &\quad = 1^2 \times 4^5 \times 5^1 + 2^6 + 6^4. \end{aligned}$$

$$\begin{aligned} \mathbf{6481} &:= 1! + (2! \times 4!) \times 5! + 6! = 1^2 + 2^6 + 4^5 \times 5^1 + 6^4. \\ &:= 1! + (3! + 2! \times 4!) \times 5! = (1^1 + 3^5) \times (2^3 + 4^2) + 5^4. \\ &\quad = 1^4 + 3^3 \times (2^5 + 4^2) \times 5^1. \end{aligned}$$

$$\mathbf{6492} := (1! \times 3! + 6!) \times 2! + 7! = 1^6 + 3^1 + 6^3 + 2^7 \times 7^2.$$

$$\begin{aligned} \mathbf{6528} &:= 2! \times 1! \times (6! + 4!) + 7! = 2^7 \times (1^6 + 6^2) + 4^4 \times 7^1. \\ &:= 4! \times 2! \times (1! + 5!) + 6! = (4^2 + 2^5) \times 1^6 + 5^1 \times 6^4. \\ &\quad = (4^4 + 2^5 \times (1^6 + 5^2)) \times 6^1. \end{aligned}$$

$$\mathbf{6534} := (1! + 5!) \times (2! \times 4! + 3!) = 1^2 + 5^5 \times 2^1 + 4^4 + 3^3.$$

$$\begin{aligned} \mathbf{6600} &:= (1! + 3! + 2! \times 4!) \times 5! = (1^3 + 3^5 + 2^4 + 4^1) \times 5^2. \\ &\quad = 1^3 + 3^1 + 2^2 \times (4^5 + 5^4). \end{aligned}$$

$$\mathbf{6696} := (1! + 3! + 2!) \times (4! + 6!) = 1^1 \times 3^4 \times (2^6 + 4^2) + 6^3.$$

$$\begin{aligned} \mathbf{6720} &:= (2! \times (4! + 1!) + 3!) \times 5! = (2^5 + 4^2) \times (1^4 + 3^3) \times 5^1. \\ &\quad = (2^5 + 4^2 \times (1^3 + 3^4)) \times 5^1. \\ &\quad = 2^5 \times (4^1 \times 1^2 + 3^4 + 5^3). \\ &:= 5! \times (1! + 4!) \times 2! + 6! = (5^1 + 1^6) \times 4^5 + 2^4 \times 6^2. \\ &\quad = 5^1 \times 1^6 \times (4^2 + 2^5 + 6^4). \end{aligned}$$

$$\begin{aligned}
 7200 &:= 2! \times (6! \times 1! + 4! \times 5!) = (2^5 \times (6^2 + 1^6) + 4^4) \times 5^1. \\
 &:= 2! \times 1! \times (3! + 4!) \times 5! = (2^3 \times (1^5 + 3^1) + 4^4) \times 5^2. \\
 &\quad = (2^3 + 1^5 + 3^4) \times 4^2 \times 5^1. \\
 &\quad = (2^5 + (1^4 + 3^1) \times 4^3) \times 5^2.
 \end{aligned}$$

$$\begin{aligned}
 7201 &:= 1! + 2! \times (4! + 3!) \times 5! = 1^3 + 2^5 + 4^4 \times (3^1 + 5^2). \\
 &\quad = 1^4 + (2^5 + 4^3) \times 3^1 \times 5^2.
 \end{aligned}$$

$$7206 := 3! + 7! + (1! + 2!) \times 6! = (3^6 + 7^3 + 1^2 + 2^7) \times 6^1.$$

$$7218 := (3! + 6!) \times (1! + 2!) + 7! = 3^6 + 6^3 + 1^1 + 2^7 \times 7^2.$$

$$7440 := 2! \times ((4! + 1!) \times 5! + 6!) = 2^6 \times 4^2 \times (1^5 + 5^1) + 6^4.$$

$$7560 := (2! + 3! + 1!) \times (5! + 6!) = 2^3 \times (3^6 + (1^5 + 5^1) \times 6^2).$$

$$\begin{aligned}
 7922 &:= 1! \times 2! + 7! + 4! \times 5! = 1^1 + 2^7 \times 7^2 + 4^5 + 5^4. \\
 &\quad = 1^2 + 2^7 + 7^1 \times 4^5 + 5^4.
 \end{aligned}$$

$$8161 := 1! + (2! + 4!) \times 5! + 7! = (1^2 \times 2^7 + 4^5) \times 5^1 + 7^4.$$

$$8280 := (1! + 2! + 4!) \times 5! + 7! = (1^7 + 2^2) \times (4^5 + 5^4 + 7^1).$$

$$8676 := (1! + 6!) \times 3! \times 2! + 4! = 1^1 \times 6^2 + 3^3 \times (2^6 + 4^4).$$

$$8760 := 1! \times 3! \times 2! \times 6! + 5! = 1^5 + 3^2 + (2^6 + 6^1) \times 5^3.$$

$$8761 := 1! + 2! \times 3! \times 6! + 5! = 1^6 \times 2^3 + 3^5 \times 6^2 + 5^1.$$

$$8762 := 1! + 3! \times 6! \times 2! + 5! = 1^6 + 3^5 \times 6^2 + 2^3 + 5^1.$$

$$8772 := 2! \times (6! + 1!) \times 3! + 5! = (2^5 + 6^2) \times (1^6 + 3^1 + 5^3).$$

$$8784 := 1! \times 3! \times (4! + 2! \times 6!) = 1^4 \times 3^6 \times (4^1 + 2^3) + 6^2.$$

$$8785 := 1! + 3! \times (4! + 2! \times 6!) = 1^4 + 3^6 \times (4^1 + 2^3) + 6^2.$$

$$8880 := 1! \times 2! \times (5! + 3! \times 6!) = (1^2 + 2^1) \times 5^3 + 3^6 + 6^5.$$

$$8940 := 2! \times (1! + 4! + 6!) \times 3! = (2^1 + 1^6) \times (4^3 + 6^2 \times 3^4).$$

$$\begin{aligned}
 9072 &:= (2! + 1!) \times 4! \times (5! + 3!) = 2^4 \times 1^5 \times (4^2 + 5^1) \times 3^3. \\
 &\quad = 2^5 \times 1^3 + 4^2 \times 5^1 \times 3^4.
 \end{aligned}$$

$$9360 := ((1! + 2!) \times 4! + 3!) \times 5! = 1^4 + (2^1 + 4^5) \times 3^2 + 5^3.$$

$$:= (1! \times 5! + 6! \times 2!) \times 3! = 1^6 + 5^3 + (6^2 + 2^1) \times 3^5.$$

$$:= 1! \times 5! + 6! \times 2! \times 3! = 1^2 + 5^3 + 6^5 + 2^1 \times 3^6.$$

$$9361 := 1! + 3! \times (2! \times 6! + 5!) = (1^2 + 3^6) \times 2^1 + 6^5 + 5^3.$$

$$9366 := 3! \times (1! + 5! + 2! \times 6!) = (3^6 + (1^3 + 5^2) \times 2^5) \times 6^1.$$

$$\begin{aligned} \mathbf{9648} &:= (2! \times (6! + 4!) + 5!) \times 3! = 2^2 \times 6^4 + 4^6 + 5^3 + 3^5. \\ &= 2^6 + 6^2 \times 4^4 + 5^3 + 3^5. \end{aligned}$$

$$\mathbf{10080} := 1! \times 2! \times 3! \times (6! + 5!) = 1^6 \times 2^5 \times (3^3 + 6^2) \times 5^1.$$

$$\mathbf{10081} := 1! + 2! \times 3! \times (6! + 5!) = 1^6 + 2^5 \times (3^3 + 6^2) \times 5^1.$$

$$\mathbf{10112} := 2! \times (1! + 7!) + 3! + 4! = 2^7 \times (1^1 + 7^2 + 3^3) + 4^4.$$

$$\mathbf{10116} := (1! \times 3! + 7!) \times 2! + 4! = (1^7 + 3^1) \times (7^4 + 2^3 \times 4^2).$$

$$\begin{aligned} \mathbf{10136} &:= 2! \times (1! + 4! + 7!) + 3! = 2^2 \times 1^4 \times (4^1 + 7^3 + 3^7). \\ &= 2^4 \times 1^2 + 4^1 \times (7^3 + 3^7). \end{aligned}$$

$$\begin{aligned} \mathbf{10140} &:= (1! \times 3! + 7! + 4!) \times 2! = (1^2 + 3^7 + 7^3) \times 4^1 + 2^4. \\ &= (1^4 + 3^7 + 7^3 + 4^1) \times 2^2. \end{aligned}$$

$$\mathbf{10200} := (1! + 3!) \times 2! \times 6! + 5! = (1^5 \times 3^1 \times 2^6 + 6^3) \times 5^2.$$

$$\mathbf{10206} := 2! \times 1! \times 7! + 5! + 3! = (2^7 + (1^5 + 7^2) \times 5^1) \times 3^3.$$

$$\begin{aligned} \mathbf{10224} &:= 1! \times 2! \times 7! + 3! \times 4! = (1^2 \times 2^7 + 7^4 + 3^3) \times 4^1. \\ &:= 1! \times 2! \times 7! + 4! \times 3! = 1^7 \times 2^4 \times (7^1 + 4^3) \times 3^2. \\ &:= 1! \times 4! + 5! + 2! \times 7! = (1^7 \times 4^2) \times 5^4 + 2^5 \times 7^1. \end{aligned}$$

$$\begin{aligned} \mathbf{10225} &:= 1! + 2! \times 7! + 4! + 5! = 1^7 + 2^5 \times 7^1 + 4^2 \times 5^4. \\ &:= 1! + 2! \times 7! + 3! \times 4! = 1^2 + (2^7 + 7^4 + 3^3) \times 4^1. \\ &:= 1! + 2! \times 7! + 4! \times 3! = 1^7 + 2^4 \times (7^1 + 4^3) \times 3^2. \end{aligned}$$

$$\mathbf{10326} := 1! \times 3! + 2! \times (5! + 7!) = 1^7 + (3^3 + 2^5) \times 5^2 \times 7^1.$$

$$\mathbf{10332} := (1! \times 3! + 5! + 7!) \times 2! = (1^7 + 3^5 + 5^3) \times 7^1 \times 2^2.$$

$$\mathbf{10344} := 1! \times 2! \times (7! + 5!) + 4! = (1^7 + 2^1) \times 7^4 + 5^5 + 4^2.$$

$$\begin{aligned} \mathbf{10368} &:= (3! \times 4! \times 1! + 7!) \times 2! = (3^2 + 4^3 + 1^4 + 7^1) \times 2^7. \\ &= (3^3 + 4^1 + 1^4 + 7^2) \times 2^7. \\ &= 3^2 \times (4^3 + 1^7 + 7^1) \times 2^4. \\ &= 3^3 \times 4^2 \times (1^7 + 7^1 + 2^4). \\ &= 3^2 \times (4^4 \times 1^3 + 7^1 \times 2^7). \end{aligned}$$

$$\begin{aligned} \mathbf{10369} &:= 1! + (3! \times 4! + 7!) \times 2! = 1^3 + 3^2 \times (4^4 + 7^1 \times 2^7). \\ &= 1! + (4! + 7! + 5!) \times 2! = 1^4 + 4^5 \times 7^1 + 5^2 \times 2^7. \end{aligned}$$

$$\begin{aligned}
 10416 &:= (1! + 3!) \times (4! + 6!) \times 2! = (1^6 \times 3^4 \times 4^2 + 6^1) \times 2^3. \\
 &= 1^6 \times 3^1 \times 4^2 + 6^4 \times 2^3. \\
 &= 1^6 \times 3^1 \times (4^2 \times 6^3 + 2^4).
 \end{aligned}$$

$$\begin{aligned}
 10800 &:= 1! \times 7! \times 2! + 5! \times 3! = (1^7 + 7^1 \times (2^5 + 5^2)) \times 3^3. \\
 10801 &:= 1! + (3! + 2!) \times 6! + 7! = (1^7 + 3^3) \times 2^6 \times 6^1 + 7^2. \\
 10806 &:= 1! \times 3! + 2! \times 7! + 6! = 1^6 \times 3^7 \times 2^2 + 7^3 \times 6^1. \\
 10807 &:= 1! + 3! + 2! \times 7! + 6! = 1^6 + 3^7 \times 2^2 + 7^3 \times 6^1. \\
 10812 &:= 2! \times (3! + 7!) \times 1! + 6! = 2^2 \times 3^7 + (7^3 + 1^6) \times 6^1. \\
 10848 &:= (1! + 5!) \times 4! \times 2! + 7! = (1^7 + 5^1) \times (4^5 + 2^4 \times 7^2).
 \end{aligned}$$

$$\begin{aligned}
 12984 &:= 4! + 3! \times (1! + 2!) \times 6! = 4^2 \times (3^6 + 1^1) + 2^3 + 6^4. \\
 &= 4! + 6! \times (1! + 2!) \times 3! = ((4^6 + 6^3) \times 1^2 + 2^4) \times 3^1.
 \end{aligned}$$

$$\begin{aligned}
 13104 &:= 3! \times ((1! + 2!) \times 6! + 4!) = (3^3 \times 1^4 + 2^6) \times 6^2 \times 4^1. \\
 13320 &:= (1! + 2!) \times (5! + 3! \times 6!) = (1^6 \times 2^1 + 5^3 + 3^5) \times 6^2. \\
 13392 &:= (1! + 2!) \times (4! + 6!) \times 3! = ((1^6 + 2^1) \times 4^3 + 6^4) \times 3^2. \\
 13680 &:= ((2! + 1!) \times 6! + 5!) \times 3! = 2^6 + (1^1 + 6^2) \times (5^3 + 3^5). \\
 13681 &:= 1! + 7! + 6! \times 3! \times 2! = (1^7 + 7^1 \times 6^3) \times 3^2 + 2^6.
 \end{aligned}$$

$$\begin{aligned}
 14400 &:= 1! \times 2! \times 7! + 3! \times 6! = 1^7 \times 2^6 \times (7^1 \times 3^3 + 6^2). \\
 &= (4! \times 5! + 3! \times 6!) \times 2! = 4^6 + (5^2 + 3^4 + 6^3) \times 2^5.
 \end{aligned}$$

$$14401 := 1! + 2! \times 7! + 3! \times 6! = 1^7 + 2^6 \times (7^1 \times 3^3 + 6^2).$$

$$\begin{aligned}
 15552 &:= (1! + 2!) \times (4! + 5! + 7!) = (1^7 \times 2^5 + 4^4) \times (5^1 + 7^2). \\
 &= (2! + 1!) \times (7! + 4! \times 3!) = 2^3 \times (1^7 + 7^1 + 4^2) \times 3^4.
 \end{aligned}$$

$$\begin{aligned}
 15840 &:= (1! \times 7! + 5! \times 4!) \times 2! = (1^7 + 7^2 + 5^1) \times (4^4 + 2^5). \\
 15888 &:= 2! \times ((1! + 5!) \times 4! + 7!) = (2^2 + 1^7) \times 5^5 + 4^4 + 7^1.
 \end{aligned}$$

$$\begin{aligned}
 17289 &:= 1! + 4! \times 6! + 2! + 3! = (1^6 + 4^1) \times 6^3 \times 2^4 + 3^2. \\
 &= 1! + 6! \times 4! + 2! + 3! = (1^3 + 6^1 \times (4^4 + 2^6)) \times 3^2.
 \end{aligned}$$

$$\begin{aligned}
 17312 &:= 2! + 4! \times (6! + 1!) + 3! = (2^4 + 4^6 + 6^3) \times (1^2 + 3^1). \\
 17334 &:= 1! \times 4! \times (2! + 6!) + 3! = (1^3 + 4^4 + 2^6) \times 6^1 \times 3^2. \\
 17408 &:= 2! + 4! \times 6! + 3! + 5! = 2^6 + 4^2 \times (6^3 + 3^5 + 5^4). \\
 17436 &:= (2! + 4! \times (1! + 5!)) \times 3! = 2^4 + (4^3 + 1^1) \times (5^2 + 3^5).
 \end{aligned}$$

$$\begin{aligned} \mathbf{17472} &:= (1! \times 2! + 6! + 3!) \times 4! = 1^3 \times 2^2 \times 6^4 + 3^1 \times 4^6. \\ &:= (2! + (1! + 5!) \times 3!) \times 4! = (2^5 \times (1^2 + 5^1) + 3^4) \times 4^3. \end{aligned}$$

$$\begin{aligned} \mathbf{17473} &:= 1! + (2! + 6! + 3!) \times 4! = 1^3 + 2^2 \times 6^4 + 3^1 \times 4^6. \\ \mathbf{17568} &:= 1! \times 3! \times 4! \times (5! + 2!) = (1^2 + 3^5 \times 4^1 + 5^3) \times 2^4. \\ \mathbf{17712} &:= (3! \times (2! + 1!) + 6!) \times 4! = 3^3 \times 2^4 \times (1^6 + 6^2 + 4^1). \\ \mathbf{18048} &:= (3! \times 5! + 2!) \times 4! + 6! = 3^5 + 5^3 + 2^2 \times 4^6 + 6^4. \\ \mathbf{18050} &:= (1! + 4!) \times (2! + 3! \times 5!) = (1^1 + 4^5) \times (2^3 + 3^2) + 5^4. \\ \mathbf{18152} &:= (1! + 4!) \times (3! + 6!) + 2! = (1^6 + 4^1 + 3^2) \times 6^4 + 2^3. \\ \mathbf{18240} &:= ((4! + 1!) \times 3! + 2!) \times 5! = 4^3 \times (1^1 + 3^5 + 2^4 + 5^2). \end{aligned}$$

$$\begin{aligned} \mathbf{18720} &:= (2! + 4!) \times 1! \times 5! \times 3! = 2^4 \times (4^1 + 1^5 + 5^3) \times 3^2. \\ &= 2^5 \times (4^1 \times (1^2 + 5^3) + 3^4). \end{aligned}$$

$$\mathbf{18876} := (1! + 5!) \times (2! + 4!) \times 3! = 1^3 + 5^2 \times (2^1 \times 4^4 + 3^5).$$

$$\begin{aligned} \mathbf{19440} &:= 3! \times (2! + 4! + 1!) \times 5! = 3^4 \times (2^5 + 4^2) \times 1^3 \times 5^1. \\ &= 3^4 \times 2^3 \times (4^1 + 1^5 + 5^2). \end{aligned}$$

$$\begin{aligned} \mathbf{20160} &:= 2! \times (6! \times (3! + 1!) + 7!) = (2^6 + 6^3) \times 3^2 \times (1^7 + 7^1). \\ \mathbf{20190} &:= (1! + 5! + 6!) \times 4! + 3! = 1^4 + 5^3 + 6^5 + 4^6 \times 3^1. \\ \mathbf{20208} &:= (1! \times 2! + 5! + 6!) \times 4! = 1^6 \times 2^5 \times (5^4 + 6^1) + 4^2. \\ \mathbf{20209} &:= 1! + (2! + 5! + 6!) \times 4! = 1^6 + 2^5 \times (5^4 + 6^1) + 4^2. \\ \mathbf{20400} &:= (4! \times (1! + 3!) + 2!) \times 5! = 4^5 + 1^1 + (3^3 + 2^2) \times 5^4. \\ \mathbf{20496} &:= (1! + 3!) \times (2! + 5!) \times 4! = (1^4 + 3^5) \times (2^2 \times 5^1 + 4^3). \end{aligned}$$

$$\begin{aligned} \mathbf{21840} &:= (1! \times 4! + 2!) \times (5! + 6!) = 1^5 \times 4^2 \times (2^6 + 5^1 + 6^4). \\ &:= (3! + 4!) \times 6! + 2! \times 5! = 3^3 + (4^4 + 6^2) \times 2^6 + 5^5. \end{aligned}$$

$$\begin{aligned} \mathbf{21841} &:= 1! + (4! + 2!) \times (5! + 6!) = 1^5 + 4^2 \times (2^6 + 5^1 + 6^4). \\ \mathbf{21866} &:= (1! + 5! + 6!) \times (2! + 4!) = 1^2 + 5^6 + 6^1 \times (2^4 + 4^5). \\ \mathbf{21888} &:= 3! \times (6! + (5! + 2!) \times 4!) = (3^3 + 6^4 + 5^5) \times 2^2 + 4^6. \\ \mathbf{22320} &:= 1! \times 4! \times 3! \times 5! + 7! = 1^7 \times 4^4 + (3^3 + 5^5) \times 7^1. \\ \mathbf{22321} &:= 1! + 4! \times 3! \times 5! + 7! = 1^7 + 4^4 + (3^3 + 5^5) \times 7^1. \end{aligned}$$

$$\begin{aligned} \mathbf{23040} &:= (1! \times 2! + 3!) \times 4! \times 5! = (1^5 + 2^3 + 3^2) \times 4^4 \times 5^1. \\ &:= (2! + 4! \times 1! + 3!) \times 6! = 2^6 \times (4^1 \times 1^3 \times 3^4 + 6^2). \\ &:= ((2! + 4!) \times 5! + 6!) \times 3! = 2^2 \times (4^6 + 5^3 + 6^4 + 3^5). \\ &:= 1! \times 6! \times (2! + 3! + 4!) = (1^6 \times 6^2 + 2^1 \times 3^3) \times 4^4. \\ &:= 1! \times 6! \times (3! + 4! + 2!) = (1^3 \times 6^2 + 3^4 \times 4^1) \times 2^6. \end{aligned}$$

$$\begin{aligned} \mathbf{23041} &:= (2! + 4! + 3!) \times 6! + 1! = 2^6 \times (4^1 \times 3^4 + 6^2) + 1^3. \\ &:= (4! + 2! + 3!) \times 6! + 1! = 4^4 \times (2^1 \times 3^3 + 6^2) + 1^6. \end{aligned}$$

$$\mathbf{23232} := (1! + 5!) \times 4! \times (3! + 2!) = (1^2 + 5^1 \times (4^3 + 3^4)) \times 2^5.$$

$$\begin{aligned} \mathbf{23760} &:= (2! + 3! + 1! + 4!) \times 6! = (2^3 \times (3^4 + 1^6) + 4^1) \times 6^2. \\ &= 2^6 \times 3^3 + (1^1 + 4^2) \times 6^4. \\ &= 2^1 \times (3^6 \times 1^4 \times 4^2 + 6^3). \end{aligned}$$

$$\begin{aligned} \mathbf{25200} &:= (5! + 6!) \times 1! \times 4! + 7! = 5^6 + 6^5 + (1^7 + 4^4) \times 7^1. \\ &:= (2! + 3! + 1!) \times 4! \times 5! = 2^5 \times 3^3 \times (1^4 + 4^1 + 5^2). \\ &:= (1! \times 2! \times 3! + 4!) \times 6! = 1^6 \times 2^3 \times 3^4 \times (4^1 + 6^2). \\ &= 1^3 \times 2^1 \times (3^6 \times 4^2 + 6^4). \end{aligned}$$

$$\begin{aligned} \mathbf{25921} &:= 1! + (2! \times 3! + 4!) \times 6! = 1^3 + 2^1 \times (3^6 \times 4^2 + 6^4). \\ &= 1^6 + 2^3 \times 3^4 \times (4^1 + 6^2). \end{aligned}$$

$$\mathbf{25956} := (2! \times 3! + 4!) \times (1! + 6!) = 2^6 \times 3^4 \times (4^1 + 1^3) + 6^2.$$

$$\begin{aligned} \mathbf{30240} &:= 6! \times ((2! + 1!) \times 3! + 4!) = (6^1 + 2^6) \times 1^4 \times 3^3 \times 4^2. \\ &:= 6! \times (3! \times (2! + 1!) + 4!) = (6^3 + 3^6) \times 2^1 \times 1^4 \times 4^2. \end{aligned}$$

$$\mathbf{30528} := (1! \times 7! + 2! \times 4!) \times 3! = 1^7 + 7^3 \times (2^2 + 4^1 + 3^4).$$

$$\mathbf{34560} := 1! \times 2! \times 3! \times 4! \times 5! = 1^5 \times 2^4 \times 3^3 \times 4^2 \times 5^1.$$

$$\mathbf{34561} := 1! + 2! \times 3! \times 4! \times 5! = 1^5 + 2^4 \times 3^3 \times 4^2 \times 5^1.$$

$$\begin{aligned} \mathbf{34562} &:= (1! + 3! \times 5! \times 4!) \times 2! = (1^5 + 3^2 + 5^3) \times 4^4 + 2^1. \\ &= (1! + 4! \times 5! \times 3!) \times 2! = (1^4 + 4^2 + 5^5) \times (3^1 + 2^3). \end{aligned}$$

$$\mathbf{34566} := 3! + 2! \times 1! \times 4! \times 6! = 3^3 \times (2^2 + 1^6) \times 4^4 + 6^1.$$

$$\begin{aligned} \mathbf{34572} &:= (1! \times 2! + 6! + 7!) \times 3! = (1^6 + 2^7) \times (6^3 + 7^2 + 3^1). \\ &:= 2! \times (4! \times 5! + 1!) \times 3! = (2^1 + 4^4) \times (5^3 \times 1^5 + 3^2). \end{aligned}$$

$$\mathbf{34590} := (1! + 2! \times 6!) \times 4! + 3! = (1^6 + 2^2) \times (6^1 + 4^4 \times 3^3).$$

$$\mathbf{34848} := (1! + 5!) \times 3! \times 4! \times 2! = (1^2 + 5^1 \times 3^3) \times 4^4 + 2^5.$$

$$\mathbf{35616} := (1! + 3!) \times (7! + 2! \times 4!) = (1^2 \times 3^1 + 7^4) \times 2^3 + 4^7.$$

$$\mathbf{36000} := 2! \times 3! \times (1! + 4!) \times 5! = (2^5 + (3^3 + 1^2) \times 4^4) \times 5^1.$$

$$\mathbf{37440} := (2! \times 3! + 1!) \times 4! \times 5! = (2^5 \times 3^2) \times (1^4 + 4^1 + 5^3).$$

$$\begin{aligned}
 38880 &:= (1! \times 6! \times 2! + 7!) \times 3! = 1^6 \times 6^3 \times (2^7 + 7^2 + 3^1). \\
 &:= (1! \times 4! \times 2! + 3!) \times 6! = (1^3 \times 4^2 + 2^6) \times 3^4 \times 6^1. \\
 &\quad = (1^6 \times 4^1 + 2^4) \times 3^2 \times 6^3.
 \end{aligned}$$

$$\begin{aligned}
 38881 &:= 1! + (2! \times 4! + 3!) \times 6! = 1^3 + (2^6 + 4^2) \times 3^4 \times 6^1. \\
 &\quad = 1^6 + (2^4 + 4^1) \times 3^2 \times 6^3. \\
 &:= 1! + 3! \times (7! + 2! \times 6!) = 1^6 + (3^1 + 7^2 + 2^7) \times 6^3.
 \end{aligned}$$

$$\begin{aligned}
 40320 &:= (1! + 3!) \times 2! \times 4! \times 5! = (1^1 + 3^2) \times 2^5 + 4^3 \times 5^4. \\
 &\quad = (1^2 + 3^3) \times (2^5 + 4^4) \times 5^1. \\
 &:= (3! + (1! + 4!) \times 2!) \times 6! = 3^2 \times 1^1 \times 4^6 + 2^4 \times 6^3. \\
 &\quad = 3^2 \times 1^4 \times 4^3 \times (2^6 + 6^1).
 \end{aligned}$$

$$40448 := 1! \times 2! + 3! + 5! + 8! = (1^5 + 2^8 + 3^1 \times 5^3) \times 8^2.$$

$$\begin{aligned}
 40512 &:= (1! + 2!) \times 4! + 5! + 8! = 1^5 \times 2^8 + (4^1 + 5^4) \times 8^2. \\
 &:= (2! \times 1! + 3!) \times (7! + 4!) = (2^1 \times 1^4 + 3^7 + 7^3) \times 4^2. \\
 &\quad = (2^7 \times 1^3 + 3^1 + 7^4) \times 4^2. \\
 &\quad = 2^4 \times (1^1 + 3^7 + 7^3) + 4^2.
 \end{aligned}$$

$$\begin{aligned}
 40513 &:= 1! + (2! + 3!) \times (7! + 4!) = 1^3 + (2^7 + 3^1 + 7^4) \times 4^2. \\
 &\quad = 1^4 + (2^1 + 3^7 + 7^3) \times 4^2.
 \end{aligned}$$

$$\begin{aligned}
 40584 &:= 1! \times 4! + 5! \times 2! + 8! = (1^8 + 4^4 + 5^5) \times (2^2 + 8^1). \\
 40752 &:= 4! \times 3! \times (2! + 1!) + 8! = 4^2 \times (3^3 + 2^8) \times (1^4 + 8^1). \\
 41072 &:= 2! + 3! + 6! + 8! + 4! = 2^8 + 3^3 \times (6^4 + 8^2) + 4^6. \\
 41280 &:= 1! \times 5! \times (3! + 2!) + 8! = (1^5 + 5^3 + 3^1) \times (2^8 + 8^2).
 \end{aligned}$$

$$\begin{aligned}
 42000 &:= (1! + 4!) \times (5! + 6!) \times 2! = 1^6 \times 4^5 \times (5^1 + 6^2) + 2^4. \\
 &:= 5! \times 2! \times (1! + 3!) + 8! = 5^3 \times (2^5 + 1^8 + 3^2) \times 8^1. \\
 &\quad = 5^3 \times (2^8 + (1^5 + 3^2) \times 8^1).
 \end{aligned}$$

$$42486 := 3! + 8! + (1! + 2!) \times 6! = (3^8 + (8^2 + 1^6) \times 2^3) \times 6^1.$$

$$\begin{aligned}
 43200 &:= (1! \times 3! + 4!) \times 2! \times 6! = (1^6 + 3^2) \times (4^1 + 2^4) \times 6^3. \\
 &:= (1! \times 3! + 4!) \times 6! \times 2! = 1^2 \times 3^3 \times (4^4 \times 6^1 + 2^6). \\
 &:= 3! \times (7! + (1! + 2!) \times 6!) = (3^6 + 7^3 \times 1^1 + 2^7) \times 6^2. \\
 &\quad = (3^2 \times (7^1 + 1^6) + 2^7) \times 6^3.
 \end{aligned}$$

$$\begin{aligned} \mathbf{43201} &:= 1! + 2! \times 6! \times (4! + 3!) = 1^2 + (2^6 + 6^1 \times 4^4) \times 3^3. \\ \mathbf{44688} &:= 3! \times 6! + 8! + 2! \times 4! = (3^6 + 6^4 + 8^3 + 2^8) \times 4^2. \end{aligned}$$

$$\begin{aligned} \mathbf{46080} &:= 2! \times (7! + (1! + 4!) \times 6!) = (2^7 \times (7^1 + 1^6) + 4^4) \times 6^2. \\ &:= 1! \times 5! \times 2! \times 4! + 8! = (1^8 + 5^2) \times 2^1 \times 4^4 + 8^5. \\ &= (1^1 + 5^2) \times (2^8 + 4^4) + 8^5. \\ &= (1^8 \times 5^1 + 2^2) \times (4^5 + 8^4). \end{aligned}$$

$$\begin{aligned} \mathbf{46081} &:= 1! + 5! \times 2! \times 4! + 8! = 1^8 + (5^1 + 2^2) \times (4^5 + 8^4). \\ &:= 1! + 6! \times (2! + 3!) + 8! = 1^6 + 6^2 \times (2^8 \times 3^1 + 8^3). \end{aligned}$$

$$\begin{aligned} \mathbf{46800} &:= 6! \times (2! + 1! + 3!) + 8! = 6^6 + (2^3 + 1^8 + 3^2) \times 8^1. \\ &= 6^6 + 2^2 \times (1^8 + 3^3 + 8^1). \end{aligned}$$

$$\begin{aligned} \mathbf{48960} &:= 1! \times 8! + 2! \times 3! \times 6! = (1^2 \times 8^3 + 2^8) \times 3^1 + 6^6. \\ &= 1^8 \times 8^1 \times 2^3 \times (3^6 + 6^2). \end{aligned}$$

$$\begin{aligned} \mathbf{48961} &:= 1! + 8! + 2! \times 3! \times 6! = 1^2 + (8^3 + 2^8) \times 3^1 + 6^6. \\ &= 1^8 + 8^1 \times 2^3 \times (3^6 + 6^2). \end{aligned}$$

$$\mathbf{50407} := 1! + 7! \times 2! + 3! + 8! = 1^2 \times 7^1 \times (2^7 + 3^8 + 8^3).$$

$$\mathbf{50408} := (1! + 7!) \times 2! + 3! + 8! = 1^2 + 7^1 \times (2^7 + 3^8 + 8^3).$$

$$\mathbf{50414} := (7! + 1! + 3!) \times 2! + 8! = 7^1 \times (1^2 + 3^8 + 2^7 + 8^3).$$

$$\begin{aligned} \mathbf{51840} &:= (1! + 2!) \times 5! \times 3! \times 4! = 1^5 \times 2^3 \times 5^1 \times 3^4 \times 4^2. \\ &= (1^5 + 2^2 + 5^1) \times 3^4 \times 4^3. \end{aligned}$$

$$\mathbf{51846} := 3! + 4! \times (2! + 1!) \times 6! = (3^3 \times (4^4 + 2^6) + 1^2) \times 6^1.$$

$$\begin{aligned} \mathbf{56160} &:= ((1! + 2!) \times 4! + 3!) \times 6! = (1^6 + 2^4 \times 4^2 + 3^1) \times 6^3. \\ &= ((2! + 1!) \times 4! + 3!) \times 6! = 2^4 \times (1^6 + 4^3) \times 3^2 \times 6^1. \end{aligned}$$

$$\mathbf{60720} := (1! \times 5! + 3! \times 7!) \times 2! = (1^5 + 5^1) \times (3^7 + 7^3) \times 2^2.$$

$$\begin{aligned} \mathbf{64800} &:= (1! + 2!) \times (4! + 3!) \times 6! = (1^2 \times 2^3) \times 4^1 \times (3^6 + 6^4). \\ &= 1^3 \times 2^1 \times 4^2 \times (3^6 + 6^4). \\ &= 3! \times 7! + 2! \times 4! \times 6! = (3^7 + 7^2) \times 2^3 + 4^4 + 6^6. \end{aligned}$$

$$76320 := 6! \times 2! \times (1! + 4!) + 8! = 6^2 \times (2^6 + (1^8 + 4^4) \times 8^1).$$

$$80640 := (1! + 3!) \times (7! + 6!) \times 2! = (1^7 + 3^3 + 7^1) \times 6^2 \times 2^6.$$

$$80928 := (1! \times 8! + 4! + 5!) \times 2! = (1^8 + 8^1) \times (4^4 + 5^2) \times 2^5.$$

$$83520 := (1! \times 2!) \times 8! + 4! \times 5! = ((1^5 + 2^8) \times 8^2 + 4^4) \times 5^1.$$

$$83521 := 1! + 2! \times 8! + 4! \times 5! = 1^5 + (2^8 + 8^2) \times (4^4 + 5^1).$$

$$88572 := (1! \times 3! + 6!) \times (5! + 2!) = (1^1 + 3^3) \times (6^2 + 5^5) + 2^6.$$

$$89298 := (2! + 5! + 1!) \times (3! + 6!) = (2^6 + 5^5) \times (1^2 + 3^3) + 6^1.$$

$$91442 := (1! + 3! + 5!) \times 6! + 2! = (1^2 + 3^6) \times 5^3 + 6^1 \times 2^5.$$

$$92160 := (1! + 2!) \times 4! \times 6! + 8! = (1^8 \times 2^6 + 4^4) \times 6^2 \times 8^1.$$

$$92880 := (3! + 6! + 4! \times 2!) \times 5! = 3^2 \times (6^4 + 4^5 + 2^6 \times 5^3).$$

$$\begin{aligned} 95040 &:= 3! \times ((2! + 1!) \times 7! + 6!) = 3^3 \times 2^6 \times 1^7 \times (7^2 + 6^1). \\ &\quad = 3^6 \times 2^7 + (1^2 + 7^1) \times 6^3. \end{aligned}$$

$$103682 := 1! \times 3! \times 4! \times 6! + 2! = (1^2 + 3^4 \times 4^3 + 6^6) \times 2^1.$$

$$103683 := 1! + 2! + (4! \times 6!) \times 3! = (1^3 \times 2^6 + 4^2) \times 6^4 + 3^1.$$

$$103688 := (1! + 6! \times 4!) \times 3! + 2! = (1^1 + 6^4 + 4^2 \times 3^6) \times 2^3.$$

$$104544 := (1! + 5!) \times (3! \times 4! + 6!) = (1^6 + 5^3) \times 3^1 \times 4^4 + 6^5.$$

$$105120 := (1! \times 3! \times 4! + 2!) \times 6! = (1^4 + 3^6) \times (4^2 + 2^3) \times 6^1.$$

$$\begin{aligned} 105840 &:= (1! + 2! + 4! \times 3!) \times 6! = (1^1 \times 2^6 + 4^2) \times (3^3 + 6^4). \\ &\quad = (1^4 + 2^3) \times 4^2 \times (3^6 + 6^1). \end{aligned}$$

$$\begin{aligned} 112320 &:= (2! \times 1! + 4!) \times 3! \times 6! = 2^4 \times (1^6 + 4^3) \times 3^1 \times 6^2. \\ &\quad = (2^6 + 1^1) \times (4^2 \times 3^3 + 6^4). \end{aligned}$$

$$\begin{aligned} 116640 &:= (1! + 2! + 4!) \times 3! \times 6! = (1^1 + 2^3) \times (4^2 \times 3^6 + 6^4). \\ &\quad := (1! + 2! + 4!) \times 6! \times 3! = (1^3 \times 2^4 + 4^1 \times 6^2) \times 3^6. \\ &\quad := (2! + 1! + 4!) \times 3! \times 6! = 2^3 \times (1^6 + 4^1) \times 3^4 \times 6^2. \\ &\quad \quad \quad = (2^3 + 1^1) \times (4^2 \times 3^6 + 6^4). \end{aligned}$$

$$\begin{aligned} 121392 &:= (3! \times (1! + 2!) + 7!) \times 4! = 3^1 \times 1^3 \times (2^7 + 7^4) \times 4^2. \\ &\quad := (2! + 1!) \times (8! + 3! \times 4!) = (2^1 \times (1^4 + 8^3) + 3^8) \times 4^2. \end{aligned}$$

$$122040 := (1! + 2!) \times (5! + 8!) + 6! = (1^6 + 2^8 + 5^5 + 8^1) \times 6^2.$$

$$122401 := 1! + 6! \times 2! + 4! \times 7! = 1^4 \times 6^2 \times (2^7 + 4^1) + 7^6.$$

$$122402 := (1! + 6!) \times 2! + 4! \times 7! = 1^4 + 6^2 \times (2^7 + 4^1) + 7^6.$$

$$123840 := 4! \times 5! + (1! + 2!) \times 8! = (4^1 + 5^2 + 1^8) \times (2^5 + 8^4).$$

$$131040 := (1! \times 3! + 5!) \times 6! + 8! = 1^8 + 3^3 \times 5^5 + 6^6 + 8^1.$$

$$\begin{aligned} \mathbf{131072} &:= (2! + 4!) \times (1! + 7!) + 3! = 2^7 \times 4^3 \times 1^4 \times (7^1 + 3^2) \\ &\quad = 2^3 \times 4^4 \times (1^7 + 7^1 \times 3^2). \end{aligned}$$

$$\begin{aligned} \mathbf{131222} &:= (1! + 7! + 3!) \times (2! + 4!) = (1^4 + 7^2) \times 3^1 + 2^3 \times 4^7. \\ \mathbf{135360} &:= (2! + 4!) \times 7! + 3! \times 6! = (2^2 + 4^7) + 7^6 + 3^3 + 6^4. \end{aligned}$$

$$\begin{aligned} \mathbf{138240} &:= (1! \times 3! + 2!) \times 4! \times 6! = (1^6 + 3^2) \times 2^4 \times 4^1 \times 6^3. \\ &\quad := (4! \times (1! + 2!) + 5!) \times 6! = 4^4 \times (1^5 + 2^6 + 5^2) \times 6^1. \end{aligned}$$

$$\mathbf{138528} := (2! \times 3! + 7! + 6!) \times 4! = 2^7 \times (3^6 + 7^3) + 6^4 + 4^2.$$

$$\begin{aligned} \mathbf{141120} &:= 4! \times (3! + 1!) \times (5! + 6!) = 4^4 \times (3^5 + 1^1 + 5^3) + 6^6. \\ &\quad := 4! \times (3! + 1!) \times (6! + 5!) = 4^5 + 3^1 \times (1^4 + 6^6) + 5^3. \end{aligned}$$

$$\begin{aligned} \mathbf{155520} &:= (1! + 3! + 2!) \times 4! \times 6! = (1^6 + 3^2) \times (2^3 + 4^1) \times 6^4. \\ &\quad := (1! + 2! + 3!) \times 4! \times 6! = (1^6 + 2^2) \times 3^4 \times 4^3 \times 6^1. \\ &\quad \quad = (1^2 + 2^1) \times (3^4 \times 4^3 + 6^6). \end{aligned}$$

$$\begin{aligned} \mathbf{161280} &:= (2! + 3!) \times 4! \times (5! + 6!) = (2^4 + 3^5 + 4^6 + 5^3) \times 6^2. \\ \mathbf{172800} &:= ((2! + 1!) \times 6! + 7!) \times 4! = 2^7 \times (1^6 + 6^4 + 7^2 + 4^1). \\ \mathbf{174252} &:= ((1! + 5!) \times 6! + 3!) \times 2! = 1^5 + (5^6 + 6^3) \times (3^2 + 2^1). \\ \mathbf{175692} &:= (1! + 5!) \times (6! + 3!) \times 2! = 1^5 + (5^2 + 6^3) \times 3^6 + 2^1. \\ \mathbf{180048} &:= (1! + 5!) \times (6! + 4!) \times 2! = (1^6 + (5^4 \times 6^1)) \times (4^2 + 2^5). \end{aligned}$$

$$\begin{aligned} \mathbf{181440} &:= (1! \times 2! \times 3! + 4!) \times 7! = (1^7 + 2^2) \times 3^4 \times 4^3 \times 7^1. \\ &\quad := (1! \times 5! + 3!) \times 6! \times 2! = (1^2 + 5^1) \times (3^6 + 6^3) \times 2^5. \end{aligned}$$

$$\mathbf{190086} := 3! + (5! \times 2! + 4!) \times 6! = 3^2 + 5^3 + 2^4 \times (4^6 + 6^5).$$

$$\begin{aligned} \mathbf{207360} &:= 1! \times 4! \times 2! \times 6! \times 3! = (1^2 \times 4^4 + 2^6) \times 6^3 \times 3^1. \\ &\quad := 1! \times 2! \times 4! \times 6! \times 3! = (1^2 \times 2^6 + 4^4) \times 6^3 \times 3^1. \\ &\quad \quad = (1^6 + 2^2) \times 4^4 \times 6^1 \times 3^3. \\ &\quad \quad = 1^3 \times 2^6 \times (4^1 + 6^2) \times 3^4. \end{aligned}$$

$$\begin{aligned} \mathbf{207361} &:= 1! + 2! \times 4! \times 6! \times 3! = 1^2 + (2^6 + 4^4) \times 6^3 \times 3^1. \\ &\quad := 1! + 2! \times 3! \times 4! \times 6! = 1^1 + 2^2 \times (3^4 \times 4^3 + 6^6). \\ &\quad \quad = 1^3 + 2^6 \times 3^4 \times (4^1 + 6^2). \end{aligned}$$

$$207480 := 2! \times 3! \times 6! \times 4! + 5! = 2^4 + 3^6 \times 6^3 + 4^2 \times 5^5.$$

$$208800 := 2! \times (1! + 5! + 4!) \times 6! = (2^6 + 1^1 + 5^2) \times (4^5 + 6^4).$$

$$\begin{aligned} 224640 &:= (2! \times 3! + 1!) \times 4! \times 6! = 2^6 \times 3^2 \times (1^4 + 4^3) \times 6^1. \\ &\quad = 2^2 \times (3^1 + 1^6 + 4^4) \times 6^3. \end{aligned}$$

$$241920 := (1! + 3!) \times 6! \times 2! \times 4! = (1^1 \times 3^6 + 6^3) \times 2^4 \times 4^2.$$

$$247680 := 6! \times (4! + 5!) \times 2! + 8! = 6^6 + 4^5 + 5^4 \times (2^8 + 8^2).$$

$$259206 := 3! + 5! \times (2! + 1!) \times 6! = (3^3 \times 5^2 \times 2^6 + 1^5) \times 6^1.$$

$$263520 := ((1! + 2!) \times 5! + 3!) \times 6! = (1^6 + 2^2 + 5^1 \times 3^5) \times 6^3.$$

$$283680 := 6! \times 2! + (1! + 3!) \times 8! = 6^2 \times (2^8 \times 1^3 + 3^6) \times 8^1.$$

$$307440 := (1! + (3! + 4!) \times 2!) \times 7! = (1^2 + 3^3) \times 4^1 + 2^7 \times 7^4.$$

$$\begin{aligned} 311040 &:= (3! + 2! \times 4!) \times (7! + 6!) = 3^4 \times (2^7 + 4^3 \times 7^2) + 6^6. \\ &\quad := (2! + 1!) \times 4! \times 3! \times 6! = (2^6 \times 1^1 + 4^4) \times 3^3 \times 6^2. \\ &\quad \quad = (2^6 \times 1^3 + 4^2) \times 3^1 \times 6^4. \\ &\quad \quad = 2^6 \times (1^4 + 4^1) \times 3^3 \times 6^2. \end{aligned}$$

$$\begin{aligned} 349920 &:= ((1! + 4!) \times 6! + 8!) \times 3! = (1^8 \times 4^4 + 6^3 + 8^1) \times 3^6. \\ &\quad = (1^8 \times 4^6 + 6^3 + 8^1) \times 3^4. \end{aligned}$$

$$350640 := 3! \times (4! \times 6! + 8!) + 7! = 3^6 + 4^8 + 6^7 + 8^4 + 7^3.$$

$$363008 := 2! \times 1! + 3! + 5! + 9! = 2^9 \times (1^5 + 3^3) \times 5^2 + 9^1.$$

$$363744 := (1! \times 4! + 5!) \times 3! + 9! = 1^9 \times 4^1 \times (5^5 \times 3^3 + 9^4).$$

$$363745 := 1! + (4! + 5!) \times 3! + 9! = 1^9 + 4^1 \times (5^5 \times 3^3 + 9^4).$$

$$364446 := 2! \times 6! + 3! + 5! + 9! = 2^9 \times 6^3 + 3^6 + 5^5 \times 9^2.$$

$$367920 := (1! + 3! + 2!) \times 8! + 7! = ((1^7 + 3^8) \times 2^3 + 8^2) \times 7^1.$$

$$367956 := 2! \times 3! + 4! + 9! + 7! = 2^7 + 3^9 + (4^3 + 9^2) \times 7^4.$$

$$466560 := 1! \times 3! \times 4! \times 6! + 9! = (1^9 \times 3^4 \times 4^3 + 6^6) \times 9^1.$$

$$466561 := 3! \times 4! \times 6! + 9! + 1! = (3^4 \times 4^3 + 6^6) \times 9^1 + 1^9.$$

$$:= 1! + 3! \times 4! \times 6! + 9! = 1^9 + (3^4 \times 4^3 + 6^6) \times 9^1.$$

$$466566 := (1! + 6! \times 4!) \times 3! + 9! = 1^9 \times 6^1 + 4^3 \times (3^6 + 9^4).$$

$$492480 := (1! \times 8! + 6!) \times 3! \times 2! = (1^8 + 8^3) \times (6^1 + 3^2) \times 2^6.$$

$$518403 := 1! + 2! + 5! \times 6! \times 3! = (1^6 + 2^5 \times 5^2 \times 6^3) \times 3^1.$$

$$529968 := (2! + 5!) \times (3! \times 6! + 4!) = 2^5 + (5^6 + 3^4 \times 6^3) \times 4^2.$$

$$540000 := (4! + 3! \times (1! + 5!)) \times 6! = (4^4 + 3^5 + 1^6) \times 5^1 \times 6^3.$$

$$604928 := (1! + 7!) \times 5! + 3! + 2! = (1^5 + 7^1 \times 5^2 \times 3^3) \times 2^7.$$

$$626400 := (1! + 4! + 5!) \times 3! \times 6! = (1^6 + 4^5 + 5^4 \times 3^1) \times 6^3.$$

$$691200 := (1! \times 3! + 2!) \times 5! \times 6! = (1^5 + 3^2) \times 2^6 \times 5^1 \times 6^3.$$

$$691200 := (1! \times 3! + 2!) \times 5! \times 6! = (1^6 + 3^1) \times 2^5 \times 5^2 \times 6^3.$$

$$725760 := (1! + 2! + 3!) \times 8! + 9! = 1^9 \times 2^8 \times (3^3 + 8^1) \times 9^2.$$

$$777600 := 5! \times (2! + 3! + 1!) \times 6! = ((5^2 + 2^3) \times 3^1 + 1^6) \times 6^5.$$

$$846720 := 1! \times 4! \times 7! + 9! \times 2! = (1^9 + 4^1 + 7^2 + 9^4) \times 2^7.$$

$$887040 := 8! \times (1! + 2! \times 3!) + 9! = 8^2 \times ((1^8 + 2^9) \times 3^3 + 9^1).$$

$$967680 := (1! \times 3! + 2!) \times 7! \times 4! = (1^2 + 3^3) \times (2^7 + 7^1) \times 4^4.$$

$$1036800 := 1! \times 2! \times 3! \times 5! \times 6! = 1^5 \times 2^6 \times 3^1 \times 5^2 \times 6^3.$$

$$1036801 := 1! + 2! \times 3! \times 5! \times 6! = 1^5 + 2^6 \times 3^1 \times 5^2 \times 6^3.$$

$$1179360 := (1! + 2!) \times (7! \times 3! + 9!) = (1^3 + 2^9 + 7^1) \times (3^7 + 9^2).$$

$$1330560 := (1! \times 4! + 2! \times 5!) \times 7! = (1^5 + 4^2) \times (2^1 + 5^7) + 7^4.$$

$$1468800 := 4! \times (2! \times 7! \times 3! + 6!) = (4^6 + 2^3 \times (7^4 + 3^7)) \times 6^2.$$

$$1555200 := (1! + 2!) \times 3! \times 5! \times 6! = (1^2 + 2^6 + 3^3 \times 5^1) \times 6^5.$$

$$1942560 := 2! \times ((5! + 8!) \times 4! + 6!) = 2^5 \times (5^2 + 8^4 + 4^6) + 6^8.$$

$$2073606 := 1! \times 5! \times 4! \times 6! + 3! = 1^3 + 5^1 + 4^5 \times (6^4 + 3^6).$$

$$2073726 := 3! + (6! \times 4! + 1!) \times 5! = (3^6 + 6^4) \times 4^5 + 1^1 + 5^3.$$

$$2080080 := (4! \times (2! + 6!) + 3!) \times 5! = (4^3 + 2^4) \times (6^5 + 3^6 \times 5^2).$$

$$2177406 := (1! + 4! \times 6!) \times (3! + 5!) = 1^1 + 4^4 \times (6^5 + 3^6) + 5^3.$$

$$2764800 := (3! + 4! + 2!) \times 6! \times 5! = (3^3 \times 4^5 + 2^6 \times 6^4) \times 5^2.$$

$$3631080 := 5! + (1! + 2! + 7!) \times 6! = (5^1 + 1^6) \times (2^7 + 7^5 \times 6^2).$$

$$3732480 := (1! \times 7! + 3! \times 4!) \times 6! = (1^3 + 7^1) \times (3^6 \times 4^4 + 6^7).$$

$$3870720 := (4! \times 2! \times 1! + 6!) \times 7! = 4^6 \times (2^7 \times (1^4 + 6^1) + 7^2).$$

$$4147200 := 1! \times 2! \times 4! \times 5! \times 6! = 1^6 \times 2^5 \times 4^1 \times 5^2 \times 6^4.$$

$$4147201 := 1! + 2! \times 4! \times 5! \times 6! = 1^6 + 2^5 \times 4^1 \times 5^2 \times 6^4.$$

$$4838406 := (1! + (8! + 9!) \times 2!) \times 3! = 1^9 + (8^1 + 9^3) \times (2^2 + 3^8).$$

$$5443200 := (2! + 3! + 1!) \times 5! \times 7! = (2^7 \times 3^5) \times 1^3 \times 5^2 \times 7^1.$$

$$= 2^7 \times 3^5 \times (1^1 + 5^3 + 7^2).$$

$$7879680 := 4! \times (2! + 3!) \times (8! + 6!) = (4^6 + 2^8 + 3^3 \times 8^2) \times 6^4.$$

$$12441600 := 1! \times 5! \times 3! \times 6! \times 4! = (1^3 + 5^1) \times (3^6 + 6^4) \times 4^5.$$

$$12614400 := (3! \times 4! + 2!) \times 6! \times 5! = (3^3 \times 4^4 + 2^6 \times 6^5) \times 5^2.$$

$$17418240 := (1! + 2!) \times 8! \times (5! + 4!) = (1^1 + 2^8 \times 8^2 + 5^4 \times 4^5).$$

$$17625600 := 4! \times 2! \times (3! \times 6! + 9!) = (4^6 + 2^9 \times 3^2) \times (6^4 + 9^3).$$

$$24883200 := 2! \times 3! \times 4! \times 6! \times 5! = 2^4 \times (3^5 \times 4^3 + 6^6) \times 5^2.$$

$$29393280 := (1! + 2! + 3! + 6!) \times 8! = 1^3 \times 2^6 \times 3^8 \times (6^1 + 8^2).$$

$$32659200 := (2! + 3! + 1!) \times 6! \times 7! = 2^7 \times 3^6 \times (1^2 + 6^1 + 7^3).$$

$$33868800 := (2! + 3!) \times 7! \times (5! + 6!) = (2^6 \times 3^7 + 7^5 + 5^2) \times 6^3.$$

$$34836480 := 1! \times 8! \times (6! + 3! \times 4!) = ((1^4 + 8^1) \times 6^3 + 3^8) \times 4^6.$$

$$35320320 := 3! \times (2! + 4! + 5!) \times 8! = (3^4 \times 2^2 + 4^8 + 5^5) \times 8^3.$$

$$39674880 := ((2! + 3!) \times 5! + 4!) \times 8! = (2^4 + (3^8 + 5^5) \times 4^3) \times 8^2.$$

$$59097600 := 2! \times 6! \times (8! + 3! \times 5!) = (2^8 \times 6^5 + 8^3 \times 3^6) \times 5^2.$$

$$88179840 := (1! + 2!) \times (6! \times 8! + 9!) = 1^8 \times 2^1 \times (6^9 + 8^2 \times 9^6).$$

$$91445760 := 1! \times 9! \times (5! + 3!) \times 2! = (1^2 + 9^3 + 5^1) \times 3^5 \times 2^9.$$

$$97977600 := (4! + 2! \times 5! + 3!) \times 9! = (4^3 + 2^9) \times 5^2 \times (3^5 + 9^4).$$

$$104509440 := (5! + 4! \times (1! + 3!)) \times 9! = 5^1 \times 4^5 \times 1^4 \times (3^9 + 9^3).$$

$$272160000 := (1! \times 3! + 6! + 4!) \times 9! = 1^6 \times 3^3 \times (6^9 + 4^4 \times 9^1).$$

$$272160001 := 1! + (3! + 6! + 4!) \times 9! = 1^6 + 3^3 \times (6^9 + 4^4 \times 9^1).$$

$$609638400 := (5! \times (2! + 3!) + 6!) \times 9! = 5^2 \times 2^9 \times (3^5 + 6^6 + 9^3).$$

$$1045094400 := 2! \times 9! \times (3! \times 5! + 6!) = (2^5 \times 9^2 + 3^9 + 5^3) \times 6^6.$$

$$8360755200 := (2! + 3!) \times 9! \times 4! \times 5! = 2^4 \times (3^9 + 9^3) \times 4^5 \times 5^2.$$

$$20901888000 := 1! \times 6! \times 3! \times 5! \times 8! = (1^8 + 6^1) \times 3^6 \times 5^3 \times 8^5.$$

$$27869184000 := (2! + 3!) \times 6! \times 5! \times 8! = 2^8 \times (3^6 + 6^5) \times 5^2 \times 8^3.$$

$$32659200000 := 5! \times (6! + 4! + 3!) \times 9! = 5^5 \times (6^9 + 4^4 \times (3^6 + 9^3)).$$

2.2 Positive and Negative Signs Expressions

The expression (4) give results for positive and negative signs. The subsections below are numbers with permutable flexible powers of same digits as of bases with positive and negative signs.

2.2.1 Up to Three Terms Expressions

$$1 := -1! + 2! = -1^2 + 2^1.$$

$$3 := 1! + 2! = -1^1 + 2^2.$$

$$4 := -1! \times 2! + 3! = -1^2 + 2^3 - 3^1.$$

$$5 := 1! - 2! + 3! = 1^2 \times 2^3 - 3^1.$$

$$\begin{aligned} 6 := (-1! + 2!) \times 3! &= 1^2 + 2^3 - 3^1 \\ &= -1^3 + 2^2 + 3^1. \\ &= -1^3 - 2^1 + 3^2. \end{aligned}$$

$$\begin{aligned} 7 := -1! + 2! + 3! &= -1^3 \times 2^1 + 3^2. \\ &= 1^3 \times 2^2 + 3^1. \end{aligned}$$

$$8 := 1! \times 2! + 3! = 1^3 - 2^1 + 3^2.$$

$$\begin{aligned} 9 := 1! + 2! + 3! &= (-1^3 + 2^1) \times 3^2. \\ &= (-1^3 + 2^2) \times 3^1. \end{aligned}$$

$$\begin{aligned} 10 := (-1! + 3!) \times 2! &= -1^2 + 3^1 + 2^3. \\ &= -1^3 + 3^2 + 2^1. \end{aligned}$$

$$\begin{aligned} 11 := 2! \times 3! - 1! &= 2^1 + 3^2 \times 1^3. \\ &= 2^2 \times 3^1 - 1^3. \\ &= 2^3 + 3^1 \times 1^2. \end{aligned}$$

$$17 := -1! - 3! + 4! = 1^1 \times 3^4 - 4^3.$$

$$18 := -1! \times 3! + 4! = 1^1 + 3^4 - 4^3.$$

$$21 := -1! - 2! + 4! = 1^2 + 2^4 + 4^1.$$

$$30 := 1! \times 3! + 4! = -1^4 + 3^3 + 4^1.$$

$$48 := 1! \times 4! \times 2! = (-1^2 + 4^1) \times 2^4.$$

$$127 := 1! + 3! + 5! = -1^5 + 3^1 + 5^3.$$

$$138 := -3! + 4! + 5! = -3^5 + 4^4 + 5^3.$$

$$144 := 1! \times 3! \times 4! = -1^1 + 3^4 + 4^3.$$

2.2.2 Four Terms Expressions

$$\begin{aligned} \mathbf{6} &:= 4! - (1! + 2!) \times 3! = -4^1 - 1^2 - 2^4 + 3^3. \\ &\quad = 4^1 + 1^4 - 2^3 + 3^2. \\ &\quad = 4^2 + 1^1 + 2^4 - 3^3. \\ &\quad = 4^2 + 1^4 - 2^3 - 3^1. \end{aligned}$$

$$\begin{aligned} \mathbf{16} &:= -1! \times 3! + 4! - 2! = 1^2 + 3^3 + 4^1 - 2^4. \\ &\quad = 1^2 + 3^4 - 4^3 - 2^1. \\ &\quad = (-1^3 + 3^1) \times 4^2 - 2^4. \\ &\quad = (-1^3 + 3^2) \times 4^1 - 2^4. \end{aligned}$$

$$\begin{aligned} \mathbf{10} &:= 4! - 2! \times (1! + 3!) = -4^1 \times 2^2 - 1^4 + 3^3. \\ &\quad = 4^1 + 2^4 - 1^3 - 3^2. \\ &\quad = 4^2 - 2^3 - 1^4 + 3^1. \\ &\quad = -4^2 - 2^1 + 1^4 + 3^3. \end{aligned}$$

$$\begin{aligned} \mathbf{17} &:= 1! - 2! - 3! + 4! = 1^2 - 2^4 \times 3^1 + 4^3. \\ &\quad = (-1^2 + 2^1) \times 3^4 - 4^3. \end{aligned}$$

$$\begin{aligned} \mathbf{11} &:= (4! - 1!) - 2! \times 3! = 4^1 \times 1^3 + 2^4 - 3^2. \\ &\quad = -4^1 \times 1^4 \times 2^2 + 3^3. \\ &\quad = 4^2 \times 1^4 - 2^3 + 3^1. \\ &\quad = 4^2 \times (1^4 - 2^1) + 3^3. \end{aligned}$$

$$\mathbf{18} := (4! - 1!) \times 3! - 5! = 4^4 \times 1^3 - 3^5 + 5^1.$$

$$\begin{aligned} \mathbf{19} &:= -1! + 2! - 3! + 4! = (1^2 - 2^4) \times 3^1 + 4^3. \\ &\quad = 1^2 \times 2^1 + 3^4 - 4^3. \\ &\quad = -1^4 \times 2^2 + 3^3 - 4^1. \\ &\quad = -1^3 - 2^4 + 3^2 \times 4^1. \end{aligned}$$

$$\begin{aligned} \mathbf{12} &:= -1! \times 2! \times 3! + 4! = -1^1 - 2^2 + 3^4 - 4^3. \\ &\quad = 1^3 + 2^4 - 3^2 + 4^1. \\ &\quad = -1^4 + 2^1 + 3^3 - 4^2. \\ &\quad = 1^4 - 2^3 + 3^1 + 4^2. \\ &:= (2! + 5!) \times 3! - 6! = 2^6 - 5^2 - 3^5 + 6^3. \end{aligned}$$

$$\begin{aligned} \mathbf{20} &:= 1! \times 2! - 3! + 4! = -1^1 + 2^2 + 3^4 - 4^3. \\ &\quad = 1^2 + 2^1 + 3^4 - 4^3. \\ &\quad = 1^4 - 2^2 + 3^3 - 4^1. \\ &\quad = -1^4 + 2^3 + 3^2 + 4^1. \\ &\quad = -1^4 + 2^3 - 3^1 + 4^2. \\ &\quad = -1^3 \times 2^4 + 3^2 \times 4^1. \end{aligned}$$

$$\begin{aligned} \mathbf{13} &:= 1! - 2! \times 3! + 4! = -1^1 \times 2^2 + 3^4 - 4^3. \\ &\quad = -(1^2 + 2^4) \times 3^1 + 4^3. \\ &\quad = 1^4 \times 2^1 + 3^3 - 4^2. \\ &\quad = 1^4 \times 2^3 + 3^2 - 4^1. \end{aligned}$$

$$\begin{aligned} \mathbf{21} &:= 1! + 2! - 3! + 4! = 1^1 \times 2^2 + 3^4 - 4^3. \\ &\quad = 1^3 \times 2^4 + 3^2 - 4^1. \\ &\quad = 1^4 \times 2^3 - 3^1 + 4^2. \\ &\quad = 1^4 \times 2^3 + 3^2 + 4^1. \\ &\quad = -1^4 + 2^1 \times (3^3 - 4^2). \end{aligned}$$

$$\begin{aligned} \mathbf{14} &:= (1! - 3!) \times 2! + 4! = 1^1 + 3^4 - 2^2 - 4^3. \\ &\quad = -1^2 + 3^3 - 2^4 + 4^1. \\ &\quad = -1^2 + 3^4 - 2^1 - 4^3. \\ &\quad = 1^4 + 3^2 + 2^3 - 4^1. \end{aligned}$$

$$\begin{aligned} \mathbf{23} &:= -1! + 3! \times 4! - 5! = 1^5 + 3^4 - 4^3 + 5^1. \\ \mathbf{24} &:= (2! - 3!) \times 4! + 5! = 2^5 + 3^4 - 4^3 - 5^2. \end{aligned}$$

$$\begin{aligned} \mathbf{15} &:= (4! - 1!) - 2! - 3! = -(4^1 - 1^4) \times 2^2 + 3^3. \\ &\quad = (4^1 - 1^4) \times 2^3 - 3^2. \\ &\quad = 4^1 \times 1^2 - 2^4 + 3^3. \\ &\quad = -4^3 \times 1^2 - 2^1 + 3^4. \end{aligned}$$

$$\begin{aligned} \mathbf{27} &:= -1! - 2! + 3! + 4! = 1^1 \times 2^4 + 3^3 - 4^2. \\ &\quad = 1^4 \times 2^2 + 3^3 - 4^1. \\ &\quad = 1^4 \times 2^3 + 3^1 + 4^2. \\ &\quad = -1^4 - 2^3 + 3^2 \times 4^1. \\ &\quad = -1^3 + (2^4 - 3^2) \times 4^1. \end{aligned}$$

$$\begin{aligned}
28 &:= -1! \times 2! + 3! + 4! = 1^1 + 2^4 + 3^3 - 4^2 \\
&= -1^3 + 2^4 - 3^1 + 4^2 \\
&= (1^3 \times 2^4 - 3^2) \times 4^1 \\
&= 1^4 + 2^2 + 3^3 - 4^1 \\
&= 1^4 + 2^3 + 3^1 + 4^2 \\
&= -1^4 \times 2^3 + 3^2 \times 4^1
\end{aligned}$$

$$\begin{aligned}
36 &:= (-1! \times 3! + 4!) \times 2! = (1^2 + 3^4 - 4^3) \times 2^1 \\
&= 1^3 + 3^1 + 4^2 + 2^4 \\
&= 1^4 + 3^3 + 4^1 + 2^2 \\
&= -1^2 - 3^3 + 4^1 \times 2^4 \\
&= (1^4 \times 3^2) \times (-4^1 + 2^3)
\end{aligned}$$

$$\begin{aligned}
29 &:= 1! - 2! + 3! + 4! = 1^3 \times 2^4 - 3^1 + 4^2 \\
&= 1^3 \times 2^4 + 3^2 + 4^1 \\
&= 1^4 - 2^3 + 3^2 \times 4^1
\end{aligned}$$

$$\begin{aligned}
37 &:= 3! \times 2! + 1! + 4! = 3^3 \times 2^1 - 1^4 - 4^2 \\
&= 3^1 \times (2^3 - 1^4) + 4^2 \\
&= -3^2 \times (2^1 + 1^4) + 4^3 \\
&= 3^2 + (2^3 - 1^4) \times 4^1 \\
&= -3^3 + 2^4 \times 1^2 \times 4^1
\end{aligned}$$

$$\begin{aligned}
30 &:= (-1! + 2!) \times 3! + 4! = 1^3 + 2^4 - 3^1 + 4^2 \\
&= 1^3 + 2^4 + 3^2 + 4^1
\end{aligned}$$

$$\begin{aligned}
38 &:= (1! + 3!) \times 2! + 4! = -1^1 - 3^2 - 2^4 + 4^3 \\
&= -1^2 + 3^3 + 2^4 - 4^1 \\
&= 1^4 \times 3^3 \times 2^1 - 4^2
\end{aligned}$$

$$\begin{aligned}
32 &:= 1! \times 3! + 2! + 4! = (1^2 - 3^1) \times 2^4 + 4^3 \\
&= (1^3 - 3^2 + 2^4) \times 4^1 \\
&= 1^3 \times 3^1 \times 2^4 - 4^2 \\
&= (-1^4 + 3^2) \times (2^3 - 4^1) \\
&= (1^4 + 3^1) \times (-2^3 + 4^2)
\end{aligned}$$

$$\begin{aligned}
40 &:= (-1! + 4!) \times 2! - 3! = 1^1 + 4^3 - 2^4 - 3^2 \\
&= 1^2 - 4^1 + 2^4 + 3^3 \\
&= -1^4 + 4^2 - 2^1 + 3^3 \\
&= -1^4 + 4^1 \times 2^3 + 3^2 \\
&= 1^4 \times 4^2 + 2^3 \times 3^1
\end{aligned}$$

$$\begin{aligned}
33 &:= 1! + 2! + 4! + 3! = (-1^2 + 2^4) \times 4^1 - 3^3 \\
&= -(1^3 + 2^1) \times 4^2 + 3^4 \\
&= 1^3 - 2^4 + 4^2 \times 3^1 \\
&= (1^4 + 2^1) \times (-4^2 + 3^3) \\
&= -1^2 + 2^1 \times (-4^3 + 3^4)
\end{aligned}$$

$$\begin{aligned}
41 &:= -1! + 2! \times 4! - 3! = (1^2 + 2^4) \times 4^1 - 3^3 \\
&= -1^4 \times 2^1 + 4^2 + 3^3 \\
&= 1^4 \times 2^3 \times 4^1 + 3^2 \\
&= 1^4 - 2^3 + 4^2 \times 3^1
\end{aligned}$$

$$\begin{aligned}
34 &:= (-1! - 3! + 4!) \times 2! = (1^2 \times 3^4 - 4^3) \times 2^1 \\
&= -1^3 + 3^1 + 4^2 + 2^4 \\
&= -1^4 + 3^3 + 4^1 + 2^2
\end{aligned}$$

$$\begin{aligned}
42 &:= 1! \times 2! \times 4! - 3! = 1^4 - 2^1 + 4^2 + 3^3 \\
&= -1^4 + 2^2 \times 4^1 + 3^3 \\
&= 1^4 + 2^3 \times 4^1 + 3^2
\end{aligned}$$

$$\begin{aligned}
35 &:= -1! + 4! + 3! \times 2! = (1^3 + 4^2) \times 3^1 - 2^4 \\
&= (-1^4 + 4^1) \times 3^2 + 2^3 \\
&= 1^4 \times 4^1 + 3^3 + 2^2 \\
&= (1^3 + 4^1) \times (-3^2 + 2^4) \\
&= 1^2 - (4^3 - 3^4) \times 2^1
\end{aligned}$$

$$\begin{aligned}
43 &:= 1! + 2! \times 4! - 3! = (-1^4 + 2^1) \times 4^2 + 3^3 \\
&= 1^4 \times 2^2 \times 4^1 + 3^3 \\
&= -1^4 + 2^3 + 4^1 \times 3^2
\end{aligned}$$

$$\begin{aligned} 44 &:= (1! + 4!) \times 2! - 3! = -1^2 + 4^3 - 2^4 - 3^1. \\ &= -1^4 + 4^2 + 2^1 + 3^3. \\ &= 1^2 \times 4^1 \times (-2^4 + 3^3). \\ &= 1^4 + 4^1 \times 2^2 + 3^3. \end{aligned}$$

$$\begin{aligned} 48 &:= -(1! + 2!) \times 4! + 5! = -1^4 \times 2^5 + 4^2 \times 5^1. \\ &:= (1! + 3!) \times 4! - 5! = -1^5 \times 3^4 + 4^1 + 5^3. \end{aligned}$$

$$\begin{aligned} 52 &:= (4! - 1!) \times 2! + 3! = 4^3 - 1^4 - 2^1 - 3^2. \\ &= 4^3 + 1^2 - 2^4 + 3^1. \\ &= 4^3 \times 1^4 - 2^2 \times 3^1. \end{aligned}$$

$$\begin{aligned} 53 &:= 2! \times 4! - 1! + 3! = (-2^1 + 4^3) \times 1^4 - 3^2. \\ &= 2^4 \times (4^1 + 1^2) - 3^3. \\ &= 2^3 + (4^1 + 1^4) \times 3^2. \\ &= 2^3 + (4^2 - 1^4) \times 3^1. \end{aligned}$$

$$\begin{aligned} 54 &:= 1! \times 4! \times 2! + 3! = 1^4 + 4^3 - 2^1 - 3^2. \\ &= -1^3 + 4^1 \times 2^4 - 3^2. \end{aligned}$$

$$\begin{aligned} 55 &:= 1! + 4! \times 2! + 3! = (1^1 + 4^2) \times 2^3 - 3^4. \\ &= (1^3 \times 4^1) \times 2^4 - 3^2. \\ &= (1^2 + 4^1) \times (-2^4 + 3^3). \end{aligned}$$

$$\begin{aligned} 56 &:= (1! + 4!) \times 2! + 3! = -1^1 + 4^3 - 2^4 + 3^2. \\ &= -1^1 - 4^2 - 2^3 + 3^4. \\ &= -1^4 + 4^3 + 2^1 - 3^2. \\ &= -1^4 + 4^3 - 2^2 - 3^1. \\ &= 1^3 + 4^1 \times 2^4 - 3^2. \end{aligned}$$

$$\begin{aligned} 58 &:= (3! - 1! + 4!) \times 2! = -3^1 + 1^4 + 4^3 - 2^2. \\ &= -3^2 + 1^4 + 4^3 + 2^1. \\ &= 3^2 + 1^1 + 4^3 - 2^4. \\ &= 3^3 - 1^1 + 4^2 + 2^4. \\ &= 3^4 + 1^1 - 4^2 - 2^3. \\ &= 3^3 - 1^4 + 4^2 \times 2^1. \end{aligned}$$

$$\begin{aligned} 59 &:= (3! + 4!) \times 2! - 1! = 3^3 + 4^2 + 2^4 \times 1^1. \\ &= 3^3 + 4^2 \times 2^1 \times 1^4. \\ &= -3^2 + 4^1 \times (2^4 + 1^3). \end{aligned}$$

$$\begin{aligned} 60 &:= 2! \times 1! \times (3! + 4!) = 2^3 \times (-1^4 + 3^2) - 4^1. \\ &:= -2! \times (3! + 4!) + 5! = 2^5 - 3^4 - 4^2 + 5^3. \end{aligned}$$

$$\begin{aligned} 61 &:= 1! + 2! \times (3! + 4!) = (-1^3 + 2^4) \times 3^1 + 4^2. \\ &:= 1! + 2! \times (4! + 3!) = -(1^3 + 2^2) \times 4^1 + 3^4. \end{aligned}$$

$$\begin{aligned} 62 &:= (1! + 3! + 4!) \times 2! = -1^3 + 3^4 - 4^2 - 2^1. \\ &= -1^4 + 3^1 + 4^3 - 2^2. \end{aligned}$$

$$\begin{aligned} 66 &:= (1! + 2!) \times 4! - 3! = -1^3 + 2^1 - 4^2 + 3^4. \\ &= 1^4 + 2^2 + 4^3 - 3^1. \\ &= 1^3 - 2^2 \times 4^1 + 3^4. \end{aligned}$$

$$71 := -1! - 4! \times 2! + 5! = (-1^4 + 4^1) \times 2^5 - 5^2.$$

$$\begin{aligned} 72 &:= (-1! + 3! - 2!) \times 4! = 1^1 - 3^2 + 2^4 + 4^3. \\ &= -1^1 + 3^4 + 2^3 - 4^2. \\ &= -1^3 + 3^4 - 2^2 - 4^1. \\ &= 1^4 + 3^1 + 2^2 + 4^3. \\ &= 1^4 + 3^2 - 2^1 + 4^3. \\ &= (1^4 + 3^2 + 2^3) \times 4^1. \\ &= (1^4 + 3^3) \times 2^1 + 4^2. \\ &= -1^3 + 3^2 + 2^4 \times 4^1. \\ &= (1^4 \times 3^1) \times (2^3 + 4^2). \\ &:= 1! \times 5! - 4! \times 2! = (1^4 + 5^2) \times 4^1 - 2^5. \end{aligned}$$

$$73 := 5! + 1! - 4! \times 2! = 5^2 - (1^5 - 4^1) \times 2^4.$$

$$\begin{aligned} 78 &:= (1! + 2!) \times 4! + 3! = 1^2 - 2^3 + 4^1 + 3^4. \\ &= 1^2 + 2^4 + 4^3 - 3^1. \end{aligned}$$

$$88 := -2! - 3! - 4! + 5! = -2^5 + 3^4 + 4^3 - 5^2.$$

$$\begin{aligned} 90 &:= (1! + 2!) \times (4! + 3!) = 1^1 - 2^3 + 4^2 + 3^4. \\ &= -1^2 + 2^4 \times 4^1 + 3^3. \\ &:= 5! \times 1! - 3! - 4! = 5^1 \times (1^5 + 3^4 - 4^3). \end{aligned}$$

$$\begin{aligned}
 92 &:= (1! - 4!) \times (2! - 3!) = -1^2 + 4^1 + 2^3 + 3^4 \\
 &\quad = 1^2 + 4^1 \times 2^4 + 3^3 \\
 &\quad = 1^4 \times 4^1 \times (-2^2 + 3^3) \\
 &:= 2! - 3! - 4! + 5! \quad = 2^5 - 3^4 + 4^2 + 5^3.
 \end{aligned}$$

$$\begin{aligned}
 93 &:= 5! - 4! - 1! - 2! = 5^2 \times (4^1 + 1^4) - 2^5 \\
 &\quad = 5^2 + 4^1 \times (1^5 + 2^4).
 \end{aligned}$$

$$\begin{aligned}
 95 &:= 1! - 4! - 2! + 5! \quad = -1^2 + 4^4 - 2^5 \times 5^1 \\
 &\quad = -1^5 + 4^2 + 2^4 \times 5^1 \\
 &:= -1! + (3! - 2!) \times 4! = 1^3 \times 3^4 - 2^1 + 4^2 \\
 &\quad = -1^3 + 3^1 \times (2^4 + 4^2).
 \end{aligned}$$

$$\begin{aligned}
 96 &:= (1! \times 3! - 2!) \times 4! = (1^1 + 3^2) \times 2^4 - 4^3 \\
 &\quad = (-1^2 + 3^1) \times 2^4 + 4^3 \\
 &\quad = (-1^2 + 3^4) \times 2^1 - 4^3 \\
 &\quad = (-1^3 + 3^2 + 2^4) \times 4^1 \\
 &\quad = 1^3 + 3^4 - 2^1 + 4^2.
 \end{aligned}$$

$$\begin{aligned}
 96 &:= (1! \times 3! - 2!) \times 4! = (1^4 + 3^3 - 2^2) \times 4^1 \\
 &\quad = -1^3 + 3^4 + 2^2 \times 4^1 \\
 &\quad = 1^3 \times 3^1 \times (2^4 + 4^2) \\
 &\quad = (1^4 + 3^1) \times (2^3 + 4^2) \\
 &\quad = (-1^4 + 3^2) \times (2^3 + 4^1).
 \end{aligned}$$

$$\begin{aligned}
 96 &:= (4! - 5!) \times (1! - 2!) = 4^2 \times 5^1 \times 1^5 + 2^4 \\
 &\quad = 4^2 \times (5^1 - 1^4) + 2^5 \\
 &\quad = 4^4 - 5^1 \times 1^2 \times 2^5 \\
 &:= 2! \times 5! - 3! \times 4! \quad = 2^3 \times (5^2 + 3^5 - 4^4).
 \end{aligned}$$

$$\begin{aligned}
 97 &:= 1! - (2! - 3!) \times 4! \quad = (-1^3 + 2^1) \times 3^4 + 4^2 \\
 &\quad = (1^4 + 2^1) \times 3^3 + 4^2 \\
 &\quad = -1^2 + 2^1 \times 3^4 - 4^3 \\
 &:= -(4! + 1!) + 2! + 5! = -4^2 \times (1^1 + 2^5) + 5^4 \\
 &\quad = 4^2 + 1^5 + 2^4 \times 5^1 \\
 &\quad = 4^4 + 1^2 - 2^5 \times 5^1.
 \end{aligned}$$

$$99 := 1! + 2! - 4! + 5! = (-1^4 + 2^5) \times 4^1 - 5^2.$$

$$\begin{aligned}
 100 &:= (-2! + 3!) \times (1! + 4!) = 2^1 + 3^4 + 1^3 + 4^2 \\
 &\quad = (2^4 + 3^2) \times 1^3 \times 4^1 \\
 &\quad = 2^1 \times (3^4 + 1^2) - 4^3 \\
 &\quad = 2^2 \times (3^3 - 1^4) - 4^1.
 \end{aligned}$$

$$\begin{aligned}
 102 &:= 5! - (1! + 2!) \times 3! = (5^2 + 1^5 + 2^3) \times 3^1 \\
 &\quad = 5^3 \times 1^1 - 2^5 + 3^2 \\
 &\quad = (5^1 + 1^5) \times (2^3 + 3^2) \\
 &\quad = -5^1 - 1^5 + 2^2 \times 3^3 \\
 &\quad = 5^2 \times (1^5 + 2^1) + 3^3.
 \end{aligned}$$

$$102 := 1! \times 5! + 3! - 4! = (1^5 + 5^1) \times (3^4 - 4^3).$$

$$\begin{aligned}
 106 &:= 5! - (1! + 3!) \times 2! = (5^2 + 1^5 + 3^3) \times 2^1 \\
 &\quad = 5^3 - 1^5 - 3^2 \times 2^1 \\
 &:= 5! - (3! + 1!) \times 2! = 5^2 \times 3^1 - 1^3 + 2^5.
 \end{aligned}$$

$$\begin{aligned}
 107 &:= 5! - 1! - 3! \times 2! = (5^2 \times 1^3) \times 3^1 + 2^5 \\
 &\quad = 5^3 \times 1^5 - 3^2 \times 2^1 \\
 &\quad = -5^1 + (1^5 + 3^3) \times 2^2.
 \end{aligned}$$

$$\begin{aligned}
 108 &:= 5! \times 1! - 3! \times 2! = 5^1 \times (1^2 + 3^3) - 2^5 \\
 &\quad = 5^2 \times (1^5 + 3^1) + 2^3 \\
 &\quad = 5^3 + 1^5 - 3^2 \times 2^1 \\
 &:= 5! \times 1! - 2! \times 3! = (5^1 - 1^5 + 2^3) \times 3^2.
 \end{aligned}$$

$$\begin{aligned}
 109 &:= 1! - 3! \times 2! + 5! = (1^5 - 3^2) \times 2^1 + 5^3 \\
 &\quad = (-1^5 + 3^3) \times 2^2 + 5^1 \\
 &\quad = -(1^5 + 3^1) \times 2^2 + 5^3.
 \end{aligned}$$

$$\begin{aligned}
 110 &:= 2! \times (1! - 3!) + 5! \quad = -(2^2 + 1^5) \times 3^1 + 5^3 \\
 &\quad = (-2^2 - 1^5 + 3^3) \times 5^1 \\
 &\quad = (2^5 - 1^3 - 3^2) \times 5^1 \\
 &:= (2! - 4!) \times (1! - 3!) = 2^1 \times (4^3 \times 1^4 - 3^2).
 \end{aligned}$$

$$111 := 5! - 3! - 2! - 1! = (5^1 + 3^2) \times 2^3 - 1^5.$$

$$\begin{aligned}
 112 &:= 5! \times 1! - 3! - 2! = (5^1 - 1^5) \times 3^3 + 2^2 \\
 &\quad = (5^1 \times 1^5 + 3^2) \times 2^3 \\
 &\quad = 5^3 - 1^5 - 3^1 \times 2^2.
 \end{aligned}$$

$$\begin{aligned}
113 &:= 1! - 2! - 3! + 5! = -1^1 - 2^2 + 3^5 - 5^3. \\
&= -1^5 \times 2^2 \times 3^1 + 5^3. \\
&= (1^5 \times 2^2) \times 3^3 + 5^1. \\
&= -1^5 - 2^1 - 3^2 + 5^3. \\
&= 1^5 + 2^3 \times (3^2 + 5^1).
\end{aligned}$$

$$\begin{aligned}
114 &:= (1! - 2!) \times 3! + 5! = -1^1 \times 2^2 + 3^5 - 5^3. \\
&= -1^5 \times 2^1 - 3^2 + 5^3. \\
&= 1^5 - 2^2 \times 3^1 + 5^3. \\
&= 1^5 + 2^2 \times 3^3 + 5^1. \\
&= -1^3 + (2^5 - 3^2) \times 5^1.
\end{aligned}$$

$$\begin{aligned}
115 &:= 2! - 1! - 3! + 5! = -2^1 + 1^5 - 3^2 + 5^3. \\
&= -2^1 - 1^2 + 3^5 - 5^3. \\
&= -2^2 + 1^1 + 3^5 - 5^3. \\
&= (-2^2 \times 1^5 + 3^3) \times 5^1. \\
&= (2^5 \times 1^3 - 3^2) \times 5^1.
\end{aligned}$$

$$\begin{aligned}
116 &:= 1! \times 2! - 3! + 5! = -1^2 \times 2^1 + 3^5 - 5^3. \\
&= (1^5 - 2^1) \times 3^2 + 5^3. \\
&= (1^5 - 2^2) \times 3^1 + 5^3. \\
&= 1^3 + (2^5 - 3^2) \times 5^1. \\
&= 1^5 - (2^2 - 3^3) \times 5^1.
\end{aligned}$$

$$\begin{aligned}
117 &:= 1! - 3! + 2! + 5! = 1^2 + 3^5 - 2^1 - 5^3. \\
&= -1^5 - 3^1 - 2^2 + 5^3. \\
&= -1^5 - 3^2 + 2^1 + 5^3. \\
&= (1^5 + 3^3) \times 2^2 + 5^1. \\
&= 1^5 \times 3^2 \times (2^3 + 5^1).
\end{aligned}$$

$$118 := (-1! + 3!) \times 4! - 2! = -1^4 - 3^2 + 4^3 \times 2^1.$$

$$\begin{aligned}
120 &:= (1! + 3! - 2!) \times 4! = (-1^4 + 3^3 + 2^2) \times 4^1. \\
&= (1^3 + 3^2) \times (2^4 - 4^1). \\
&= (1^4 - 3^1) \times (2^2 - 4^3). \\
&= 1^4 - 3^2 + 2^1 \times 4^3. \\
&= (1^4 + 3^2) \times (2^3 + 4^1).
\end{aligned}$$

$$\begin{aligned}
123 &:= 3! - 1! + 5! - 2! = 3^1 - 1^5 + 5^3 - 2^2. \\
&= 3^5 + 1^1 - 5^3 + 2^2.
\end{aligned}$$

$$\begin{aligned}
124 &:= -1! \times 2! + 3! + 5! = (1^3 + 2^5) \times 3^1 + 5^2. \\
&= -1^5 \times 2^2 + 3^1 + 5^3. \\
&= (1^3 - 2^5) \times (-3^2 + 5^1). \\
&= -1^1 + (2^5 - 3^3) \times 5^2. \\
&= -1^5 + (2^3 - 3^1) \times 5^2.
\end{aligned}$$

$$\begin{aligned}
125 &:= 1! - 2! + 3! + 5! = (1^1 \times 2^5 - 3^3) \times 5^2. \\
&= (1^5 \times 2^2 - 3^1) \times 5^3. \\
&= (1^5 \times 2^3 - 3^1) \times 5^2.
\end{aligned}$$

$$\begin{aligned}
126 &:= (-1! + 2!) \times 3! + 5! = 1^5 \times 2^2 - 3^1 + 5^3. \\
&= (1^5 + 2^3) \times (3^2 + 5^1). \\
&= 1^1 + (2^5 - 3^3) \times 5^2. \\
&= 1^5 + (2^3 - 3^1) \times 5^2.
\end{aligned}$$

$$\begin{aligned}
127 &:= (-1! + 2!) + 3! + 5! = 1^5 + 2^2 - 3^1 + 5^3. \\
&= -1^3 + 2^5 \times (3^2 - 5^1). \\
&= -1^5 + 2^2 \times (3^3 + 5^1).
\end{aligned}$$

$$\begin{aligned}
128 &:= 1! \times 2! + 5! + 3! = (-1^2 + 2^5) \times 5^1 - 3^3. \\
&= 1^3 \times 2^5 \times (-5^1 + 3^2).
\end{aligned}$$

$$129 := 1! + 2! + 3! + 5! = 1^3 + 2^5 \times (3^2 - 5^1).$$

$$\begin{aligned}
130 &:= 2! \times (3! - 1!) + 5! = (2^3 - 3^1) \times (1^5 + 5^2). \\
&= (2^5 - 3^3) \times (1^1 + 5^2). \\
&= -2^5 + 3^3 \times (1^2 + 5^1). \\
&:= (3! - 1!) \times 2! + 5! = 3^3 \times (1^5 + 2^2) - 5^1.
\end{aligned}$$

$$\begin{aligned}
131 &:= 5! + 2! \times 3! - 1! = 5^3 - 2^1 + 3^2 - 1^5. \\
&= 5^3 + 2^2 + 3^1 - 1^5. \\
&= -5^3 + 2^5 \times (3^2 - 1^1). \\
&:= 5! + 3! \times 2! - 1! = 5^1 \times 3^3 - 2^2 \times 1^5. \\
&= 5^3 + 3^1 + 2^2 - 1^5. \\
&= 5^3 + 3^2 - 2^1 - 1^5.
\end{aligned}$$

$$\begin{aligned}
132 &:= 5! + 2! \times 1! \times 3! = 5^1 \times 2^5 - 1^2 - 3^3 \\
&\quad = (5^3 - 2^1) \times 1^5 + 3^2 \\
&\quad = 5^3 \times (2^1 + 1^2) - 3^5 \\
&\quad = 5^3 \times (2^2 - 1^1) - 3^5 \\
&:= 1! \times 3! \times (4! - 2!) = (1^3 + 3^4 - 4^2) \times 2^1 \\
&\quad = (-1^4 + 3^1) \times 4^3 + 2^2 \\
&\quad = 1^4 + 3^1 + 4^2 \times 2^3.
\end{aligned}$$

$$\begin{aligned}
133 &:= 1! + 3! \times 2! + 5! = 1^5 + 3^2 - 2^1 + 5^3 \\
&\quad = -1^2 \times 3^3 + 2^5 \times 5^1 \\
&:= 3! \times (4! - 2!) + 1! = (3^1 + 4^2) \times (2^3 - 1^4).
\end{aligned}$$

$$\begin{aligned}
134 &:= 2! \times (1! + 3!) + 5! = (2^1 - 1^5) \times 3^2 + 5^3 \\
&\quad = (2^2 - 1^5) \times 3^1 + 5^3 \\
&\quad = 2^2 - (1^5 - 3^3) \times 5^1.
\end{aligned}$$

$$\begin{aligned}
136 &:= 3! \times (-1! + 4!) - 2! = (3^1 - 1^4) \times (4^3 + 2^2) \\
&\quad = 3^2 - 1^4 + 4^3 \times 2^1.
\end{aligned}$$

$$137 := 5! + 4! - 3! - 1! = 5^3 + 4^4 - 3^5 - 1^1.$$

$$\begin{aligned}
138 &:= 3! \times (2! + 1!) + 5! = (-3^2 + 2^5) \times (1^3 + 5^1) \\
&\quad = (3^3 - 2^2) \times (1^5 + 5^1) \\
&\quad = -3^3 + (2^5 + 1^2) \times 5^1 \\
&:= (1! - 2! + 4!) \times 3! = 1^4 + 2^1 \times 4^3 + 3^2 \\
&:= 1! \times 4! - 3! + 5! = 1^1 \times 4^4 - 3^5 + 5^3.
\end{aligned}$$

$$\begin{aligned}
139 &:= 1! - 3! + 4! + 5! = 1^1 - 3^5 + 4^4 + 5^3 \\
&\quad = -1^5 + 3^4 + 4^3 - 5^1.
\end{aligned}$$

$$\begin{aligned}
140 &:= 2! + 3! \times (4! - 1!) = -2^2 + 3^4 + 4^3 - 1^1 \\
&\quad = (2^4 \times 3^2 - 4^1) \times 1^3 \\
&:= 2! + 4! - 3! + 5! = -2^5 \times 4^2 + 3^3 + 5^4.
\end{aligned}$$

$$\begin{aligned}
141 &:= 3! \times 4! - 1! - 2! = (3^4 + 4^3) \times 1^1 - 2^2 \\
&\quad = 3^1 \times (4^3 - 1^2 - 2^4) \\
&\quad = -3^1 + 4^2 \times (1^4 + 2^3) \\
&:= 4! - 1! + 5! - 2! = (4^1 + 1^5) \times 5^2 + 2^4.
\end{aligned}$$

$$\begin{aligned}
142 &:= 1! \times 3! \times 4! - 2! = 1^1 + 3^4 + 4^3 - 2^2 \\
&\quad = -1^2 + 3^4 + 4^3 - 2^1.
\end{aligned}$$

$$\begin{aligned}
143 &:= 1! + 3! \times 4! - 2! = 1^2 \times 3^4 + 4^3 - 2^1 \\
&\quad = -1^2 + 3^1 \times (4^3 - 2^4) \\
&:= 1! - 2! + 5! + 4! = -1^4 + 2^5 \times 5^1 - 4^2.
\end{aligned}$$

$$\begin{aligned}
144 &:= (2! - 1!) \times 3! \times 4! = -2^1 + 1^2 + 3^4 + 4^3 \\
&\quad = 2^1 \times (-1^3 + 3^4) - 4^2 \\
&\quad = -2^2 \times (1^1 + 3^3) + 4^4 \\
&\quad = 2^1 \times (-1^4 + 3^2 + 4^3) \\
&\quad = 2^3 \times (-1^4 + 3^1 + 4^2) \\
&\quad = 2^4 - (1^2 - 3^1) \times 4^3 \\
&:= (2! - 1!) \times 5! + 4! = 2^5 \times 1^4 \times 5^1 - 4^2.
\end{aligned}$$

$$\begin{aligned}
145 &:= 4! - 1! + 2! + 5! = -(4^2 - 1^1) \times 2^5 + 5^4 \\
&\quad = -4^2 + 1^4 + 2^5 \times 5^1 \\
&:= 4! \times 3! + 2! - 1! = (4^3 + 3^2) \times 2^1 - 1^4 \\
&\quad = -4^2 + 3^4 \times 2^1 - 1^3 \\
&\quad = (4^3 + 3^4) \times (2^1 - 1^2).
\end{aligned}$$

$$\begin{aligned}
146 &:= 1! \times 4! \times 3! + 2! = -1^2 + 4^3 + 3^4 + 2^1 \\
&\quad = -1^3 \times 4^2 + 3^4 \times 2^1.
\end{aligned}$$

$$\begin{aligned}
147 &:= 4! \times 3! + 2! + 1! = 4^1 + 3^2 \times 2^4 - 1^3 \\
&\quad = -4^2 + 3^4 \times 2^1 + 1^3 \\
&\quad = 4^4 - 3^3 \times 2^2 - 1^1 \\
&:= 3! \times 4! + 2! + 1! = 3^1 \times (4^3 - 2^4 + 1^2).
\end{aligned}$$

$$\begin{aligned}
148 &:= (4! + 1!) \times 3! - 2! = 4^3 - 1^1 + 3^4 + 2^2 \\
&\quad = 4^3 + 1^2 + 3^4 + 2^1 \\
&\quad = (4^3 + 1^4 + 3^2) \times 2^1 \\
&\quad = 4^1 \times 1^3 + 3^2 \times 2^4 \\
&\quad = 4^4 \times 1^1 - 3^3 \times 2^2 \\
&\quad = -4^2 + (1^3 + 3^4) \times 2^1.
\end{aligned}$$

$$\begin{aligned}
149 &:= 3! - 1! + 4! + 5! = 3^4 - 1^5 + 4^3 + 5^1 \\
150 &:= (2! - 1! + 4!) \times 3! = 2^2 + 1^1 + 4^3 + 3^4.
\end{aligned}$$

$$\begin{aligned} 152 &:= 2! + 3! + 4! + 5! = 2^5 + 3^4 + 4^3 - 5^2. \\ &:= 2! + 3! \times (1! + 4!) = 2^2 \times (-3^3 + 1^1) + 4^4. \end{aligned}$$

$$155 := -1! + (2! + 4!) \times 3! = (1^4 + 2^2) \times (4^1 + 3^3).$$

$$156 := 1! \times 3! \times (2! + 4!) = (1^3 + 3^2) \times 2^4 - 4^1.$$

$$168 := (-1! + 2! + 3!) \times 4! = (-1^2 + 2^4 + 3^3) \times 4^1.$$

$$184 := (-1! + 4!) \times (2! + 3!) = 1^1 \times 4^4 - 2^3 \times 3^2.$$

$$191 := -1! + 4! \times (3! + 2!) = (1^4 + 4^3) \times 3^1 - 2^2.$$

$$\begin{aligned} 192 &:= 4! \times (3! \times 1! + 2!) = (4^1 + 3^2 - 1^3) \times 2^4. \\ &= (4^2 - 3^1 - 1^3) \times 2^4. \\ &= (-4^2 + 3^3 + 1^1) \times 2^4. \\ &= (4^2 + 3^4 - 1^3) \times 2^1. \\ &= 4^3 + (3^2 - 1^1) \times 2^4. \\ &= 4^4 - (3^2 - 1^1) \times 2^3. \end{aligned}$$

$$\begin{aligned} 192 &:= 2! \times (-4! + 5!) \times 1! = (2^4 + 4^2) \times (5^1 + 1^5). \\ &= (2^5 + 4^2) \times (5^1 - 1^4). \end{aligned}$$

$$\begin{aligned} 193 &:= (2! + 3!) \times 4! + 1! = 2^1 \times (3^4 + 4^2) - 1^3. \\ &= 2^2 + 3^1 \times (4^3 - 1^4). \\ &:= 4! \times (3! + 2!) + 1! = 4^4 - 3^2 \times (2^3 - 1^1). \end{aligned}$$

$$200 := (4! + 1!) \times (3! + 2!) = 4^4 - (1^2 + 3^3) \times 2^1.$$

$$\begin{aligned} 216 &:= (2! + 3! + 1!) \times 4! = 2^3 \times 3^2 \times (-1^4 + 4^1). \\ &:= 5! + (3! - 2!) \times 4! = (-5^3 + 3^5) \times 2^2 - 4^4. \end{aligned}$$

$$218 := (1! + 5!) \times 2! - 4! = -1^2 - 5^1 - 2^5 + 4^4.$$

$$\begin{aligned} 222 &:= 2! \times 5! - 4! + 3! = -2^5 + 5^2 + 4^4 - 3^3. \\ &= 2^5 + 5^3 - 4^2 + 3^4. \end{aligned}$$

$$226 := 2! \times (5! - 1! - 3!) = (2^3 - 5^2) \times 1^1 + 3^5.$$

$$227 := 2! \times (5! - 3!) - 1! = (2^3 - 5^2) + 3^5 + 1^1.$$

$$\begin{aligned} 228 &:= 1! \times 2! \times (5! - 3!) = (1^3 - 2^2) \times 5^1 + 3^5. \\ &= (1^5 + 2^3) \times 5^2 + 3^1. \end{aligned}$$

$$\begin{aligned} 229 &:= 1! - 2! \times (3! - 5!) = -1^2 - 2^3 + 3^5 - 5^1. \\ &:= 2! \times (-3^3 + 1^1) + 4^4. \end{aligned}$$

$$\begin{aligned} 230 &:= (1! - 3! + 5!) \times 2! = 1^2 \times 3^5 - 5^1 - 2^3. \\ &= (-1^5 - 3^2 + 5^3) \times 2^1. \end{aligned}$$

$$\begin{aligned} 232 &:= 2! \times (5! - 1!) - 3! = 2^1 \times (5^3 \times 1^5 - 3^2). \\ &= 2^3 \times (5^2 + 1^5 + 3^1). \end{aligned}$$

$$\begin{aligned} 233 &:= 2! \times 5! - 3! - 1! = -2^2 - 5^1 + 3^5 - 1^3. \\ &= 2^1 \times (5^3 - 3^2) + 1^5. \end{aligned}$$

$$\begin{aligned} 234 &:= 2! \times 5! \times 1! - 3! = -(2^2 + 5^1) \times 1^3 + 3^5. \\ &= (2^5 - 5^1 - 1^3) \times 3^2. \\ &= (2^2 + 5^1) \times (-1^5 + 3^3). \\ &= 2^1 \times (-5^3 - 1^2 + 3^5). \\ &= 2^1 \times (5^3 + 1^5 - 3^2). \end{aligned}$$

$$\begin{aligned} 235 &:= 1! - 3! + 5! \times 2! = 1^3 + 3^5 - 5^1 - 2^2. \\ &= -1^2 + (3^5 - 5^3) \times 2^1. \end{aligned}$$

$$\begin{aligned} 236 &:= (1! + 5!) \times 2! - 3! = (-1^2 + 5^1) \times (2^5 + 3^3). \\ &:= 2! \times (1! + 5!) - 3! = 2^1 \times 1^2 \times (-5^3 + 3^5). \end{aligned}$$

$$\begin{aligned} 240 &:= 4! \times 2! \times (3! - 1!) = (4^3 + 2^4) \times 3^1 \times 1^2. \\ &= 4^4 - 2^3 - 3^2 + 1^1. \\ &= (4^3 - 2^2) \times (3^1 + 1^4). \\ &= 4^4 - 2^1 \times (3^2 - 1^3). \\ &= 4^4 - 2^2 \times (3^1 + 1^3). \\ &= 4^4 - 2^3 \times (3^1 - 1^2). \end{aligned}$$

$$:= 5! - 4! \times (1! - 3!) = 5^1 \times 4^3 + 1^5 - 3^4.$$

$$\begin{aligned} 244 &:= 3! + 2! \times (5! - 1!) = (3^5 - 2^2 + 5^1) \times 1^3. \\ &= 3^2 \times (2^5 - 5^1) + 1^3. \\ &= 3^3 \times (2^2 + 5^1) + 1^5. \end{aligned}$$

$$\begin{aligned} 245 &:= 3! - 1! + 2! \times 5! = 3^5 - 1^2 + 2^3 - 5^1. \\ &= 3^5 + 1^3 - 2^2 + 5^1. \end{aligned}$$

$$\begin{aligned} 246 &:= 1! \times 3! + 5! \times 2! = 1^2 \times 3^5 - 5^1 + 2^3. \\ &\quad = (-1^5 + 3^1) \times 5^3 - 2^2. \end{aligned}$$

$$247 := 2! \times 5! + 1! + 3! = 2^3 - 5^1 + 1^2 + 3^5.$$

$$\begin{aligned} 250 &:= (5! - 1! + 3!) \times 2! = 5^2 \times (-1^5 + 3^1 + 2^3). \\ &\quad = 5^3 \times (1^5 - 3^1 + 2^2). \end{aligned}$$

$$251 := -1! + 2! \times (3! + 5!) = -1^3 + 2^2 + 3^5 + 5^1.$$

$$252 := 1! \times 2! \times (5! + 3!) = (1^3 + 2^5 - 5^1) \times 3^2.$$

$$254 := (1! + 3! + 5!) \times 2! = (-1^5 + 3^1) \times 5^3 + 2^2.$$

$$258 := 5! + (4! - 1!) \times 3! = 5^3 \times 4^1 + 1^4 - 3^5.$$

$$\begin{aligned} 262 &:= (5! - 1!) \times 2! + 4! = -5^2 - 1^1 + 2^5 + 4^4. \\ &\quad = 5^1 + 1^5 + 2^4 \times 4^2. \end{aligned}$$

$$263 := 2! \times 5! - 1! + 4! = 2^5 - 5^2 \times 1^1 + 4^4.$$

$$\begin{aligned} 264 &:= 1! \times 2! \times 5! + 4! = 1^1 + 2^5 - 5^2 + 4^4. \\ &\quad = -1^5 + 2^2 + 5^1 + 4^4. \end{aligned}$$

$$\begin{aligned} 264 &:= (2! \times 3! - 1!) \times 4! = -2^1 + 3^2 + 1^3 + 4^4. \\ &\quad = 2^2 + 3^1 + 1^3 + 4^4. \\ &\quad = 2^2 \times (3^4 + 1^1) - 4^3. \\ &\quad = 2^2 \times (3^1 - 1^4 + 4^3). \end{aligned}$$

$$266 := 2! + 3! \times 4! + 5! = -2^4 + 3^5 + 4^3 - 5^2.$$

$$276 := 2! \times (3! + 5!) + 4! = -2^5 + 3^3 + 5^2 + 4^4.$$

$$\begin{aligned} 282 &:= (2! \times 4! - 1!) \times 3! = -2^1 + 4^4 + 1^2 + 3^3. \\ &\quad = 2^4 \times 4^2 - 1^1 + 3^3. \end{aligned}$$

$$\begin{aligned} 286 &:= 2! \times (3! \times 4! - 1!) = 2^1 + 3^3 + 4^4 + 1^2. \\ &\quad = 2^2 + 3^3 + 4^4 - 1^1. \end{aligned}$$

$$\begin{aligned} 287 &:= 2! \times 3! \times 4! - 1! = 2^2 + 3^3 + 4^4 \times 1^1. \\ &\quad = 2^3 \times 3^2 \times 4^1 - 1^4. \end{aligned}$$

$$\begin{aligned} 288 &:= 2! \times 3! \times 1! \times 4! = (-2^3 + 3^4 - 1^2) \times 4^1. \\ &\quad = (2^4 + 3^1 - 1^3) \times 4^2. \\ &\quad = 2^1 \times (3^4 - 1^2 + 4^3). \end{aligned}$$

$$:= 2! \times (4! \times 1! + 5!) = (2^4 - 4^1) \times (-1^5 + 5^2).$$

$$289 := 1! + 2! \times 3! \times 4! = -1^2 + 2^1 \times (3^4 + 4^3).$$

$$\begin{aligned} 312 &:= (1! + 3! \times 2!) \times 4! = (1^3 + 3^4 - 2^2) \times 4^1. \\ &\quad = (1^2 - 3^3) \times (-2^4 + 4^1). \end{aligned}$$

$$\begin{aligned} 336 &:= (1! + 2!) \times 5! - 4! = (1^5 \times 2^4 + 5^1) \times 4^2. \\ &\quad = 1^5 \times 2^4 \times (5^2 - 4^1). \\ &:= (1! + 3!) \times 2! \times 4! = (-1^3 + 3^4 + 2^2) \times 4^1. \\ &\quad = -1^1 + 3^4 + 2^2 \times 4^3. \\ &\quad = (1^2 + 3^3) \times (2^4 - 4^1). \end{aligned}$$

$$\begin{aligned} 342 &:= (2! + 1!) \times (5! - 3!) = (2^5 + 1^3 + 5^1) \times 3^2. \\ &\quad = -2^5 - 1^2 + 5^3 \times 3^1. \end{aligned}$$

$$\begin{aligned} 354 &:= (1! + 2!) \times 5! - 3! = (1^1 - 2^2) \times (5^3 - 3^5). \\ &\quad = (1^2 + 2^1) \times (-5^3 + 3^5). \end{aligned}$$

$$\begin{aligned} 366 &:= 3! + (1! + 2!) \times 5! = 3^5 \times 1^2 - 2^1 + 5^3. \\ &\quad = 3^1 \times (1^5 - 2^2 + 5^3). \\ &\quad = -3^2 + (1^5 + 2^1) \times 5^3. \end{aligned}$$

$$378 := (1! + 2!) \times (3! + 5!) = -1^5 + 2^2 + 3^1 \times 5^3.$$

$$\begin{aligned} 384 &:= 4! + 5! \times (1! + 2!) = (4^2 - 5^1 + 1^4) \times 2^5. \\ &\quad = 4^4 + (5^1 - 1^2) \times 2^5. \end{aligned}$$

$$\begin{aligned} 432 &:= 4! \times (1! + 2!) \times 3! = (4^1 - 1^3) \times 2^4 \times 3^2. \\ &\quad = (4^3 \times 1^1 - 2^4) \times 3^2. \\ &\quad = 4^2 \times (-1^4 + 2^1) \times 3^3. \\ &:= (4! + 5!) \times (1! + 2!) = 4^2 \times (-5^1 \times 1^4 + 2^5). \end{aligned}$$

$$\mathbf{468} := 6! - 2! \times (3! + 5!) = 6^2 + 2^6 + 3^5 + 5^3.$$

$$\mathbf{476} := (5! - 1!) \times (3! - 2!) = (-5^3 + 1^1 + 3^5) \times 2^2.$$

$$\mathbf{480} := 1! \times 5! \times (3! - 2!) = (1^3 + 5^1 + 3^2) \times 2^5.$$

$$\mathbf{484} := (1! + 5!) \times (3! - 2!) = (-1^5 + 5^3 - 3^1) \times 2^2.$$

$$\mathbf{552} := 6! - (1! + 3!) \times 4! = -6^3 \times 1^6 + 3^1 \times 4^4.$$

$$\mathbf{570} := 6! - 3! \times (1! + 4!) = 6^4 - 3^6 - 1^3 + 4^1.$$

$$\mathbf{576} := (4! + 5!) \times (3! - 2!) = 4^5 + (5^2 - 3^4) \times 2^3.$$

$$\mathbf{577} := 1! + (5! - 4!) \times 3! = -(1^5 - 5^3) \times 4^1 + 3^4.$$

$$\mathbf{582} := (1! - 4! + 5!) \times 3! = 1^5 + 4^1 \times 5^3 + 3^4.$$

$$:= (3! - 4! - 5!) + 6! = 3^6 + 4^5 + 5^3 - 6^4.$$

$$\mathbf{598} := (3! - 1!) \times 5! - 2! = (3^3 - 1^5) \times (5^2 - 2^1).$$

$$\begin{aligned}\mathbf{600} &:= (1! - 2! + 3!) \times 5! = 1^5 \times 2^3 \times 3^1 \times 5^2. \\ &\quad = (-1^5 - 2^1 + 3^3) \times 5^2.\end{aligned}$$

$$:= 5! \times (1! - 2!) + 6! = (5^1 + 1^5) \times (2^6 + 6^2).$$

$$\mathbf{608} := (2! - 5!) + 3! + 6! = -2^5 - 5^3 + 3^6 + 6^2.$$

$$\mathbf{610} := (5! + 2!) \times (3! - 1!) = 5^3 + 2^1 \times 3^5 - 1^2.$$

$$\begin{aligned}\mathbf{624} &:= (3! - 1!) \times 5! + 4! = (-3^4 + 1^3) \times 5^1 + 4^5. \\ &\quad = 3^5 \times 1^1 + 5^3 + 4^4.\end{aligned}$$

$$\mathbf{672} := 3! \times 5! - 4! \times 2! = (-3^4 + 5^3) \times 4^2 - 2^5.$$

$$\mathbf{689} := 6! - 4! - 3! - 1! = 6^3 - 4^4 + 3^6 \times 1^1.$$

$$\mathbf{690} := 6! - 4! - 3! \times 1! = 6^3 - 4^4 + 3^6 + 1^1.$$

$$\begin{aligned}\mathbf{702} &:= (-1! - 2! + 5!) \times 3! = (-1^2 + 2^5 - 5^1) \times 3^3. \\ &\quad = (-1^5 + 2^1 + 5^2) \times 3^3.\end{aligned}$$

$$\mathbf{702} := 6! - 3! \times (2! + 1!) = -6^2 + 3^6 + 2^3 + 1^1.$$

$$\mathbf{704} := 2! + 3! - 4! + 6! = (-2^6 + 3^3) \times 4^2 + 6^4.$$

$$\mathbf{706} := 6! - 2! \times (1! + 3!) = -6^1 \times 2^2 + 1^3 + 3^6.$$

$$\mathbf{707} := -1! + 3! \times (5! - 2!) = 1^1 \times 3^3 \times 5^2 + 2^5.$$

$$\mathbf{708} := 1! \times 3! \times (5! - 2!) = 1^1 + 3^3 \times 5^2 + 2^5.$$

$$\mathbf{709} := 1! + 6! - 2! \times 3! = (1^3 - 6^1) \times 2^2 + 3^6.$$

$$:= 1! + 6! - 3! \times 2! = (-1^2 + 6^3) \times 3^1 + 2^6.$$

$$\mathbf{711} := -1! - 2! + 6! - 3! = (1^3 - 2^2) \times 6^1 + 3^6.$$

$$= -1^2 + 2^6 + 6^3 \times 3^1.$$

$$\mathbf{712} := 6! - 3! - 2! \times 1! = (6^3 \times 3^1 + 2^6) \times 1^2.$$

$$\mathbf{713} := 1! - 2! - 3! + 6! = 1^2 + 2^6 + 3^1 \times 6^3.$$

$$\mathbf{714} := (1! - 2!) \times 3! + 6! = -1^2 - 2^3 + 3^6 - 6^1.$$

$$:= (1! - 2! + 5!) \times 3! = (1^3 - 2^2) \times (5^1 - 3^5).$$

$$\mathbf{715} := 6! - 1! - 3! + 2! = -6^1 \times 1^2 + 3^6 - 2^3.$$

$$= (6^3 + 1^2) \times 3^1 + 2^6.$$

$$\mathbf{716} := 1! \times 2! - 3! + 6! = 1^2 - 2^3 + 3^6 - 6^1.$$

$$:= -1! \times 3! + 2! + 6! = 1^2 + 3^6 - 2^3 - 6^1.$$

$$:= 1! \times 6! - 3! + 2! = 1^2 - 6^1 + 3^6 - 2^3.$$

$$\mathbf{720} := (-1! + 3!) \times (4! + 5!) = (-1^5 + 3^4 + 4^3) \times 5^1.$$

$$\mathbf{724} := (1! + 5!) \times 3! - 2! = -1^3 + 5^2 \times (-3^1 + 2^5).$$

$$= -1^5 + 5^2 \times (3^3 + 2^1).$$

$$\mathbf{726} := 3! \times (2! + 5! - 1!) = -(3^1 - 2^5) \times 5^2 + 1^3.$$

$$= (3^3 + 2^1) \times 5^2 + 1^5.$$

$$:= (2! - 1!) \times 6! + 3! = 2^2 - 1^3 - 6^1 + 3^6.$$

$$= -2^3 - 1^2 + 6^1 + 3^6.$$

$$\mathbf{727} := 2! - 1! + 3! + 6! = 2^2 \times 1^3 + 3^6 - 6^1.$$

$$= -2^3 \times 1^2 + 3^6 + 6^1.$$

$$\mathbf{728} := 1! \times 3! + 2! + 6! = -(1^1 - 3^2) \times 2^6 + 6^3.$$

$$= 1^2 + 3^6 - 2^3 + 6^1.$$

$$= 1^3 + 3^6 + 2^2 - 6^1.$$

$$= (1^1 - 3^3) \times (-2^6 + 6^2).$$

$$\mathbf{729} := 1! + 2! + 6! + 3! = (-1^1 + 2^6 - 6^2) \times 3^3.$$

$$= (-1^2 + 2^3 - 6^1) \times 3^6.$$

$$= (-1^3 - 2^2 + 6^1) \times 3^6.$$

$$\begin{aligned} 730 &:= (3! - 1!) \times 2! + 6! = 3^6 - 1^2 + 2^3 - 6^1 \\ &\quad = 3^6 - 1^3 - 2^2 + 6^1. \end{aligned}$$

$$\begin{aligned} 731 &:= 2! \times 3! - 1! + 6! = -2^2 + 3^6 \times 1^3 + 6^1 \\ &\quad = 2^3 + 3^6 \times 1^2 - 6^1. \end{aligned}$$

$$\begin{aligned} 732 &:= 1! \times 2! \times 3! + 6! = 1^2 + 2^3 + 3^6 - 6^1 \\ &\quad = 1^3 - 2^2 + 3^6 + 6^1. \\ &:= 1! \times 3! \times (2! + 5!) = (1^2 + 3^5) \times (2^3 - 5^1). \end{aligned}$$

$$738 := (1! + 2!) \times 3! + 6! = -1^3 + 2^2 + 3^6 + 6^1.$$

$$743 := 3! \times 5! - 1! + 4! = 3^5 + 5^3 \times 1^4 \times 4^1.$$

$$756 := 4! + (2! + 5!) \times 3! = 4^3 \times 2^4 - 5^2 - 3^5.$$

$$768 := 1! \times 6! + 2! \times 4! = (1^6 + 6^1 - 2^2) \times 4^4.$$

$$780 := 2! \times (4! + 3!) + 6! = 2^6 - 4^4 + 3^3 \times 6^2.$$

$$816 := 5! \times (1! + 3!) - 4! = 5^4 - 1^5 + 3^1 \times 4^3.$$

$$826 := (1! + 3!) \times (-2! + 5!) = -1^1 + 3^3 + 2^5 \times 5^2.$$

$$838 := 1! \times 5! - 2! + 6! = (1^6 + 5^2) \times 2^5 + 6^1.$$

$$:= (1! + 3!) \times 5! - 2! = 1^1 + 3^2 \times (5^3 - 2^5).$$

$$\begin{aligned} 840 &:= (2! + 3! - 1!) \times 5! = 2^5 \times 3^3 + 1^1 - 5^2. \\ &\quad = (2^5 + 3^1) \times (-1^3 + 5^2). \end{aligned}$$

$$842 := 2! + (1! + 3!) \times 5! = (2^5 - 1^2) \times 3^3 + 5^1.$$

$$847 := 1! + 3! + 5! + 6! = -1^5 + 3^6 + 5^3 - 6^1.$$

$$848 := 2! + 6! + 3! + 5! = -2^6 \times 6^2 + 3^3 + 5^5.$$

$$854 := (5! + 2!) \times (1! + 3!) = 5^3 + (2^2 - 1^1) \times 3^5.$$

$$863 := (4! + 5!) \times 3! - 1! = -4^1 + 5^4 + 3^5 - 1^3.$$

$$\begin{aligned} 864 &:= 1! \times 3! \times 4! + 6! = (-1^6 + 3^4 + 4^3) \times 6^1. \\ &\quad = (1! \times 4! + 5!) \times 3! = -1^3 \times 4^1 + 5^4 + 3^5. \end{aligned}$$

$$865 := 1! + 3! \times (4! + 5!) = 1^3 + 3^5 - 4^1 + 5^4.$$

$$876 := (5! + 4! + 2!) \times 3! = 5^4 + 4^2 - 2^3 + 3^5.$$

$$936 := (2! + 3!) \times 5! - 4! = 2^2 + 3^5 + 5^4 + 4^3.$$

$$952 := (2! + 3!) \times (5! - 1!) = 2^2 \times (3^5 - 5^1) \times 1^3.$$

$$\begin{aligned} 960 &:= 1! \times 6! + 5! \times 2! = (-1^6 + 6^1 + 5^2) \times 2^5. \\ &\quad = (-1^6 + 6^2 - 5^1) \times 2^5. \end{aligned}$$

$$\begin{aligned} 961 &:= 1! + 2! \times 5! + 6! = (1^6 - 2^5) \times (5^1 - 6^2). \\ &\quad = (-1^6 + 2^5) \times (5^2 + 6^1). \end{aligned}$$

$$\begin{aligned} 968 &:= (2! + 3!) \times (1! + 5!) = 2^2 \times 3^5 + 1^3 - 5^1. \\ &\quad = -2^5 + (3^2 - 1^1) \times 5^3. \end{aligned}$$

$$984 := (2! + 3!) \times 5! + 4! = 2^2 + 3^4 - 5^3 + 4^5.$$

$$1200 := 2! \times (3! - 1!) \times 5! = (-2^2 + 3^5 + 1^3) \times 5^1.$$

$$1296 := 2! \times 6! - 3! \times 4! = -2^3 \times 6^4 + 3^6 \times 4^2.$$

$$\begin{aligned} 1392 &:= (3! \times 5! - 4!) \times 2! = 3^5 + 5^3 + 4^4 \times 2^2. \\ &\quad := 2! \times (3! \times 5! - 4!) = 2^5 \times (-3^4 + 5^3) - 4^2. \end{aligned}$$

$$1434 := (-1! + 5! \times 2!) \times 3! = (1^3 + 5^1) \times (-2^2 + 3^5).$$

$$1439 := 2! \times 3! \times 5! - 1! = 2^5 \times 3^2 \times 5^1 - 1^3.$$

$$1440 := 4! \times 5! - 2! \times 6! = -4^4 \times 5^2 + 2^6 + 6^5.$$

$$1464 := 2! \times 3! \times 5! + 4! = 2^2 \times (-3^5 + 5^4) - 4^3.$$

$$1466 := 4! + (1! + 6!) \times 2! = (4^4 - 1^2) \times 6^1 - 2^6.$$

$$\begin{aligned} 1488 &:= 2! \times (3! \times 5! + 4!) = 2^3 \times (3^5 - 5^2) - 4^4. \\ &\quad = 2^2 \times (-3^3 - 5^4 + 4^5). \end{aligned}$$

$$:= 2! \times (4! \times 1! + 6!) = 2^6 \times (4^1 - 1^2) + 6^4.$$

$$1584 := 3! \times (5! \times 2! + 4!) = (3^3 + 5^4) \times 2^2 - 4^5.$$

$$1680 := (1! \times 5! + 6!) \times 2! = (-1^5 + 5^2) \times (6^1 + 2^6).$$

$$1728 := 2! \times (3! \times 4! + 6!) = 2^6 \times 3^4 - 4^2 \times 6^3.$$

$$1920 := (-2! - 3! + 4!) \times 5! = 2^5 \times (-3^4 + 4^2 + 5^3).$$

$$\begin{aligned} 2160 &:= (3! - 1! - 2!) \times 6! = (-3^1 - 1^3 + 2^6) \times 6^2. \\ &\quad = (3^2 - 1^6 + 2^1) \times 6^3. \end{aligned}$$

$$2208 := (2! + 5!) \times 4! - 6! = (2^6 - 5^2) \times 4^4 - 6^5.$$

$$2400 := (4! + 2! - 3!) \times 5! = 4^4 + 2^3 \times (3^5 + 5^2).$$

$$2520 := 5! \times (4! - 1! - 2!) = (5^4 + 4^1 + 1^5) \times 2^2.$$

$$2640 := (-1! \times 2! + 4!) \times 5! = (1^4 + 2^5) \times 4^2 \times 5^1.$$

$$2784 := (2! - 3! + 5!) \times 4! = (-2^5 + 3^4 + 5^3) \times 4^2.$$

$$2868 := 4! \times 5! - 2! \times 3! = -4^4 + 5^5 + 2^3 - 3^2.$$

$$\begin{aligned}
& \mathbf{2873} := 4! \times 5! - 1! - 3! = -4^4 + 5^5 + 1^3 + 3^1. & \mathbf{11520} := (4! - 3! - 2!) \times 6! = -4^4 \times 3^2 + 2^6 \times 6^3. \\
& \mathbf{2880} := (-2! + 3!) \times 1! \times 6! = 2^6 \times 3^2 \times (-1^3 + 6^1). & \mathbf{12960} := (1! + 2!) \times 3! \times 6! = (-1^2 + 2^6 - 3^1) \times 6^3. \\
& \mathbf{2892} := 2! \times 3! + 4! \times 5! = -2^2 + 3^3 - 4^4 + 5^5. & \mathbf{13800} := (4! - 1!) \times (-5! + 6!) = 4^1 \times (1^6 + 5^5) + 6^4. \\
& \mathbf{2898} := (-1! + 4!) \times (3! + 5!) = -1^3 + 4^5 + 3^1 \times 5^4. & \mathbf{15840} := 2! \times (4! \times 5! + 7!) = 2^5 + 4^7 - 5^4 + 7^2. \\
& \mathbf{2976} := 4! \times (3! - 2! + 5!) = -4^3 - 3^4 - 2^2 + 5^5. & \mathbf{17160} := 1! \times 4! \times 6! - 5! = -1^5 + 4^4 \times 6^1 + 5^6. \\
& \mathbf{2994} := 5! \times (1! + 4!) - 3! = (5^1 + 1^3) \times (4^4 + 3^5). & \mathbf{17161} := 1! - 5! + 4! \times 6! = 1^5 \times 5^6 + 4^4 \times 6^1. \\
& \mathbf{3048} := (1! + 3! + 5!) \times 4! = -1^3 \times 3^4 + 5^5 + 4^1. & \mathbf{17274} := (4! \times 5! - 1!) \times 3! = 4^5 - 5^4 \times (1^1 - 3^3). \\
& \mathbf{3072} := (2! + 3! + 5!) \times 4! = 2^3 \times (-3^5 + 5^4) + 4^2. & \\
& \mathbf{3094} := (2! + 4!) \times (5! - 1!) = -2^1 \times 4^2 + 5^5 + 1^4. & \mathbf{19440} := (1! + 2! + 4!) \times 6! = (1^6 - 2^1 + 4^2) \times 6^4. \\
& & = -2^4 - 4^2 + 5^5 + 1^4. & = (-1^6 + 2^2 \times 4^1) \times 6^4. \\
& \mathbf{3360} := 6! + 5! \times (4! - 2!) = -6^6 + 5^5 \times 4^2 + 2^4. & \mathbf{20160} := (4! - 2! + 3!) \times 6! = (4^4 + 2^6) \times (3^3 + 6^2). \\
& \mathbf{3840} := (2! + 3! + 4!) \times 5! = 2^5 \times (3^4 + 4^3 - 5^2). & \mathbf{23040} := (2! + 3! + 4!) \times 6! = 2^6 \times 3^2 \times (4^4 - 6^3). \\
& \mathbf{4170} := (-1! - 4! + 6!) \times 3! = -1^3 + 4^6 - 6^1 + 3^4. & \mathbf{25920} := (2! \times 3! + 4!) \times 6! = -2^2 \times 3^4 \times 4^3 + 6^6. \\
& \mathbf{4182} := (1! - 4! + 6!) \times 3! = -1^3 + 4^6 + 6^1 + 3^4. & \mathbf{29952} := 3! \times (7! - 4! \times 2!) = (3^3 - 7^2 + 4^4) \times 2^7. \\
& \mathbf{4320} := (2! - 1!) \times 3! \times 6! = (-2^3 - 1^2 + 3^6) \times 6^1. & \\
& & = 2^1 \times (1^6 + 3^2) \times 6^3. & \mathbf{30240} := (2! \times 4! - 3!) \times 6! = (2^4 + 4^2) \times (3^6 + 6^3). \\
& & := (2! - 1!) \times 7! - 6! = (2^7 - 1^6 - 7^1) \times 6^2. & \mathbf{37440} := 4! \times (5! + 2! \times 6!) = 4^5 \times (-5^2 + 2^4) + 6^6. \\
& \mathbf{4326} := 3! \times (2! - 1! + 6!) = (3^6 - 2^3) \times 1^2 \times 6^1. & \mathbf{43200} := 2! \times (4! + 3!) \times 6! = (-2^6 + 4^4) \times (3^2 + 6^3). \\
& \mathbf{4332} := 1! \times 3! \times (2! + 6!) = (1^2 + 3^6 - 2^3) \times 6^1. & \mathbf{46080} := 2! \times (8! - 4! \times 6!) = -2^8 - 8^2 - 4^4 + 6^6. \\
& \mathbf{4608} := 3! \times (4! \times 2! + 6!) = 3^3 \times 4^4 - 2^6 \times 6^2. & \mathbf{48960} := 6! \times 3! \times 2! + 8! = 6^6 - 3^2 \times (2^8 - 8^3). \\
& \mathbf{4800} := 1! \times 7! - 2! \times 5! = (-1^7 + 7^1) \times 2^5 \times 5^2. & \\
& \mathbf{5050} := 2! \times (3! - 1!) + 7! = (2^7 - 3^3) \times (1^1 + 7^2). & \mathbf{69120} := (-2! + 3!) \times 4! \times 6! = (2^6 \times 3^2 - 4^4) \times 6^3. \\
& \mathbf{5058} := (2! + 1!) \times 3! + 7! = 2^1 \times (-1^2 + 3^7 + 7^3). & & = 2^6 \times (3^4 \times 4^2 - 6^3). \\
& \mathbf{5136} := 7! + (3! - 2!) \times 4! = (7^4 - 3^7) \times (2^3 + 4^2). & & := (3! - 2!) \times 6! \times 4! = 3^3 \times (2^6 \times 6^2 + 4^4). \\
& \mathbf{5178} := 3! \times (4! - 1!) + 7! = 3^4 \times 4^3 + 1^7 - 7^1. & \mathbf{95040} := (4! - 2!) \times 6! \times 3! = (4^6 - 2^4 \times 6^2) \times 3^3. \\
& \mathbf{5190} := (1! + 4!) \times 3! + 7! = -1^7 + 4^3 \times 3^4 + 7^1. & \\
& \mathbf{5736} := (2! \times 5! - 1!) \times 4! = 2^1 \times (5^5 - 1^2 - 4^4). & \mathbf{131040} := (2! + 4!) \times 1! \times 7! = (-2^2 + 4^7) \times (1^4 + 7^1). \\
& \mathbf{7800} := 5! \times (4! - 1!) + 7! = 5^4 + (4^5 + 1^7) \times 7^1. & \mathbf{138240} := (2! + 3!) \times 6! \times 4! = 2^6 \times (-3^4 + 6^3) \times 4^2. \\
& \mathbf{8640} := 1! \times 6! \times 2! \times 3! = (-1^2 + 6^1) \times 2^6 \times 3^3. & \mathbf{155520} := (2! \times 6! + 7!) \times 4! = 2^7 \times (6^4 - 7^2) - 4^6. \\
& & \mathbf{161280} := (4! + 2! + 3!) \times 7! = 4^3 \times (2^7 - 3^2 + 7^4).
\end{aligned}$$

2.2.3 Five Terms Expressions

Since the number is too high, this will be dealt in next work [12].

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