

RESEARCH GROUP IN MATHEMATICAL INEQUALITIES AND APPLICATIONS

PROBLEM CORNER

Problem 9, (2009)

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Conjecture. Let $x_1, x_2, \dots, x_n, y_1, y_2, \dots, y_n$ be positive real numbers and let $p \geq 1, q \geq 1$. Then

$$\sum_{i=1}^n \frac{\left(x_i^{p+1} + x_{i+1}^{p+1}\right) \left(y_i^{q+1} + y_{i+1}^{q+1}\right)}{\left(x_i^p + x_{i+1}^p\right) \left(y_i^q + y_{i+1}^q\right)} \geq \frac{1}{n^2} \sum_{i=1}^n x_i \sum_{i=1}^n y_i$$

where $x_{n+1} = x_1, y_{n+1} = y_1$. If $p \leq -1, q \leq -1$, then the above inequality is reversed.