

Palindromic-Type Pandigital Patterns in Pythagorean Triples - I

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Abstract

This paper brings examples of Palindromic-Type Pandigital Patterns in Pythagorean Triples. These are constructed in a padronized way. This means that in all the patterns we have pandigital palindromic-type expressions. The only change appears is in the middle term and last numbers in the first and third values. The results are obtained in such a way that we have total values as: 9, 99, 999, 9999, 99999, etc. The construction is based on a procedure well known in the literature. There is very much uniformity among the results.

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1 Procedure

Let's consider the following three functions:

$$\begin{aligned} F(m, n) &:= m^2 - n^2 \\ G(m, n) &:= 2mn \\ H(m, n) &:= m^2 + n^2 \end{aligned} \tag{1.1}$$

Then we can easily check that

$$\begin{aligned} F(m, n)^2 + G(m, n)^2 &= (m^2 - n^2)^2 + (2mn)^2 \\ &= m^4 - 2m^2n^2 + n^4 + 4m^2n^2 \\ &= m^4 + 2m^2n^2 + n^4 \\ &= (m^2 + n^2)^2 = H(m, n)^2. \end{aligned}$$

This proves that the triple (F, G, H) is a **Pythagorean triple**. The Procedure (1.1) is very famous in the literature [1]. Some patterned examples based on the Procedure (1.1) are studied by author [6]. Some particular cases are as follows:

$$\begin{aligned} (F(3, 2), G(3, 2), H(3, 2)) &\Rightarrow (5, 12, 13) \\ (F(4, 2), G(4, 2), H(4, 2)) &\Rightarrow (12, 16, 20) \\ (F(5, 2), G(5, 2), H(5, 2)) &\Rightarrow (21, 20, 29) \\ (F(6, 2), G(6, 2), H(6, 2)) &\Rightarrow (32, 24, 40) \\ (F(9, 3), G(9, 3), H(9, 3)) &\Rightarrow (72, 54, 90) \\ (F(9, 7), G(9, 7), H(9, 7)) &\Rightarrow (32, 126, 130) \\ (F(10, 9), G(10, 9), H(10, 9)) &\Rightarrow (19, 180, 181) \end{aligned}$$

The aim of this work is to write **Palindromic-Type Pandigital Patterns in Pythagorean Triples**. This we have done in three different ways. First way give 9 patterns, second way give 99 patterns, and the third way give 999 patterns. All the patterns are very much similar in terms of palindromic-type pandigital patterns. This similarity we call as "**uniformity of results**". This uniformity is explain in the following section.

2 Uniformity of Results

In order to get **Palindromic-Type Pandigital Patterns in Pythagorean Triples**, the following pattern appears automatically in the beginning of each part:

$$\begin{aligned}
 99^2 + 20^2 &= 101^2 & := 10201 \\
 9999^2 + 200^2 &= 10001^2 & := 100020001 \\
 999999^2 + 2000^2 &= 1000001^2 & := 1000002000001 \\
 99999999^2 + 20000^2 &= 100000001^2 & := 1000000200000001 \\
 999999999^2 + 200000^2 &= 1000000001^2 & := 10000000020000000001 \\
 9999999999^2 + 2000000^2 &= 10000000001^2 & := 1000000000200000000001
 \end{aligned} \tag{2.1}$$

The above pattern is obtained by considering $n = 1$; $m = 9, 99, 999, 9999, 99999, \dots$ in following Procedure:

$$\begin{aligned}
 F_1(m, n) &:= m(2n + m) \\
 G_1(m, n) &:= 2n(n + m) \\
 H_1(m, n) &:= m^2 + 2mn + 2n^2
 \end{aligned} \tag{2.2}$$

More details on the Procedures given in (1.1) and (2.2) can be seen in Taneja [5, 6]. We shall show below as an idea how each row is connected with our results. We get total number of result in each case given as below:

$$\begin{aligned}
 \text{Line 1} \Rightarrow \text{Total patterns: } &9 \\
 \text{Line 2} \Rightarrow \text{Total patterns: } &99 \\
 \text{Line 3} \Rightarrow \text{Total patterns: } &999 \\
 \text{Line 4} \Rightarrow \text{Total patterns: } &9999 \\
 \text{Line 5} \Rightarrow \text{Total patterns: } &99999 \\
 &\dots \quad \dots \quad \dots \quad \dots \quad \dots \quad \dots
 \end{aligned}$$

Let's see how it works in each subsection below:

2.1 First Line

Let's consider

$$m = 10, 110, 1110, 11110, 111110, 1111110, 11111110, 111111110$$

in (1.1), then for $n = 1$ and $n = 9$, we have the first and the last *palindromic-type pandigital Pythagorean patterns* given below:

► First Pattern

$$\begin{aligned}
 099^2 + 20^2 &= \mathbf{1}01^2 \\
 12099^2 + 220^2 &= \mathbf{121}01^2 \\
 1232099^2 + 2220^2 &= \mathbf{12321}01^2 \\
 123432099^2 + 22220^2 &= \mathbf{1234321}01^2 \\
 12345432099^2 + 222220^2 &= \mathbf{123454321}01^2 \\
 1234565432099^2 + 2222220^2 &= \mathbf{12345654321}01^2 \\
 123456765432099^2 + 22222220^2 &= \mathbf{1234567654321}01^2 \\
 12345678765432099^2 + 222222220^2 &= \mathbf{123456787654321}01^2 \\
 1234567898765432099^2 + 2222222220^2 &= \mathbf{12345678987654321}01^2
 \end{aligned} \tag{2.3}$$

► Last Pattern

$$\begin{aligned}
 019^2 + 180^2 &= 181^2 \\
 12019^2 + 1980^2 &= 12181^2 \\
 1232019^2 + 19980^2 &= 1232181^2 \\
 123432019^2 + 199980^2 &= 123432181^2 \\
 12345432019^2 + 1999980^2 &= 12345432181^2 \\
 1234565432019^2 + 19999980^2 &= 1234565432181^2 \\
 123456765432019^2 + 199999980^2 &= 123456765432181^2 \\
 12345678765432019^2 + 1999999980^2 &= 12345678765432181^2 \\
 1234567898765432019^2 + 19999999980^2 &= 1234567898765432181^2
 \end{aligned} \tag{2.4}$$

Below are some remarks based on above two patterns:

Remark 1. (i) *The first line of first pattern (2.3) is the first line as given in pattern (2.1), i.e.,*

$$99^2 + 20^2 = 101^2.$$

(ii) *The last two digits follow the square of as of numbers, i.e.,*

$$01 = 1^2, 04 = 2^2, \dots, 81 = 9^2.$$

(iii) *The sum of the last two digits of first and third members of each line is same, i.e.,*

$$\begin{aligned}
 n = 1 &\Rightarrow 99 + 01 = 100 \\
 n = 2 &\Rightarrow 96 + 04 = 100 \\
 n = 3 &\Rightarrow 91 + 09 = 100 \\
 n = 4 &\Rightarrow 84 + 16 = 100 \\
 n = 5 &\Rightarrow 75 + 25 = 100 \\
 n = 6 &\Rightarrow 64 + 36 = 100 \\
 n = 7 &\Rightarrow 51 + 49 = 100 \\
 n = 8 &\Rightarrow 19 + 64 = 100 \\
 n = 9 &\Rightarrow 19 + 81 = 100
 \end{aligned}$$

For details see the Section 3.

2.2 Second Line

Let's consider

$$m = 100, 1100, 11100, 111100, 1111100, 11111100, 111111100, 1111111100$$

in (1.1), then for $n = 1$ and $n = 999$, we have the first and the last *palindromic-type pandigital Pythagorean patterns* given below:

► First Pattern

$$\begin{aligned}
 09999^2 + 200^2 &= 10001^2 \\
 1209999^2 + 2200^2 &= 1210001^2 \\
 123209999^2 + 22200^2 &= 123210001^2 \\
 12343209999^2 + 222200^2 &= 12343210001^2 \\
 1234543209999^2 + 2222200^2 &= 1234543210001^2 \\
 123456543209999^2 + 22222200^2 &= 123456543210001^2 \\
 12345676543209999^2 + 222222200^2 &= 12345676543210001^2 \\
 1234567876543209999^2 + 2222222200^2 &= 1234567876543210001^2 \\
 123456789876543209999^2 + 22222222200^2 &= 123456789876543210001^2
 \end{aligned} \tag{2.5}$$

► Last Pattern

$$\begin{aligned}
 00199^2 + 19800^2 &= 19801^2 \\
 1200199^2 + 217800^2 &= 1219801^2 \\
 123200199^2 + 2197800^2 &= 123219801^2 \\
 12343200199^2 + 21997800^2 &= 12343219801^2 \\
 1234543200199^2 + 219997800^2 &= 1234543219801^2 \\
 123456543200199^2 + 2199997800^2 &= 123456543219801^2 \\
 12345676543200199^2 + 21999997800^2 &= 1234567876543219801^2 \\
 123456789876543200199^2 + 219999997800^2 &= 123456789876543219801^2
 \end{aligned} \tag{2.6}$$

In this case, we observe that the second term in the first line doesn't give good pattern. It happens with many results. Below are some remarks based on above two patterns:

Remark 2. (i) *The first line of first pattern (2.5) is the second line as given in pattern (2.1), i.e.,*

$$9999^2 + 200^2 = 10001^2.$$

(ii) *The last four digits follow the square of as of numbers, i.e.,*

$$0001 = 1^2, 0004 = 2^2, \dots, 9801 = 99^2.$$

(iii) *The sum of the last four digits of first and third members of each line is same, i.e.,*

$$\begin{aligned}
 n = 1 &\Rightarrow 9999 + 0001 = 10000 \\
 n = 2 &\Rightarrow 9996 + 0004 = 10000 \\
 n = 3 &\Rightarrow 9991 + 0009 = 10000 \\
 n = 4 &\Rightarrow 9984 + 0016 = 10000 \\
 &\dots &&\dots &&\dots \\
 &\dots &&\dots &&\dots \\
 n = 97 &\Rightarrow 0591 + 9409 = 10000 \\
 n = 98 &\Rightarrow 0396 + 9604 = 10000 \\
 n = 99 &\Rightarrow 0199 + 9801 = 10000
 \end{aligned}$$

For details see the Section 4.

2.3 Third Line

Let's consider

$$m = 1000, 11000, 111000, 1111000, 11111000, 111111000, 1111111000, 11111111000$$

in (1.1), then for $n = 1$ and $n = 999$, we have the first and the last *palindromic-type pandigital Pythagorean patterns* given below:

► First Pattern

$$\begin{aligned}
 0999999^2 + 2000^2 &= 1000001^2 \\
 120999999^2 + 22000^2 &= 121000001^2 \\
 1232099999^2 + 222000^2 &= 12321000001^2 \\
 123432099999^2 + 2222000^2 &= 1234321000001^2 \\
 12345432099999^2 + 22222000^2 &= 123454321000001^2 \\
 1234565432099999^2 + 222222000^2 &= 12345654321000001^2 \\
 123456765432099999^2 + 2222222000^2 &= 1234567654321000001^2 \\
 12345678765432099999^2 + 22222222000^2 &= 123456787654321000001^2 \\
 1234567898765432099999^2 + 222222222000^2 &= 12345678987654321000001^2
 \end{aligned} \tag{2.7}$$

► Last Pattern

$$\begin{aligned}
 0001999^2 + 1998000^2 &= 1998001^2 \\
 120001999^2 + 21978000^2 &= 121998001^2 \\
 12320001999^2 + 221778000^2 &= 12321998001^2 \\
 1234320001999^2 + 2219778000^2 &= 1234321998001^2 \\
 123454320001999^2 + 22199778000^2 &= 123454321998001^2 \\
 12345654320001999^2 + 221999778000^2 &= 12345654321998001^2 \\
 1234567654320001999^2 + 2219999778000^2 &= 1234567654321998001^2 \\
 123456787654320001999^2 + 22199999778000^2 &= 123456787654321998001^2 \\
 12345678987654320001999^2 + 221999999778000^2 &= 12345678987654321998001^2
 \end{aligned} \tag{2.8}$$

In this case, we observe that the second term in the first line doesn't give good pattern. It happens with many results. Below are some remarks based on above two patterns:

Remark 3. (i) *The first line of first pattern (2.7) is the third line as given in pattern (2.1), i.e.,*

$$99999^2 + 2000^2 = 1000001^2.$$

(ii) *The last six digits follow the square of as of numbers, i.e.,*

$$000001 = 1^2, 000004 = 2^2, \dots, 999801 = 999^2.$$

(iii) The sum of the last six digits of first and third members of each line is same, i.e.,

$$\begin{aligned}
 n = 1 &\Rightarrow 999999 + 000001 = 1000000 \\
 n = 2 &\Rightarrow 999996 + 000004 = 1000000 \\
 n = 3 &\Rightarrow 999991 + 000009 = 1000000 \\
 n = 4 &\Rightarrow 999984 + 000016 = 1000000 \\
 \dots &\dots \dots \dots \dots \\
 \dots &\dots \dots \dots \dots \\
 n = 997 &\Rightarrow 005991 + 994009 = 1000000 \\
 n = 998 &\Rightarrow 003996 + 996004 = 1000000 \\
 n = 999 &\Rightarrow 001999 + 998001 = 1000000.
 \end{aligned}$$

For details see the Section 5.

2.4 Forth Line

Let's consider

$m = 10000, 110000, 1110000, 11110000, 111110000, 1111110000, 11111110000, 111111110000$ in (1.1), then for $n = 1$ and $n = 9999$, we have the first and the last *palindromic-type pandigital Pythagorean patterns* given below:

► First Pattern

$$\begin{aligned}
 099999999^2 + 20000^2 &= 100000001^2 \\
 1209999999^2 + 220000^2 &= 1210000001^2 \\
 123209999999^2 + 2220000^2 &= 123210000001^2 \\
 12343209999999^2 + 22220000^2 &= 12343210000001^2 \\
 1234543209999999^2 + 222220000^2 &= 1234543210000001^2 \\
 123456543209999999^2 + 2222220000^2 &= 123456543210000001^2 \\
 12345676543209999999^2 + 22222220000^2 &= 12345676543210000001^2 \\
 1234567876543209999999^2 + 222222220000^2 &= 1234567876543210000001^2 \\
 123456789876543209999999^2 + 2222222220000^2 &= 123456789876543210000001^2 \quad (2.9)
 \end{aligned}$$

► Last Pattern

$$\begin{aligned}
 000019999^2 + 199980000^2 &= 199980001^2 \\
 12000019999^2 + 2199780000^2 &= 12199980001^2 \\
 1232000019999^2 + 22197780000^2 &= 1232199980001^2 \\
 123432000019999^2 + 222177780000^2 &= 123432199980001^2 \\
 12345432000019999^2 + 2221977780000^2 &= 12345432199980001^2 \\
 1234565432000019999^2 + 22219977780000^2 &= 1234565432199980001^2 \\
 123456765432000019999^2 + 222199977780000^2 &= 123456765432199980001^2 \\
 12345678765432000019999^2 + 2221999977780000^2 &= 12345678765432199980001^2 \\
 1234567898765432000019999^2 + 22219999977780000^2 &= 1234567898765432199980001^2 \quad (2.10)
 \end{aligned}$$

In this case, we observe that the second term in the first line doesn't give good pattern. It happens with many results. Below are some remarks based on above two patterns:

Remark 4. (i) *The first line of first pattern (2.9) is the forth line as given in pattern (2.1), i.e.,*

$$99999999^2 + 20000^2 = 100000001^2.$$

(ii) *The last eight digits follow the square of as of numbers, i.e.,*

$$00000001 = 1^2, 00000004 = 2^2, \dots, 99980001 = 9999^2.$$

(iii) *The sum of the last eight digits of first and third members of each line is same, i.e.,*

$$\begin{aligned} n = 1 &\Rightarrow 99999999 + 00000001 = 100000000 \\ n = 2 &\Rightarrow 99999996 + 00000004 = 100000000 \\ n = 3 &\Rightarrow 99999991 + 00000009 = 100000000 \\ n = 4 &\Rightarrow 99999984 + 00000016 = 100000000 \\ \dots &\dots \dots \dots \dots \\ \dots &\dots \dots \dots \dots \dots \\ n = 9997 &\Rightarrow 00059991 + 99940009 = 100000000 \\ n = 9998 &\Rightarrow 00039996 + 99960004 = 100000000 \\ n = 9999 &\Rightarrow 00019999 + 99980001 = 100000000. \end{aligned}$$

The results are not written in this paper, but are similar to one seen in Section 5.

2.5 Fifth Line

Let's consider

$$m = 100000, 1100000, 11100000, 111100000, 1111100000, 11111100000, 111111100000, 1111111100000$$

in (1.1), then for $n = 1$ and $n = 9999$, we have the first and the last *palindromic-type pandigital Pythagorean patterns* given below:

► First Pattern

$$\begin{aligned} 0999999999^2 + 200000^2 &= 1000000001^2 \\ 12\ 0999999999^2 + 2200000^2 &= 121\ 000000001^2 \\ 1232\ 0999999999^2 + 22200000^2 &= 12321\ 000000001^2 \\ 123432\ 0999999999^2 + 222200000^2 &= 1234321\ 000000001^2 \\ 12345432\ 0999999999^2 + 2222200000^2 &= 123454321\ 000000001^2 \\ 1234565432\ 0999999999^2 + 22222200000^2 &= 12345654321\ 000000001^2 \\ 123456765432\ 0999999999^2 + 222222200000^2 &= 1234567654321\ 000000001^2 \\ 12345678765432\ 0999999999^2 + 2222222200000^2 &= 123456787654321\ 000000001^2 \\ 1234567898765432\ 0999999999^2 + 22222222200000^2 &= 12345678987654321\ 000000001^2 \end{aligned} \tag{2.11}$$

► Last Pattern

$$\begin{aligned}
 & 0000019999^2 + 19999800000^2 = 19999800001^2 \\
 & 120000019999^2 + 219997800000^2 = 1219999800001^2 \\
 & 1232000019999^2 + 2219977800000^2 = 123219999800001^2 \\
 & 123432000019999^2 + 22219777800000^2 = 12343219999800001^2 \\
 & 12345432000019999^2 + 222217777800000^2 = 1234543219999800001^2 \\
 & 1234565432000019999^2 + 22221997777800000^2 = 123456543219999800001^2 \\
 & 123456765432000019999^2 + 222219997777800000^2 = 12345676543219999800001^2 \\
 & 1234567898765432000019999^2 + 2222199997777800000^2 = 123456789876543219999800001^2 \quad (2.12) \\
 & 1234567898765432000019999^2 + 2222199997777800000^2 = 123456789876543219999800001^2
 \end{aligned}$$

In this case, we observe that the second term in the first line doesn't give good pattern. It happens with many results. Below are some remarks based on above two patterns:

Remark 5. (i) *The first line of first pattern (2.9) is the fifth line as given in pattern (2.1), i.e.,*

$$999999999^2 + 200000^2 = 10000000001^2.$$

(ii) *The last ten digits follow the square of as of numbers, i.e.,*

$$0000000001 = 1^2, 0000000004 = 2^2, \dots, 9999800001 = 9999^2.$$

(iii) *The sum of the last ten digits of first and third members of each line is same, i.e.,*

$$\begin{aligned}
 n = 1 & \Rightarrow 999999999 + 0000000001 = 10000000000 \\
 n = 2 & \Rightarrow 999999996 + 0000000004 = 10000000000 \\
 n = 3 & \Rightarrow 999999991 + 0000000009 = 10000000000 \\
 n = 4 & \Rightarrow 999999984 + 0000000016 = 10000000000 \\
 & \dots & \dots & \dots & \dots & \dots & \dots \\
 & \dots & \dots & \dots & \dots & \dots & \dots \\
 n = 997 & \Rightarrow 0000599991 + 9999400009 = 10000000000 \\
 n = 998 & \Rightarrow 0000399996 + 9999600004 = 10000000000 \\
 n = 999 & \Rightarrow 0000199999 + 9999800001 = 10000000000.
 \end{aligned}$$

The results are not written in this paper, but are similar to one seen in Section 5.

According to above five lines of example (2.1), the same procedure continues for further lines. The results in this paper are divided in three groups based on first three lines. **First group** is with 9 results, the **second group** is with 99 results, and the **third group** is with 999 results. In second and third groups first 20 patterns are written complete, and the other patterns are written just with first four lines. The continuation is obvious following the similar way.

3 First Group

Below are 9 examples of **pattern in Pythagorean triples** with 9 digits from 1 to 9 written as **palindromic-type**, where the **first line** of first pattern is the same as **first line** of example (2.1). Moreover, this section is an extension of subsection 2.1.

3.1 For $n = 1, 2, 3, \dots, 7, 8, 9$:

Let's consider

$$m = 10, 110, 1110, 11110, 111110, 1111110, 11111110, 111111110, 1111111110$$

in (1.1), then for each value of $n = 1, 2, 3, \dots, 7, 8, 9$; there are 9 *palindromic-type pandigital Pythagorean patterns* given below:

$$\begin{aligned}
 099^2 + 20^2 &= 101^2 \\
 12099^2 + 220^2 &= 12101^2 \\
 1232099^2 + 2220^2 &= 1232101^2 \\
 123432099^2 + 22220^2 &= 123432101^2 \\
 12345432099^2 + 222220^2 &= 12345432101^2 \\
 1234565432099^2 + 2222220^2 &= 1234565432101^2 \\
 123456765432099^2 + 22222220^2 &= 123456765432101^2 \\
 12345678765432099^2 + 222222220^2 &= 12345678765432101^2 \\
 1234567898765432099^2 + 2222222220^2 &= 1234567898765432101^2
 \end{aligned} \tag{3.1}$$

$$\begin{aligned}
 096^2 + 40^2 &= 104^2 \\
 12096^2 + 440^2 &= 12104^2 \\
 1232096^2 + 4440^2 &= 1232104^2 \\
 123432096^2 + 44440^2 &= 123432104^2 \\
 12345432096^2 + 444440^2 &= 12345432104^2 \\
 1234565432096^2 + 4444440^2 &= 1234565432104^2 \\
 123456765432096^2 + 44444440^2 &= 123456765432104^2 \\
 12345678765432096^2 + 444444440^2 &= 12345678765432104^2
 \end{aligned} \tag{3.2}$$

$$\begin{aligned}
 091^2 + 60^2 &= 109^2 \\
 12091^2 + 660^2 &= 12109^2 \\
 1232091^2 + 6660^2 &= 1232109^2 \\
 123432091^2 + 66660^2 &= 123432109^2 \\
 12345432091^2 + 666660^2 &= 12345432109^2 \\
 1234565432091^2 + 6666660^2 &= 1234565432109^2 \\
 123456765432091^2 + 66666660^2 &= 123456765432109^2 \\
 12345678765432091^2 + 666666660^2 &= 12345678765432109^2 \\
 1234567898765432091^2 + 6666666660^2 &= 1234567898765432109^2 \tag{3.3}
 \end{aligned}$$

$$\begin{aligned}
 084^2 + 80^2 &= 116^2 \\
 12084^2 + 880^2 &= 12116^2 \\
 1232084^2 + 8880^2 &= 1232116^2 \\
 123432084^2 + 88880^2 &= 123432116^2 \\
 12345432084^2 + 888880^2 &= 12345432116^2 \\
 123456765432084^2 + 8888880^2 &= 123456765432116^2 \\
 12345678765432084^2 + 88888880^2 &= 12345678765432116^2 \\
 1234567898765432084^2 + 888888880^2 &= 1234567898765432116^2 \tag{3.4}
 \end{aligned}$$

$$\begin{aligned}
 075^2 + 100^2 &= 125^2 \\
 12075^2 + 1100^2 &= 12125^2 \\
 1232075^2 + 11100^2 &= 1232125^2 \\
 123432075^2 + 111100^2 &= 123432125^2 \\
 12345432075^2 + 1111100^2 &= 12345432125^2 \\
 1234565432075^2 + 11111100^2 &= 1234565432125^2 \\
 123456765432075^2 + 111111100^2 &= 123456765432125^2 \\
 12345678765432075^2 + 1111111100^2 &= 12345678765432125^2 \\
 1234567898765432075^2 + 11111111100^2 &= 1234567898765432125^2 \tag{3.5}
 \end{aligned}$$

$$\begin{aligned}
 064^2 + 120^2 &= 136^2 \\
 12064^2 + 1320^2 &= 12136^2 \\
 1232064^2 + 13320^2 &= 1232136^2 \\
 123432064^2 + 133320^2 &= 123432136^2 \\
 12345432064^2 + 1333320^2 &= 12345432136^2 \\
 123456765432064^2 + 13333320^2 &= 123456765432136^2 \\
 12345678765432064^2 + 133333320^2 &= 12345678765432136^2 \\
 1234567898765432064^2 + 1333333320^2 &= 1234567898765432136^2 \tag{3.6}
 \end{aligned}$$

$$\begin{aligned}
 051^2 + 140^2 &= 149^2 \\
 12051^2 + 1540^2 &= 12149^2 \\
 1232051^2 + 15540^2 &= 1232149^2 \\
 123432051^2 + 155540^2 &= 123432149^2 \\
 12345432051^2 + 1555540^2 &= 12345432149^2 \\
 1234565432051^2 + 15555540^2 &= 1234565432149^2 \\
 123456765432051^2 + 155555540^2 &= 123456765432149^2 \\
 12345678765432051^2 + 1555555540^2 &= 12345678765432149^2 \\
 1234567898765432051^2 + 15555555540^2 &= 1234567898765432149^2
 \end{aligned} \tag{3.7}$$

$$\begin{aligned}
 036^2 + 160^2 &= 164^2 \\
 12036^2 + 1760^2 &= 12164^2 \\
 1232036^2 + 17760^2 &= 1232164^2 \\
 123432036^2 + 177760^2 &= 123432164^2 \\
 12345432036^2 + 1777760^2 &= 12345432164^2 \\
 1234565432036^2 + 17777760^2 &= 1234565432164^2 \\
 123456765432036^2 + 177777760^2 &= 123456765432164^2 \\
 12345678765432036^2 + 1777777760^2 &= 12345678765432164^2 \\
 1234567898765432036^2 + 17777777760^2 &= 1234567898765432164^2
 \end{aligned} \tag{3.8}$$

$$\begin{aligned}
 019^2 + 180^2 &= 181^2 \\
 12019^2 + 1980^2 &= 12181^2 \\
 1232019^2 + 19980^2 &= 1232181^2 \\
 123432019^2 + 199980^2 &= 123432181^2 \\
 12345432019^2 + 1999980^2 &= 12345432181^2 \\
 1234565432019^2 + 19999980^2 &= 1234565432181^2 \\
 123456765432019^2 + 199999980^2 &= 123456765432181^2 \\
 12345678765432019^2 + 1999999980^2 &= 12345678765432181^2 \\
 1234567898765432019^2 + 19999999980^2 &= 1234567898765432181^2
 \end{aligned} \tag{3.9}$$

From the 9 patterns given above, we have following remark:

Remark 6. It is interesting to observe the following symmetry in squared value in last two digits:

$$\begin{array}{ll}
 \text{Equation (2.1)} & \Rightarrow 01 = 1^2 \\
 \text{Equation (2.2)} & \Rightarrow 04 = 2^2 \\
 \text{Equation (2.3)} & \Rightarrow 09 = 3^2 \\
 \cdots & \cdots \quad \cdots \quad \cdots \\
 \cdots & \cdots \quad \cdots \quad \cdots \\
 \text{Equation (2.7)} & \Rightarrow 49 = 7^2 \\
 \text{Equation (2.8)} & \Rightarrow 64 = 8^2 \\
 \text{Equation (2.9)} & \Rightarrow 81 = 9^2.
 \end{array}$$

4 Second Group

Below are 99 examples of **pattern in Pythagorean triples** with 9 digits from 1 to 9 written as **palindromic-type**, where the **first line** of first pattern is the same as **second line** of example (2.1). Moreover, this section is an extension of subsection 2.2.

4.1 For $n = 1, 2, 3, \dots, 97, 98, 99$:

This subsection is divided in two parts. The first part give first 19 results as complete patterns. The other 80 are written only with four lines. The other four lines follows on similar lines.

4.1.1 For $n = 1, 2, 3, \dots, 17, 18, 19$:

Let's consider

$$m = 100, 1100, 11100, 111100, 1111100, 11111100, 111111100, 1111111100$$

in (1.1), then for each value of $n = 1, 2, 3, \dots, 17, 18, 19$; there are 19 *palindromic-type pandigital Pythagorean patterns* given below:

$$\begin{aligned}
 09999^2 + 200^2 &= 1\ 0001^2 \\
 12\ 09999^2 + 2200^2 &= 121\ 0001^2 \\
 1232\ 09999^2 + 22200^2 &= 12321\ 0001^2 \\
 123432\ 09999^2 + 222200^2 &= 1234321\ 0001^2 \\
 12345432\ 09999^2 + 2222200^2 &= 123454321\ 0001^2 \\
 1234565432\ 09999^2 + 22222200^2 &= 12345654321\ 0001^2 \\
 123456765432\ 09999^2 + 222222200^2 &= 1234567654321\ 0001^2 \\
 12345678765432\ 09999^2 + 2222222200^2 &= 123456787654321\ 0001^2 \\
 1234567898765432\ 09999^2 + 22222222200^2 &= 12345678987654321\ 0001^2 \tag{4.1}
 \end{aligned}$$

$$\begin{aligned}
 09996^2 + 400^2 &= 10004^2 \\
 1209996^2 + 4400^2 &= 1210004^2 \\
 123209996^2 + 44400^2 &= 123210004^2 \\
 12343209996^2 + 444400^2 &= 12343210004^2 \\
 1234543209996^2 + 4444400^2 &= 1234543210004^2 \\
 123456543209996^2 + 44444400^2 &= 123456543210004^2 \\
 12345676543209996^2 + 444444400^2 &= 12345676543210004^2 \\
 1234567876543209996^2 + 4444444400^2 &= 1234567876543210004^2 \\
 123456789876543209996^2 + 44444444400^2 &= 123456789876543210004^2 \tag{4.2}
 \end{aligned}$$

$$\begin{aligned}
 09991^2 + 600^2 &= 10009^2 \\
 1209991^2 + 6600^2 &= 1210009^2 \\
 123209991^2 + 66600^2 &= 123210009^2 \\
 12343209991^2 + 666600^2 &= 12343210009^2 \\
 1234543209991^2 + 6666600^2 &= 1234543210009^2 \\
 123456543209991^2 + 66666600^2 &= 123456543210009^2 \\
 12345676543209991^2 + 666666600^2 &= 12345676543210009^2 \\
 1234567876543209991^2 + 6666666600^2 &= 1234567876543210009^2 \\
 123456789876543209991^2 + 66666666600^2 &= 123456789876543210009^2 \tag{4.3}
 \end{aligned}$$

$$\begin{aligned}
 09984^2 + 800^2 &= 10016^2 \\
 1209984^2 + 8800^2 &= 1210016^2 \\
 123209984^2 + 88800^2 &= 123210016^2 \\
 12343209984^2 + 888800^2 &= 12343210016^2 \\
 1234543209984^2 + 8888800^2 &= 1234543210016^2 \\
 12345676543209984^2 + 88888800^2 &= 12345676543210016^2 \\
 1234567876543209984^2 + 888888800^2 &= 1234567876543210016^2 \\
 123456789876543209984^2 + 8888888800^2 &= 123456789876543210016^2 \tag{4.4}
 \end{aligned}$$

$$\begin{aligned}
 09975^2 + 1000^2 &= 10025^2 \\
 1209975^2 + 11000^2 &= 1210025^2 \\
 123209975^2 + 111000^2 &= 123210025^2 \\
 12343209975^2 + 1111000^2 &= 12343210025^2 \\
 1234543209975^2 + 11111000^2 &= 1234543210025^2 \\
 123456543209975^2 + 111111000^2 &= 123456543210025^2 \\
 12345676543209975^2 + 1111111000^2 &= 12345676543210025^2 \\
 1234567876543209975^2 + 11111111000^2 &= 1234567876543210025^2 \\
 123456789876543209975^2 + 111111111000^2 &= 123456789876543210025^2 \tag{4.5}
 \end{aligned}$$

$$\begin{aligned}
 09964^2 + 1200^2 &= 10036^2 \\
 1209964^2 + 13200^2 &= 1210036^2 \\
 123209964^2 + 133200^2 &= 123210036^2 \\
 12343209964^2 + 1333200^2 &= 12343210036^2 \\
 1234543209964^2 + 13333200^2 &= 1234543210036^2 \\
 123456543209964^2 + 133333200^2 &= 123456543210036^2 \\
 12345676543209964^2 + 1333333200^2 &= 12345676543210036^2 \\
 1234567876543209964^2 + 13333333200^2 &= 1234567876543210036^2 \\
 123456789876543209964^2 + 133333333200^2 &= 123456789876543210036^2
 \end{aligned} \tag{4.6}$$

$$\begin{aligned}
 09951^2 + 1400^2 &= 149^2 \\
 1209951^2 + 15400^2 &= 1210049^2 \\
 123209951^2 + 155400^2 &= 123210049^2 \\
 12343209951^2 + 1555400^2 &= 12343210049^2 \\
 1234543209951^2 + 15555400^2 &= 1234543210049^2 \\
 123456543209951^2 + 155555400^2 &= 123456543210049^2 \\
 12345676543209951^2 + 1555555400^2 &= 12345676543210049^2 \\
 1234567876543209951^2 + 15555555400^2 &= 1234567876543210049^2 \\
 123456789876543209951^2 + 155555555400^2 &= 123456789876543210049^2
 \end{aligned} \tag{4.7}$$

$$\begin{aligned}
 09936^2 + 1600^2 &= 10064^2 \\
 1209936^2 + 17600^2 &= 1210064^2 \\
 123209936^2 + 177600^2 &= 123210064^2 \\
 12343209936^2 + 1777600^2 &= 12343210064^2 \\
 1234543209936^2 + 17777600^2 &= 1234543210064^2 \\
 123456543209936^2 + 177777600^2 &= 123456543210064^2 \\
 12345676543209936^2 + 1777777600^2 &= 12345676543210064^2 \\
 1234567876543209936^2 + 17777777600^2 &= 1234567876543210064^2 \\
 123456789876543209936^2 + 177777777600^2 &= 123456789876543210064^2
 \end{aligned} \tag{4.8}$$

$$\begin{aligned}
 09919^2 + 1800^2 &= \mathbf{1} 81^2 \\
 1209919^2 + 19800^2 &= \mathbf{121} 0081^2 \\
 123209919^2 + 199800^2 &= \mathbf{12321} 0081^2 \\
 12343209919^2 + 1999800^2 &= \mathbf{1234321} 0081^2 \\
 1234543209919^2 + 19999800^2 &= \mathbf{123454321} 0081^2 \\
 123456543209919^2 + 199999800^2 &= \mathbf{12345654321} 0081^2 \\
 12345676543209919^2 + 1999999800^2 &= \mathbf{1234567654321} 0081^2 \\
 1234567876543209919^2 + 19999999800^2 &= \mathbf{123456787654321} 0081^2 \\
 123456789876543209919^2 + 199999999800^2 &= \mathbf{12345678987654321} 0081^2 \tag{4.9}
 \end{aligned}$$

$$\begin{aligned}
 09900^2 + 2000^2 &= \mathbf{1} 0100^2 \\
 1209900^2 + 22000^2 &= \mathbf{121} 0100^2 \\
 123209900^2 + 222000^2 &= \mathbf{12321} 0100^2 \\
 12343209900^2 + 2222000^2 &= \mathbf{1234321} 0100^2 \\
 1234543209900^2 + 22222000^2 &= \mathbf{123454321} 0100^2 \\
 123456543209900^2 + 222222000^2 &= \mathbf{12345654321} 0100^2 \\
 12345676543209900^2 + 2222222000^2 &= \mathbf{1234567654321} 0100^2 \\
 1234567876543209900^2 + 22222222000^2 &= \mathbf{123456787654321} 0100^2 \\
 123456789876543209900^2 + 222222222000^2 &= \mathbf{12345678987654321} 0100^2 \tag{4.10}
 \end{aligned}$$

$$\begin{aligned}
 09879^2 + 2200^2 &= \mathbf{1} 0121^2 \\
 1209879^2 + 24200^2 &= \mathbf{121} 0121^2 \\
 123209879^2 + 244200^2 &= \mathbf{12321} 0121^2 \\
 12343209879^2 + 2444200^2 &= \mathbf{1234321} 0121^2 \\
 1234543209879^2 + 24444200^2 &= \mathbf{123454321} 0121^2 \\
 123456543209879^2 + 244444200^2 &= \mathbf{12345654321} 0121^2 \\
 12345676543209879^2 + 2444444200^2 &= \mathbf{1234567654321} 0121^2 \\
 1234567876543209879^2 + 24444444200^2 &= \mathbf{123456787654321} 0121^2 \tag{4.11}
 \end{aligned}$$

$$\begin{aligned}
 09856^2 + 2400^2 &= \mathbf{1} 0144^2 \\
 1209856^2 + 26400^2 &= \mathbf{121} 0144^2 \\
 123209856^2 + 266400^2 &= \mathbf{12321} 0144^2 \\
 12343209856^2 + 2666400^2 &= \mathbf{1234321} 0144^2 \\
 1234543209856^2 + 26666400^2 &= \mathbf{123454321} 0144^2 \\
 123456543209856^2 + 26666400^2 &= \mathbf{12345654321} 0144^2 \\
 12345676543209856^2 + 266666400^2 &= \mathbf{1234567654321} 0144^2 \\
 1234567876543209856^2 + 2666666400^2 &= \mathbf{123456787654321} 0144^2 \\
 123456789876543209856^2 + 26666666400^2 &= \mathbf{12345678987654321} 0144^2 \tag{4.12}
 \end{aligned}$$

$$\begin{aligned}
 09831^2 + 2600^2 &= 10169^2 \\
 1209831^2 + 28600^2 &= 1210169^2 \\
 123209831^2 + 288600^2 &= 123210169^2 \\
 12343209831^2 + 2888600^2 &= 12343210169^2 \\
 1234543209831^2 + 28888600^2 &= 1234543210169^2 \\
 123431543209831^2 + 28888600^2 &= 123431543210169^2 \\
 12343176543209831^2 + 288888600^2 &= 12343176543210169^2 \\
 1234317876543209831^2 + 2888888600^2 &= 1234317876543210169^2 \\
 123431789876543209831^2 + 28888888600^2 &= 123431789876543210169^2
 \end{aligned} \tag{4.13}$$

$$\begin{aligned}
 09804^2 + 2800^2 &= 10196^2 \\
 1209804^2 + 30800^2 &= 1210196^2 \\
 123209804^2 + 310800^2 &= 123210196^2 \\
 12343209804^2 + 3110800^2 &= 12343210196^2 \\
 1234543209804^2 + 31110800^2 &= 1234543210196^2 \\
 123456543209804^2 + 311110800^2 &= 123404543210196^2 \\
 12345676543209804^2 + 3111110800^2 &= 12340476543210196^2 \\
 1234567876543209804^2 + 31111110800^2 &= 1234047876543210196^2 \\
 123456789876543209804^2 + 311111110800^2 &= 123404789876543210196^2
 \end{aligned} \tag{4.14}$$

$$\begin{aligned}
 09775^2 + 3300^2 &= 10225^2 \\
 1209775^2 + 33000^2 &= 1210225^2 \\
 123209775^2 + 333000^2 &= 123210225^2 \\
 12343209775^2 + 3333000^2 &= 12343210225^2 \\
 1234543209775^2 + 33333000^2 &= 1234543210225^2 \\
 123404543209775^2 + 333333000^2 &= 123404543210225^2 \\
 12340476543209775^2 + 3333333000^2 &= 12340476543210225^2 \\
 1234047876543209775^2 + 33333333000^2 &= 1234047876543210225^2 \\
 123404789876543209775^2 + 333333333000^2 &= 123404789876543210225^2
 \end{aligned} \tag{4.15}$$

$$\begin{aligned}
 09744^2 + 3200^2 &= 10256^2 \\
 1209744^2 + 35200^2 &= 1210256^2 \\
 123209744^2 + 355200^2 &= 123210256^2 \\
 12343209744^2 + 3555200^2 &= 12343210256^2 \\
 1234543209744^2 + 35555200^2 &= 1234543210256^2 \\
 123404543209744^2 + 355555200^2 &= 123404543210256^2 \\
 12340476543209744^2 + 3555555200^2 &= 12340476543210256^2 \\
 1234047876543209744^2 + 35555555200^2 &= 1234047876543210256^2 \\
 123404789876543209744^2 + 355555555200^2 &= 123404789876543210256^2 \tag{4.16}
 \end{aligned}$$

$$\begin{aligned}
 09711^2 + 3400^2 &= 10289^2 \\
 1209711^2 + 37400^2 &= 1210289^2 \\
 123209711^2 + 377400^2 &= 123210289^2 \\
 12343209711^2 + 3777400^2 &= 12343210289^2 \\
 1234543209711^2 + 37777400^2 &= 1234543210289^2 \\
 123404543209711^2 + 377777400^2 &= 123404543210289^2 \\
 12340476543209711^2 + 3777777400^2 &= 12340476543210289^2 \\
 1234047876543209711^2 + 37777777400^2 &= 1234047876543210289^2 \\
 123404789876543209711^2 + 377777777400^2 &= 123404789876543210289^2 \tag{4.17}
 \end{aligned}$$

$$\begin{aligned}
 09676^2 + 3600^2 &= 10324^2 \\
 1209676^2 + 39600^2 &= 1210324^2 \\
 123209676^2 + 399600^2 &= 123210324^2 \\
 12343209676^2 + 3999600^2 &= 12343210324^2 \\
 1234543209676^2 + 39999600^2 &= 1234543210324^2 \\
 123456543209676^2 + 399999600^2 &= 123404543210324^2 \\
 12345676543209676^2 + 3999999600^2 &= 12340476543210324^2 \\
 1234567876543209676^2 + 39999999600^2 &= 1234047876543210324^2 \\
 123456789876543209676^2 + 399999999600^2 &= 123404789876543210324^2 \tag{4.18}
 \end{aligned}$$

$$\begin{aligned}
 09639^2 + 3800^2 &= 10361^2 \\
 1209639^2 + 41800^2 &= 1210361^2 \\
 123209639^2 + 421800^2 &= 123210361^2 \\
 12343209639^2 + 4221800^2 &= 12343210361^2 \\
 1234543209639^2 + 42221800^2 &= 1234543210361^2 \\
 1234564543209639^2 + 422221800^2 &= 123404543210361^2 \\
 12345676543209639^2 + 4222221800^2 &= 12340476543210361^2 \\
 1234567876543209639^2 + 42222221800^2 &= 1234047876543210361^2 \\
 123456789876543209639^2 + 422222221800^2 &= 123404789876543210361^2 \tag{4.19}
 \end{aligned}$$

4.1.2 For $n = 20, 21, 23, \dots, 97, 98, 99$:

Let's consider

$$m = 100, 1100, 11100, 111100, 1111100, 11111100, 111111100, 1111111100$$

in (1.1), then for each value of $n = 20, 21, 23, \dots, 97, 98, 99$; there are 80 *palindromic-type pandigital Pythagorean patterns* given below. In each case, only first four values are written. The other 5 values can be written on similar lines as done in subsection 4.1.1.

$$\begin{aligned} 09600^2 + 4000^2 &= 10400^2 \\ 1209600^2 + 44000^2 &= 1210400^2 \\ 123209600^2 + 444000^2 &= 123210400^2 \\ 12343209600^2 + 4444000^2 &= 12343210400^2 \end{aligned} \quad (4.20)$$

$$\begin{aligned} 09559^2 + 4200^2 &= 10441^2 \\ 1209559^2 + 46200^2 &= 1210441^2 \\ 123209559^2 + 466200^2 &= 123210441^2 \\ 12343209559^2 + 4666200^2 &= 12343210441^2 \end{aligned} \quad (4.21)$$

$$\begin{aligned} 09516^2 + 4400^2 &= 10484^2 \\ 1209516^2 + 48400^2 &= 1210484^2 \\ 123209516^2 + 488400^2 &= 123210484^2 \\ 12343209516^2 + 4888400^2 &= 12343210484^2 \end{aligned} \quad (4.22)$$

$$\begin{aligned} 09471^2 + 4600^2 &= 10529^2 \\ 1209471^2 + 50600^2 &= 1210529^2 \\ 123209471^2 + 510600^2 &= 123210529^2 \\ 12343209471^2 + 5110600^2 &= 12343210529^2 \end{aligned} \quad (4.23)$$

$$\begin{aligned} 09424^2 + 4800^2 &= 10576^2 \\ 1209424^2 + 52800^2 &= 1210576^2 \\ 123209424^2 + 532800^2 &= 123210576^2 \\ 12343209424^2 + 5332800^2 &= 12343210576^2 \end{aligned} \quad (4.24)$$

$$\begin{aligned} 09375^2 + 5000^2 &= 10625^2 \\ 1209375^2 + 55000^2 &= 1210625^2 \\ 123209375^2 + 555000^2 &= 123210625^2 \\ 12343209375^2 + 5555000^2 &= 12343210625^2 \end{aligned} \quad (4.25)$$

$$\begin{aligned} 09324^2 + 5200^2 &= 10672^2 \\ 1209324^2 + 57200^2 &= 1210672^2 \\ 123209324^2 + 577200^2 &= 123210672^2 \\ 12343209324^2 + 5777200^2 &= 12343210672^2 \end{aligned} \quad (4.26)$$

$$\begin{aligned} 09271^2 + 5400^2 &= 10729^2 \\ 1209271^2 + 59400^2 &= 1210729^2 \\ 123209271^2 + 599400^2 &= 123210729^2 \\ 12343209271^2 + 5999400^2 &= 12343210729^2 \end{aligned} \quad (4.27)$$

$$\begin{aligned} 09216^2 + 5600^2 &= 10784^2 \\ 1209216^2 + 61600^2 &= 1210784^2 \\ 123209216^2 + 621600^2 &= 123210784^2 \\ 12343209216^2 + 6221600^2 &= 12343210784^2 \end{aligned} \quad (4.28)$$

$$\begin{aligned} 09159^2 + 5800^2 &= 10841^2 \\ 1209159^2 + 63800^2 &= 1210841^2 \\ 123209159^2 + 643800^2 &= 123210841^2 \\ 12343209159^2 + 6443800^2 &= 12343210841^2 \end{aligned} \quad (4.29)$$

$$\begin{aligned} 09100^2 + 6000^2 &= 10900^2 \\ 1209100^2 + 66000^2 &= 1210900^2 \\ 123209100^2 + 666000^2 &= 123210900^2 \\ 12343209100^2 + 6666000^2 &= 12343210900^2 \end{aligned} \quad (4.30)$$

$$\begin{aligned} 09039^2 + 6200^2 &= 10961^2 \\ 1209039^2 + 68200^2 &= 1210961^2 \\ 123209039^2 + 688200^2 &= 123210961^2 \\ 12343209039^2 + 6888200^2 &= 12343210961^2 \end{aligned} \quad (4.31)$$

$$\begin{aligned} 08976^2 + 6400^2 &= 11024^2 \\ 1208976^2 + 70400^2 &= 1211024^2 \\ 123208976^2 + 710400^2 &= 123211024^2 \\ 12343208976^2 + 7110400^2 &= 12343211024^2 \end{aligned} \quad (4.32)$$

$$\begin{aligned}
 08911^2 + 6600^2 &= \mathbf{1} 1089^2 \\
 12 08911^2 + 72600^2 &= \mathbf{121} 1089^2 \\
 1232 08911^2 + 732600^2 &= \mathbf{12321} 1089^2 \\
 123432 08911^2 + 7332600^2 &= \mathbf{1234321} 1089^2 \quad (4.33)
 \end{aligned}
 \qquad
 \begin{aligned}
 08319^2 + 8200^2 &= \mathbf{1} 1681^2 \\
 12 08319^2 + 90200^2 &= \mathbf{121} 1681^2 \\
 1232 08319^2 + 910200^2 &= \mathbf{12321} 1681^2 \\
 123432 08319^2 + 9110200^2 &= \mathbf{1234321} 1681^2 \quad (4.41)
 \end{aligned}$$

$$\begin{aligned}
 08844^2 + 6800^2 &= \mathbf{1} 1156^2 \\
 12 08844^2 + 74800^2 &= \mathbf{121} 1156^2 \\
 1232 08844^2 + 754800^2 &= \mathbf{12321} 1156^2 \\
 123432 08844^2 + 7554800^2 &= \mathbf{1234321} 1156^2 \quad (4.34)
 \end{aligned}
 \qquad
 \begin{aligned}
 08236^2 + 8400^2 &= \mathbf{1} 1764^2 \\
 12 08236^2 + 92400^2 &= \mathbf{121} 1764^2 \\
 1232 08236^2 + 932400^2 &= \mathbf{12321} 1764^2 \\
 123432 08236^2 + 9332400^2 &= \mathbf{1234321} 1764^2 \quad (4.42)
 \end{aligned}$$

$$\begin{aligned}
 08775^2 + 7000^2 &= \mathbf{1} 1225^2 \\
 12 08775^2 + 77000^2 &= \mathbf{121} 1225^2 \\
 1232 08775^2 + 777000^2 &= \mathbf{12321} 1225^2 \\
 123432 08775^2 + 7777000^2 &= \mathbf{1234321} 1225^2 \quad (4.35)
 \end{aligned}
 \qquad
 \begin{aligned}
 08151^2 + 8600^2 &= \mathbf{1} 1849^2 \\
 12 08151^2 + 94600^2 &= \mathbf{121} 1849^2 \\
 1232 08151^2 + 954600^2 &= \mathbf{12321} 1849^2 \\
 123432 08151^2 + 9554600^2 &= \mathbf{1234321} 1849^2 \quad (4.43)
 \end{aligned}$$

$$\begin{aligned}
 08704^2 + 7200^2 &= \mathbf{1} 1296^2 \\
 12 08704^2 + 79200^2 &= \mathbf{121} 1296^2 \\
 1232 08704^2 + 799200^2 &= \mathbf{12321} 1296^2 \\
 123432 08704^2 + 7999200^2 &= \mathbf{1234321} 1296^2 \quad (4.36)
 \end{aligned}
 \qquad
 \begin{aligned}
 08064^2 + 8800^2 &= \mathbf{1} 1936^2 \\
 12 08064^2 + 96800^2 &= \mathbf{121} 1936^2 \\
 1232 08064^2 + 976800^2 &= \mathbf{12321} 1936^2 \\
 123432 08064^2 + 9776800^2 &= \mathbf{1234321} 1936^2 \quad (4.44)
 \end{aligned}$$

$$\begin{aligned}
 08631^2 + 7400^2 &= \mathbf{1} 1369^2 \\
 12 08631^2 + 81400^2 &= \mathbf{121} 1369^2 \\
 1232 08631^2 + 821400^2 &= \mathbf{12321} 1369^2 \\
 123432 08631^2 + 8221400^2 &= \mathbf{1234321} 1369^2 \quad (4.37)
 \end{aligned}
 \qquad
 \begin{aligned}
 07975^2 + 9000^2 &= \mathbf{1} 2025^2 \\
 12 07975^2 + 99000^2 &= \mathbf{121} 2025^2 \\
 1232 07975^2 + 999000^2 &= \mathbf{12321} 2025^2 \\
 123432 07975^2 + 9999000^2 &= \mathbf{1234321} 2025^2 \quad (4.45)
 \end{aligned}$$

$$\begin{aligned}
 08556^2 + 7600^2 &= \mathbf{1} 1444^2 \\
 12 08556^2 + 83600^2 &= \mathbf{121} 1444^2 \\
 1232 08556^2 + 843600^2 &= \mathbf{12321} 1444^2 \\
 123432 08556^2 + 8443600^2 &= \mathbf{1234321} 1444^2 \quad (4.38)
 \end{aligned}
 \qquad
 \begin{aligned}
 07884^2 + 9200^2 &= \mathbf{1} 2116^2 \\
 12 07884^2 + 101200^2 &= \mathbf{121} 2116^2 \\
 1232 07884^2 + 1021200^2 &= \mathbf{12321} 2116^2 \\
 123432 07884^2 + 10221200^2 &= \mathbf{1234321} 2116^2 \quad (4.46)
 \end{aligned}$$

$$\begin{aligned}
 08479^2 + 7800^2 &= \mathbf{1} 1521^2 \\
 12 08479^2 + 85800^2 &= \mathbf{121} 1521^2 \\
 1232 08479^2 + 865800^2 &= \mathbf{12321} 1521^2 \\
 123432 08479^2 + 8665800^2 &= \mathbf{1234321} 1521^2 \quad (4.39)
 \end{aligned}
 \qquad
 \begin{aligned}
 07791^2 + 9400^2 &= \mathbf{1} 2209^2 \\
 12 07791^2 + 103400^2 &= \mathbf{121} 2209^2 \\
 1232 07791^2 + 1043400^2 &= \mathbf{12321} 2209^2 \\
 123432 07791^2 + 10443400^2 &= \mathbf{1234321} 2209^2 \quad (4.47)
 \end{aligned}$$

$$\begin{aligned}
 08400^2 + 8000^2 &= \mathbf{1} 1600^2 \\
 12 08400^2 + 88000^2 &= \mathbf{121} 1600^2 \\
 1232 08400^2 + 888000^2 &= \mathbf{12321} 1600^2 \\
 123432 08400^2 + 8888000^2 &= \mathbf{1234321} 1600^2 \quad (4.40)
 \end{aligned}
 \qquad
 \begin{aligned}
 07696^2 + 9600^2 &= \mathbf{1} 2304^2 \\
 12 07696^2 + 105600^2 &= \mathbf{121} 2304^2 \\
 1232 07696^2 + 1065600^2 &= \mathbf{12321} 2304^2 \\
 123432 07696^2 + 10665600^2 &= \mathbf{1234321} 2304^2 \quad (4.48)
 \end{aligned}$$

$$\begin{aligned}
 07599^2 + 9800^2 &= \mathbf{1} 2401^2 \\
 12 07599^2 + 107800^2 &= \mathbf{121} 2401^2 \\
 1232 07599^2 + 1087800^2 &= \mathbf{12321} 2401^2 \\
 123432 07599^2 + 10887800^2 &= \mathbf{1234321} 2401^2 \quad (4.49)
 \end{aligned}
 \qquad
 \begin{aligned}
 06751^2 + 11400^2 &= \mathbf{1} 3249^2 \\
 12 06751^2 + 125400^2 &= \mathbf{121} 3249^2 \\
 1232 06751^2 + 1265400^2 &= \mathbf{12321} 3249^2 \\
 123432 06751^2 + 12665400^2 &= \mathbf{1234321} 3249^2 \quad (4.57)
 \end{aligned}$$

$$\begin{aligned}
 07500^2 + 10000^2 &= \mathbf{1} 2500^2 \\
 12 07500^2 + 110000^2 &= \mathbf{121} 2500^2 \\
 1232 07500^2 + 1110000^2 &= \mathbf{12321} 2500^2 \\
 123432 07500^2 + 11110000^2 &= \mathbf{1234321} 2500^2 \quad (4.50)
 \end{aligned}
 \qquad
 \begin{aligned}
 06636^2 + 11600^2 &= \mathbf{1} 3364^2 \\
 12 06636^2 + 127600^2 &= \mathbf{121} 3364^2 \\
 1232 06636^2 + 1287600^2 &= \mathbf{12321} 3364^2 \\
 123432 06636^2 + 12887600^2 &= \mathbf{1234321} 3364^2 \quad (4.58)
 \end{aligned}$$

$$\begin{aligned}
 07399^2 + 10200^2 &= \mathbf{1} 2601^2 \\
 12 07399^2 + 112200^2 &= \mathbf{121} 2601^2 \\
 1232 07399^2 + 1132200^2 &= \mathbf{12321} 2601^2 \\
 123432 07399^2 + 11332200^2 &= \mathbf{1234321} 2601^2 \quad (4.51)
 \end{aligned}
 \qquad
 \begin{aligned}
 06519^2 + 11800^2 &= \mathbf{1} 3481^2 \\
 12 06519^2 + 129800^2 &= \mathbf{121} 3481^2 \\
 1232 06519^2 + 1309800^2 &= \mathbf{12321} 3481^2 \\
 123432 06519^2 + 13109800^2 &= \mathbf{1234321} 3481^2 \quad (4.59)
 \end{aligned}$$

$$\begin{aligned}
 07296^2 + 10400^2 &= \mathbf{1} 2704^2 \\
 12 07296^2 + 114400^2 &= \mathbf{121} 2704^2 \\
 1232 07296^2 + 1154400^2 &= \mathbf{12321} 2704^2 \\
 123432 07296^2 + 11554400^2 &= \mathbf{1234321} 2704^2 \quad (4.52)
 \end{aligned}
 \qquad
 \begin{aligned}
 06400^2 + 12000^2 &= \mathbf{1} 3600^2 \\
 12 06400^2 + 132000^2 &= \mathbf{121} 3600^2 \\
 1232 06400^2 + 1332000^2 &= \mathbf{12321} 3600^2 \\
 123432 06400^2 + 13332000^2 &= \mathbf{1234321} 3600^2 \quad (4.60)
 \end{aligned}$$

$$\begin{aligned}
 07191^2 + 10600^2 &= \mathbf{1} 2809^2 \\
 12 07191^2 + 116600^2 &= \mathbf{121} 2809^2 \\
 1232 07191^2 + 1176600^2 &= \mathbf{12321} 2809^2 \\
 123432 07191^2 + 11776600^2 &= \mathbf{1234321} 2809^2 \quad (4.53)
 \end{aligned}
 \qquad
 \begin{aligned}
 06279^2 + 12200^2 &= \mathbf{1} 3721^2 \\
 12 06279^2 + 134200^2 &= \mathbf{121} 3721^2 \\
 1232 06279^2 + 1354200^2 &= \mathbf{12321} 3721^2 \\
 123432 06279^2 + 13554200^2 &= \mathbf{1234321} 3721^2 \quad (4.61)
 \end{aligned}$$

$$\begin{aligned}
 07084^2 + 10800^2 &= \mathbf{1} 2916^2 \\
 12 07084^2 + 118800^2 &= \mathbf{121} 2916^2 \\
 1232 07084^2 + 1198800^2 &= \mathbf{12321} 2916^2 \\
 123432 07084^2 + 11998800^2 &= \mathbf{1234321} 2916^2 \quad (4.54)
 \end{aligned}
 \qquad
 \begin{aligned}
 06156^2 + 12400^2 &= \mathbf{1} 3844^2 \\
 12 06156^2 + 136400^2 &= \mathbf{121} 3844^2 \\
 1232 06156^2 + 1376400^2 &= \mathbf{12321} 3844^2 \\
 123432 06156^2 + 13776400^2 &= \mathbf{1234321} 3844^2 \quad (4.62)
 \end{aligned}$$

$$\begin{aligned}
 06975^2 + 11000^2 &= \mathbf{1} 3025^2 \\
 12 06975^2 + 121000^2 &= \mathbf{121} 3025^2 \\
 1232 06975^2 + 1221000^2 &= \mathbf{12321} 3025^2 \\
 123432 06975^2 + 12221000^2 &= \mathbf{1234321} 3025^2 \quad (4.55)
 \end{aligned}
 \qquad
 \begin{aligned}
 06031^2 + 12600^2 &= \mathbf{1} 3969^2 \\
 12 06031^2 + 138600^2 &= \mathbf{121} 3969^2 \\
 1232 06031^2 + 1398600^2 &= \mathbf{12321} 3969^2 \\
 123432 06031^2 + 13998600^2 &= \mathbf{1234321} 3969^2 \quad (4.63)
 \end{aligned}$$

$$\begin{aligned}
 06864^2 + 11200^2 &= \mathbf{1} 3136^2 \\
 12 06864^2 + 123200^2 &= \mathbf{121} 3136^2 \\
 1232 06864^2 + 1243200^2 &= \mathbf{12321} 3136^2 \\
 123432 06864^2 + 12443200^2 &= \mathbf{1234321} 3136^2 \quad (4.56)
 \end{aligned}
 \qquad
 \begin{aligned}
 05904^2 + 12800^2 &= \mathbf{1} 4096^2 \\
 12 05904^2 + 140800^2 &= \mathbf{121} 4096^2 \\
 1232 05904^2 + 1420800^2 &= \mathbf{12321} 4096^2 \\
 123432 05904^2 + 14220800^2 &= \mathbf{1234321} 4096^2 \quad (4.64)
 \end{aligned}$$

$$\begin{aligned}
 05775^2 + 13000^2 &= \mathbf{1} 4225^2 \\
 12 05775^2 + 143000^2 &= \mathbf{121} 4225^2 \\
 1232 05775^2 + 1443000^2 &= \mathbf{12321} 4225^2 \\
 123432 05775^2 + 14443000^2 &= \mathbf{1234321} 4225^2 \quad (4.65)
 \end{aligned}
 \qquad
 \begin{aligned}
 04671^2 + 14600^2 &= \mathbf{1} 5329^2 \\
 12 04671^2 + 160600^2 &= \mathbf{121} 5329^2 \\
 1232 04671^2 + 1620600^2 &= \mathbf{12321} 5329^2 \\
 123432 04671^2 + 16220600^2 &= \mathbf{1234321} 5329^2 \quad (4.73)
 \end{aligned}$$

$$\begin{aligned}
 05644^2 + 13200^2 &= \mathbf{1} 4356^2 \\
 12 05644^2 + 145200^2 &= \mathbf{121} 4356^2 \\
 1232 05644^2 + 1465200^2 &= \mathbf{12321} 4356^2 \\
 123432 05644^2 + 14665200^2 &= \mathbf{1234321} 4356^2 \quad (4.66)
 \end{aligned}
 \qquad
 \begin{aligned}
 04524^2 + 14800^2 &= \mathbf{1} 5476^2 \\
 12 04524^2 + 162800^2 &= \mathbf{121} 5476^2 \\
 1232 04524^2 + 1642800^2 &= \mathbf{12321} 5476^2 \\
 123432 04524^2 + 16442800^2 &= \mathbf{1234321} 5476^2 \quad (4.74)
 \end{aligned}$$

$$\begin{aligned}
 05511^2 + 13400^2 &= \mathbf{1} 4489^2 \\
 12 05511^2 + 147400^2 &= \mathbf{121} 4489^2 \\
 1232 05511^2 + 1487400^2 &= \mathbf{12321} 4489^2 \\
 123432 05511^2 + 14887400^2 &= \mathbf{1234321} 4489^2 \quad (4.67)
 \end{aligned}
 \qquad
 \begin{aligned}
 04375^2 + 15000^2 &= \mathbf{1} 5625^2 \\
 12 04375^2 + 165000^2 &= \mathbf{121} 5625^2 \\
 1232 04375^2 + 1665000^2 &= \mathbf{12321} 5625^2 \\
 123432 04375^2 + 16665000^2 &= \mathbf{1234321} 5625^2 \quad (4.75)
 \end{aligned}$$

$$\begin{aligned}
 05376^2 + 13600^2 &= \mathbf{1} 4624^2 \\
 12 05376^2 + 149600^2 &= \mathbf{121} 4624^2 \\
 1232 05376^2 + 1509600^2 &= \mathbf{12321} 4624^2 \\
 123432 05376^2 + 15109600^2 &= \mathbf{1234321} 4624^2 \quad (4.68)
 \end{aligned}
 \qquad
 \begin{aligned}
 04224^2 + 15200^2 &= \mathbf{1} 5776^2 \\
 12 04224^2 + 167200^2 &= \mathbf{121} 5776^2 \\
 1232 04224^2 + 1687200^2 &= \mathbf{12321} 5776^2 \\
 123432 04224^2 + 16887200^2 &= \mathbf{1234321} 5776^2 \quad (4.76)
 \end{aligned}$$

$$\begin{aligned}
 05239^2 + 13800^2 &= \mathbf{1} 4761^2 \\
 12 05239^2 + 151800^2 &= \mathbf{121} 4761^2 \\
 1232 05239^2 + 1531800^2 &= \mathbf{12321} 4761^2 \\
 123432 05239^2 + 15331800^2 &= \mathbf{1234321} 4761^2 \quad (4.69)
 \end{aligned}
 \qquad
 \begin{aligned}
 04071^2 + 15400^2 &= \mathbf{1} 5929^2 \\
 12 04071^2 + 169400^2 &= \mathbf{121} 5929^2 \\
 1232 04071^2 + 1709400^2 &= \mathbf{12321} 5929^2 \\
 123432 04071^2 + 17109400^2 &= \mathbf{1234321} 5929^2 \quad (4.77)
 \end{aligned}$$

$$\begin{aligned}
 05100^2 + 14000^2 &= \mathbf{1} 4900^2 \\
 12 05100^2 + 154000^2 &= \mathbf{121} 4900^2 \\
 1232 05100^2 + 1554000^2 &= \mathbf{12321} 4900^2 \\
 123432 05100^2 + 15554000^2 &= \mathbf{1234321} 4900^2 \quad (4.70)
 \end{aligned}
 \qquad
 \begin{aligned}
 03916^2 + 15600^2 &= \mathbf{1} 6084^2 \\
 12 03916^2 + 171600^2 &= \mathbf{121} 6084^2 \\
 1232 03916^2 + 1731600^2 &= \mathbf{12321} 6084^2 \\
 123432 03916^2 + 17331600^2 &= \mathbf{1234321} 6084^2 \quad (4.78)
 \end{aligned}$$

$$\begin{aligned}
 04959^2 + 14200^2 &= \mathbf{1} 5041^2 \\
 12 04959^2 + 156200^2 &= \mathbf{121} 5041^2 \\
 1232 04959^2 + 1576200^2 &= \mathbf{12321} 5041^2 \\
 123432 04959^2 + 15776200^2 &= \mathbf{1234321} 5041^2 \quad (4.71)
 \end{aligned}
 \qquad
 \begin{aligned}
 03759^2 + 15800^2 &= \mathbf{1} 6241^2 \\
 12 03759^2 + 173800^2 &= \mathbf{121} 6241^2 \\
 1232 03759^2 + 1753800^2 &= \mathbf{12321} 6241^2 \\
 123432 03759^2 + 17553800^2 &= \mathbf{1234321} 6241^2 \quad (4.79)
 \end{aligned}$$

$$\begin{aligned}
 04816^2 + 14400^2 &= \mathbf{1} 5184^2 \\
 12 04816^2 + 158400^2 &= \mathbf{121} 5184^2 \\
 1232 04816^2 + 1598400^2 &= \mathbf{12321} 5184^2 \\
 123432 04816^2 + 15998400^2 &= \mathbf{1234321} 5184^2 \quad (4.72)
 \end{aligned}
 \qquad
 \begin{aligned}
 03600^2 + 16000^2 &= \mathbf{1} 6400^2 \\
 12 03600^2 + 176000^2 &= \mathbf{121} 6400^2 \\
 1232 03600^2 + 1776000^2 &= \mathbf{12321} 6400^2 \\
 123432 03600^2 + 17776000^2 &= \mathbf{1234321} 6400^2 \quad (4.80)
 \end{aligned}$$

$03439^2 + 16200^2 = \mathbf{1} 6561^2$	$02079^2 + 17800^2 = \mathbf{1} 7921^2$
$12 03439^2 + 178200^2 = \mathbf{121} 6561^2$	$12 02079^2 + 195800^2 = \mathbf{121} 7921^2$
$1232 03439^2 + 1798200^2 = \mathbf{12321} 6561^2$	$1232 02079^2 + 1975800^2 = \mathbf{12321} 7921^2$
$123432 03439^2 + 17998200^2 = \mathbf{1234321} 6561^2 \quad (4.81)$	$123432 02079^2 + 19775800^2 = \mathbf{1234321} 7921^2 \quad (4.89)$
$03276^2 + 16400^2 = \mathbf{1} 6724^2$	$01900^2 + 18000^2 = \mathbf{1} 8100^2$
$12 03276^2 + 180400^2 = \mathbf{121} 6724^2$	$12 01900^2 + 198000^2 = \mathbf{121} 8100^2$
$1232 03276^2 + 1820400^2 = \mathbf{12321} 6724^2$	$1232 01900^2 + 1998000^2 = \mathbf{12321} 8100^2$
$123432 03276^2 + 18220400^2 = \mathbf{1234321} 6724^2 \quad (4.82)$	$123432 01900^2 + 19998000^2 = \mathbf{1234321} 8100^2 \quad (4.90)$
$03111^2 + 16600^2 = \mathbf{1} 6889^2$	$01719^2 + 18200^2 = \mathbf{1} 8281^2$
$12 03111^2 + 182600^2 = \mathbf{121} 6889^2$	$12 01719^2 + 200200^2 = \mathbf{121} 8281^2$
$1232 03111^2 + 1842600^2 = \mathbf{12321} 6889^2$	$1232 01719^2 + 2020200^2 = \mathbf{12321} 8281^2$
$123432 03111^2 + 18442600^2 = \mathbf{1234321} 6889^2 \quad (4.83)$	$123432 01719^2 + 20220200^2 = \mathbf{1234321} 8281^2 \quad (4.91)$
$02944^2 + 16800^2 = \mathbf{1} 7056^2$	$01536^2 + 18400^2 = \mathbf{1} 8464^2$
$12 02944^2 + 184800^2 = \mathbf{121} 7056^2$	$12 01536^2 + 202400^2 = \mathbf{121} 8464^2$
$1232 02944^2 + 1864800^2 = \mathbf{12321} 7056^2$	$1232 01536^2 + 2042400^2 = \mathbf{12321} 8464^2$
$123432 02944^2 + 18664800^2 = \mathbf{1234321} 7056^2 \quad (4.84)$	$123432 01536^2 + 20442400^2 = \mathbf{1234321} 8464^2 \quad (4.92)$
$02775^2 + 17000^2 = \mathbf{1} 7225^2$	$01351^2 + 18600^2 = \mathbf{1} 8649^2$
$12 02775^2 + 187000^2 = \mathbf{121} 7225^2$	$12 01351^2 + 204600^2 = \mathbf{121} 8649^2$
$1232 02775^2 + 1887000^2 = \mathbf{12321} 7225^2$	$1232 01351^2 + 2064600^2 = \mathbf{12321} 8649^2$
$123432 02775^2 + 18887000^2 = \mathbf{1234321} 7225^2 \quad (4.85)$	$123432 01351^2 + 20664600^2 = \mathbf{1234321} 8649^2 \quad (4.93)$
$02604^2 + 17200^2 = \mathbf{1} 7396^2$	$01164^2 + 18800^2 = \mathbf{1} 8836^2$
$12 02604^2 + 189200^2 = \mathbf{121} 7396^2$	$12 01164^2 + 206800^2 = \mathbf{121} 8836^2$
$1232 02604^2 + 1909200^2 = \mathbf{12321} 7396^2$	$1232 01164^2 + 2086800^2 = \mathbf{12321} 8836^2$
$123432 02604^2 + 19109200^2 = \mathbf{1234321} 7396^2 \quad (4.86)$	$123432 01164^2 + 20886800^2 = \mathbf{1234321} 8836^2 \quad (4.94)$
$02431^2 + 17400^2 = \mathbf{1} 7569^2$	$00975^2 + 19000^2 = \mathbf{1} 9025^2$
$12 02431^2 + 191400^2 = \mathbf{121} 7569^2$	$12 00975^2 + 209000^2 = \mathbf{121} 9025^2$
$1232 02431^2 + 1931400^2 = \mathbf{12321} 7569^2$	$1232 00975^2 + 2109000^2 = \mathbf{12321} 9025^2$
$123432 02431^2 + 19331400^2 = \mathbf{1234321} 7569^2 \quad (4.87)$	$123432 00975^2 + 21109000^2 = \mathbf{1234321} 9025^2 \quad (4.95)$
$02256^2 + 17600^2 = \mathbf{1} 7744^2$	$00784^2 + 19200^2 = \mathbf{1} 9216^2$
$12 02256^2 + 193600^2 = \mathbf{121} 7744^2$	$12 00784^2 + 211200^2 = \mathbf{121} 9216^2$
$1232 02256^2 + 1953600^2 = \mathbf{12321} 7744^2$	$1232 00784^2 + 2131200^2 = \mathbf{12321} 9216^2$
$123432 02256^2 + 19553600^2 = \mathbf{1234321} 7744^2 \quad (4.88)$	$123432 00784^2 + 21331200^2 = \mathbf{1234321} 9216^2 \quad (4.96)$

$$\begin{array}{ll}
 00591^2 + 19400^2 & = 19409^2 \\
 12\ 00591^2 + 213400^2 & = 121\ 9409^2 \\
 1232\ 00591^2 + 2153400^2 & = 12321\ 9409^2 \\
 123432\ 00591^2 + 21553400^2 & = 1234321\ 9409^2 \quad (4.97) \\
 \\
 00199^2 + 19800^2 & = 19801^2 \\
 12\ 00199^2 + 217800^2 & = 121\ 9801^2 \\
 1232\ 00199^2 + 2197800^2 & = 12321\ 9801^2 \\
 123432\ 00199^2 + 21997800^2 & = 1234321\ 9801^2 \quad (4.99)
 \end{array}$$

$$\begin{array}{ll}
 00396^2 + 19600^2 & = 19604^2 \\
 12\ 00396^2 + 215600^2 & = 121\ 9604^2 \\
 1232\ 00396^2 + 2175600^2 & = 12321\ 9604^2 \\
 123432\ 00396^2 + 21775600^2 & = 1234321\ 9604^2 \quad (4.98)
 \end{array}$$

Based on above 99 results given in subsections 4.1.1 and 4.1.2, below are some remarks:

Remark 7. In many cases, the second term in first line is out of pattern, but the continuations is well patterned. From $n=20$ to 99, we have written only first four lines. The rest 5 lines follows on similar way as of $n=1$ to 19 given in subsection 4.1. Also the last four digits in each case forms a perfect square. See below:

$$\begin{array}{ll}
 \text{Equation (3.1)} & \Rightarrow 0001 = 1^2 \\
 \text{Equation (3.2)} & \Rightarrow 0004 = 2^2 \\
 \text{Equation (3.3)} & \Rightarrow 0009 = 3^2 \\
 \dots & \dots \\
 \dots & \dots \\
 \text{Equation (3.97)} & \Rightarrow 9409 = 97^2 \\
 \text{Equation (3.98)} & \Rightarrow 9604 = 98^2 \\
 \text{Equation (3.99)} & \Rightarrow 9801 = 99^2.
 \end{array}$$

5 Third Group

Below are 999 examples of **pattern in Pythagorean triples** with 9 digits from 1 to 9 written as **palindromic-type**, where the **first line** of first pattern is the same as **third line** of example (2.1). Moreover, this section is an extension of subsection 2.3. First 19 examples are complete. Then from 20 to 999, the results are written in reduced form. These can be completed on similar lines.

5.1 For $n = 1, 2, 3, \dots, 97, 98, 99$:

This subsection is divided in two parts. The first part give first 19 results give complete patterns. The other 80 are with first four lines.

5.1.1 For $n = 1, 2, 3, \dots, 17, 18, 19$:

Let's consider

$$m = 1000, 11000, 111000, 1111000, 11111000, 111111000, 1111111000, 11111111000$$

in (1.1), then for each value of $n = 1, 2, 3, \dots, 17, 18, 19$; there are 19 *palindromic-type pandigital Pythagorean patterns* given below:

$$\begin{aligned}
 0999999^2 + 2000^2 &= 1000001^2 \\
 120999999^2 + 22000^2 &= 121000001^2 \\
 1232099999^2 + 222000^2 &= 12321000001^2 \\
 123432099999^2 + 2222000^2 &= 1234321000001^2 \\
 12345432099999^2 + 22222000^2 &= 123454321000001^2 \\
 1234565432099999^2 + 222222000^2 &= 12345654321000001^2 \\
 123456765432099999^2 + 2222222000^2 &= 1234567654321000001^2 \\
 12345678765432099999^2 + 22222222000^2 &= 123456787654321000001^2 \\
 1234567898765432099999^2 + 222222222000^2 &= 12345678987654321000001^2
 \end{aligned} \tag{5.1}$$

$$\begin{aligned}
 0999996^2 + 4000^2 &= 1000004^2 \\
 120999996^2 + 44000^2 &= 121000004^2 \\
 1232099996^2 + 444000^2 &= 12321000004^2 \\
 123432099996^2 + 4444000^2 &= 1234321000004^2 \\
 12345432099996^2 + 44444000^2 &= 123454321000004^2 \\
 1234565432099996^2 + 444444000^2 &= 12345654321000004^2 \\
 123456765432099996^2 + 4444444000^2 &= 1234567654321000004^2 \\
 12345678765432099996^2 + 44444444000^2 &= 123456787654321000004^2 \\
 1234567898765432099996^2 + 444444444000^2 &= 12345678987654321000004^2
 \end{aligned} \tag{5.2}$$

$$\begin{aligned}
 0999991^2 + 6000^2 &= 1000009^2 \\
 120999991^2 + 66000^2 &= 121000009^2 \\
 1232099991^2 + 666000^2 &= 12321000009^2 \\
 123432099991^2 + 6666000^2 &= 1234321000009^2 \\
 12345432099991^2 + 66666000^2 &= 123454321000009^2 \\
 1234565432099991^2 + 666666000^2 &= 12345654321000009^2 \\
 123456765432099991^2 + 6666666000^2 &= 1234567654321000009^2 \\
 12345678765432099991^2 + 66666666000^2 &= 123456787654321000009^2 \\
 1234567898765432099991^2 + 666666666000^2 &= 12345678987654321000009^2
 \end{aligned} \tag{5.3}$$

$$\begin{aligned}
 0999984^2 + 8000^2 &= 1000016^2 \\
 120999984^2 + 88000^2 &= 121000016^2 \\
 12320999984^2 + 888000^2 &= 12321000016^2 \\
 1234320999984^2 + 8888000^2 &= 1234321000016^2 \\
 123454320999984^2 + 88888000^2 &= 123454321000016^2 \\
 12345654320999984^2 + 888888000^2 &= 12345654321000016^2 \\
 1234567654320999984^2 + 8888888000^2 &= 1234567654321000016^2 \\
 123456787654320999984^2 + 88888888000^2 &= 123456787654321000016^2 \\
 12345678987654320999984^2 + 888888888000^2 &= 12345678987654321000016^2
 \end{aligned} \tag{5.4}$$

$$\begin{aligned}
 0999975^2 + 10000^2 &= 1000025^2 \\
 120999975^2 + 110000^2 &= 121000025^2 \\
 12320999975^2 + 1110000^2 &= 12321000025^2 \\
 1234320999975^2 + 11110000^2 &= 1234321000025^2 \\
 123454320999975^2 + 111110000^2 &= 123454321000025^2 \\
 12345654320999975^2 + 1111110000^2 &= 12345654321000025^2 \\
 1234567654320999975^2 + 11111110000^2 &= 1234567654321000025^2 \\
 123456787654320999975^2 + 111111110000^2 &= 123456787654321000025^2 \\
 12345678987654320999975^2 + 1111111110000^2 &= 12345678987654321000025^2
 \end{aligned} \tag{5.5}$$

$$\begin{aligned}
 0999964^2 + 12000^2 &= 1000036^2 \\
 120999964^2 + 132000^2 &= 121000036^2 \\
 12320999964^2 + 1332000^2 &= 12321000036^2 \\
 1234320999964^2 + 13332000^2 &= 1234321000036^2 \\
 123454320999964^2 + 133332000^2 &= 123454321000036^2 \\
 12345654320999964^2 + 1333332000^2 &= 12345654321000036^2 \\
 1234567654320999964^2 + 13333332000^2 &= 1234567654321000036^2 \\
 123456787654320999964^2 + 133333332000^2 &= 123456787654321000036^2 \\
 12345678987654320999964^2 + 1333333332000^2 &= 12345678987654321000036^2
 \end{aligned} \tag{5.6}$$

$$\begin{aligned}
 0999951^2 + 14000^2 &= 1000049^2 \\
 120999951^2 + 154000^2 &= 121000049^2 \\
 12320999951^2 + 1554000^2 &= 12321000049^2 \\
 1234320999951^2 + 15554000^2 &= 1234321000049^2 \\
 123454320999951^2 + 155554000^2 &= 123454321000049^2 \\
 12345654320999951^2 + 1555554000^2 &= 12345654321000049^2 \\
 1234567654320999951^2 + 15555554000^2 &= 1234567654321000049^2 \\
 123456787654320999951^2 + 155555554000^2 &= 123456787654321000049^2 \\
 12345678987654320999951^2 + 1555555554000^2 &= 12345678987654321000049^2
 \end{aligned} \tag{5.7}$$

$$\begin{aligned}
 0999936^2 + 16000^2 &= 1000064^2 \\
 120999936^2 + 176000^2 &= 121000064^2 \\
 12320999936^2 + 1776000^2 &= 12321000064^2 \\
 1234320999936^2 + 17776000^2 &= 1234321000064^2 \\
 123454320999936^2 + 177776000^2 &= 123454321000064^2 \\
 12345654320999936^2 + 1777776000^2 &= 12345654321000064^2 \\
 1234567654320999936^2 + 17777776000^2 &= 1234567654321000064^2 \\
 123456787654320999936^2 + 177777776000^2 &= 123456787654321000064^2 \\
 12345678987654320999936^2 + 1777777776000^2 &= 12345678987654321000064^2
 \end{aligned} \tag{5.8}$$

$$\begin{aligned}
 0999919^2 + 18000^2 &= 1000081^2 \\
 120999919^2 + 198000^2 &= 121000081^2 \\
 12320999919^2 + 1998000^2 &= 12321000081^2 \\
 1234320999919^2 + 19998000^2 &= 1234321000081^2 \\
 123454320999919^2 + 199998000^2 &= 123454321000081^2 \\
 12345654320999919^2 + 1999998000^2 &= 12345654321000081^2 \\
 1234567654320999919^2 + 19999998000^2 &= 1234567654321000081^2 \\
 123456787654320999919^2 + 199999998000^2 &= 123456787654321000081^2 \\
 12345678987654320999919^2 + 1999999998000^2 &= 12345678987654321000081^2
 \end{aligned} \tag{5.9}$$

$$\begin{aligned}
 0999900^2 + 20000^2 &= 1000100^2 \\
 120999900^2 + 220000^2 &= 121000100^2 \\
 12320999900^2 + 2220000^2 &= 12321000100^2 \\
 1234320999900^2 + 22220000^2 &= 1234321000100^2 \\
 123454320999900^2 + 222220000^2 &= 123454321000100^2 \\
 12345654320999900^2 + 2222220000^2 &= 12345654321000100^2 \\
 1234567654320999900^2 + 22222220000^2 &= 1234567654321000100^2 \\
 123456787654320999900^2 + 222222220000^2 &= 123456787654321000100^2 \\
 12345678987654320999900^2 + 2222222220000^2 &= 12345678987654321000100^2 \quad (5.10)
 \end{aligned}$$

$$\begin{aligned}
 0999879^2 + 22000^2 &= 1000121^2 \\
 120999879^2 + 242000^2 &= 121000121^2 \\
 12320999879^2 + 2442000^2 &= 12321000121^2 \\
 1234320999879^2 + 24442000^2 &= 1234321000121^2 \\
 123454320999879^2 + 244442000^2 &= 123454321000121^2 \\
 12345654320999879^2 + 2444442000^2 &= 12345654321000121^2 \\
 1234567654320999879^2 + 24444442000^2 &= 1234567654321000121^2 \\
 123456787654320999879^2 + 244444442000^2 &= 123456787654321000121^2 \\
 12345678987654320999879^2 + 2444444442000^2 &= 12345678987654321000121^2 \quad (5.11)
 \end{aligned}$$

$$\begin{aligned}
 0999856^2 + 24000^2 &= 1000144^2 \\
 120999856^2 + 264000^2 &= 121000144^2 \\
 12320999856^2 + 2664000^2 &= 12321000144^2 \\
 1234320999856^2 + 26664000^2 &= 1234321000144^2 \\
 123454320999856^2 + 266664000^2 &= 123454321000144^2 \\
 12345654320999856^2 + 2666664000^2 &= 12345654321000144^2 \\
 1234567654320999856^2 + 26666664000^2 &= 1234567654321000144^2 \\
 123456787654320999856^2 + 266666664000^2 &= 123456787654321000144^2 \\
 12345678987654320999856^2 + 2666666664000^2 &= 12345678987654321000144^2 \quad (5.12)
 \end{aligned}$$

$$\begin{aligned}
 0999831^2 + 26000^2 &= 1000169^2 \\
 120999831^2 + 286000^2 &= 121000169^2 \\
 12320999831^2 + 2886000^2 &= 12321000169^2 \\
 1234320999831^2 + 28886000^2 &= 1234321000169^2 \\
 123454320999831^2 + 288886000^2 &= 123454321000169^2 \\
 12345654320999831^2 + 288886000^2 &= 12345654321000169^2 \\
 1234567654320999831^2 + 2888886000^2 &= 1234567654321000169^2 \\
 123456787654320999831^2 + 28888886000^2 &= 123456787654321000169^2 \\
 12345678987654320999831^2 + 288888886000^2 &= 12345678987654321000169^2 \quad (5.13)
 \end{aligned}$$

$$\begin{aligned}
 0999804^2 + 28000^2 &= 1000196^2 \\
 120999804^2 + 308000^2 &= 121000196^2 \\
 12320999804^2 + 3108000^2 &= 12321000196^2 \\
 1234320999804^2 + 31108000^2 &= 1234321000196^2 \\
 123454320999804^2 + 311108000^2 &= 123454321000196^2 \\
 12345654320999804^2 + 3111108000^2 &= 12345654321000196^2 \\
 1234567654320999804^2 + 31111108000^2 &= 1234567654321000196^2 \\
 123456787654320999804^2 + 311111108000^2 &= 123456787654321000196^2 \quad (5.14)
 \end{aligned}$$

$$\begin{aligned}
 0999775^2 + 30000^2 &= 1000225^2 \\
 120999775^2 + 330000^2 &= 121000225^2 \\
 12320999775^2 + 3330000^2 &= 12321000225^2 \\
 1234320999775^2 + 33330000^2 &= 1234321000225^2 \\
 123454320999775^2 + 333330000^2 &= 123454321000225^2 \\
 12345654320999775^2 + 3333330000^2 &= 12345654321000225^2 \\
 1234567654320999775^2 + 33333330000^2 &= 1234567654321000225^2 \\
 123456787654320999775^2 + 333333330000^2 &= 123456787654321000225^2 \\
 12345678987654320999775^2 + 3333333330000^2 &= 12345678987654321000225^2 \quad (5.15)
 \end{aligned}$$

$$\begin{aligned}
 0999744^2 + 32000^2 &= 1000256^2 \\
 120999744^2 + 352000^2 &= 121000256^2 \\
 12320999744^2 + 3552000^2 &= 12321000256^2 \\
 1234320999744^2 + 35552000^2 &= 1234321000256^2 \\
 123454320999744^2 + 355552000^2 &= 123454321000256^2 \\
 12345654320999744^2 + 3555552000^2 &= 12345654321000256^2 \\
 1234567654320999744^2 + 35555552000^2 &= 1234567654321000256^2 \\
 123456787654320999744^2 + 355555552000^2 &= 123456787654321000256^2 \\
 12345678987654320999744^2 + 3555555552000^2 &= 12345678987654321000256^2
 \end{aligned} \tag{5.16}$$

$$\begin{aligned}
 0999711^2 + 34000^2 &= 1000289^2 \\
 120999711^2 + 374000^2 &= 121000289^2 \\
 12320999711^2 + 3774000^2 &= 12321000289^2 \\
 1234320999711^2 + 37774000^2 &= 1234321000289^2 \\
 123454320999711^2 + 377774000^2 &= 123454321000289^2 \\
 12345654320999711^2 + 3777774000^2 &= 12345654321000289^2 \\
 1234567654320999711^2 + 37777774000^2 &= 1234567654321000289^2 \\
 123456787654320999711^2 + 377777774000^2 &= 123456787654321000289^2 \\
 12345678987654320999711^2 + 3777777774000^2 &= 12345678987654321000289^2
 \end{aligned} \tag{5.17}$$

$$\begin{aligned}
 0999676^2 + 36000^2 &= 1000324^2 \\
 120999676^2 + 396000^2 &= 121000324^2 \\
 12320999676^2 + 3996000^2 &= 12321000324^2 \\
 1234320999676^2 + 39996000^2 &= 1234321000324^2 \\
 123454320999676^2 + 399996000^2 &= 123454321000324^2 \\
 12345654320999676^2 + 3999996000^2 &= 12345654321000324^2 \\
 1234567654320999676^2 + 39999996000^2 &= 1234567654321000324^2 \\
 123456787654320999676^2 + 399999996000^2 &= 123456787654321000324^2 \\
 12345678987654320999676^2 + 3999999996000^2 &= 12345678987654321000324^2
 \end{aligned} \tag{5.18}$$

$$\begin{aligned}
 & 0999639^2 + 38000^2 = 1000361^2 \\
 & 120999639^2 + 418000^2 = 121000361^2 \\
 & 12320999639^2 + 4218000^2 = 12321000361^2 \\
 & 1234320999639^2 + 42218000^2 = 1234321000361^2 \\
 & 123454320999639^2 + 422218000^2 = 123454321000361^2 \\
 & 12345654320999639^2 + 4222218000^2 = 12345654321000361^2 \\
 & 1234567654320999639^2 + 42222218000^2 = 1234567654321000361^2 \\
 & 123456787654320999639^2 + 422222218000^2 = 123456787654321000361^2 \\
 & 12345678987654320999639^2 + 4222222218000^2 = 12345678987654321000361^2 \quad (5.19)
 \end{aligned}$$

5.1.2 For $n = 20, 21, 22, \dots, 97, 98, 99$:

Let's consider

$$m = 1000, 11000, 111000, 1111000, 11111000, 111111000, 1111111000, 11111111000$$

in (1.1), then for each value of $n = 20, 21, 22, \dots, 97, 98, 99$; there are 80 *palindromic-type pandigital Pythagorean patterns* given below. In each case, only first four values are written. The other 5 values can be written on similar lines as done in subsection 5.1.

$$\begin{aligned}
 & 0999600^2 + 40000^2 = 1000400^2 & 0999375^2 + 50000^2 = 1000625^2 \\
 & 120999600^2 + 440000^2 = 121000400^2 & 120999375^2 + 550000^2 = 121000625^2 \\
 & 12320999600^2 + 4440000^2 = 12321000400^2 & 12320999375^2 + 5550000^2 = 12321000625^2 \\
 & 1234320999600^2 + 44440000^2 = 1234321000400^2 \quad (5.20) & 1234320999375^2 + 55550000^2 = 1234321000625^2 \quad (5.25) \\
 & 0999559^2 + 42000^2 = 1000441^2 & 0999324^2 + 52000^2 = 1000676^2 \\
 & 120999559^2 + 462000^2 = 121000441^2 & 120999324^2 + 572000^2 = 121000676^2 \\
 & 12320999559^2 + 4662000^2 = 12321000441^2 & 12320999324^2 + 5772000^2 = 12321000676^2 \\
 & 1234320999559^2 + 46662000^2 = 1234321000441^2 \quad (5.21) & 1234320999324^2 + 57772000^2 = 1234321000676^2 \quad (5.26) \\
 & 0999516^2 + 44000^2 = 1000484^2 & 0999271^2 + 54000^2 = 1000729^2 \\
 & 120999516^2 + 484000^2 = 121000484^2 & 120999271^2 + 594000^2 = 121000729^2 \\
 & 12320999516^2 + 4884000^2 = 12321000484^2 & 12320999271^2 + 5994000^2 = 12321000729^2 \\
 & 1234320999516^2 + 48884000^2 = 1234321000484^2 \quad (5.22) & 1234320999271^2 + 59994000^2 = 1234321000729^2 \quad (5.27) \\
 & 0999471^2 + 46000^2 = 1000529^2 & 0999216^2 + 56000^2 = 1000784^2 \\
 & 120999471^2 + 506000^2 = 121000529^2 & 120999216^2 + 616000^2 = 121000784^2 \\
 & 12320999471^2 + 5106000^2 = 12321000529^2 & 12320999216^2 + 6216000^2 = 12321000784^2 \\
 & 1234320999471^2 + 51106000^2 = 1234321000529^2 \quad (5.23) & 1234320999216^2 + 62216000^2 = 1234321000784^2 \quad (5.28) \\
 & 0999424^2 + 48000^2 = 1000576^2 \\
 & 120999424^2 + 528000^2 = 121000576^2 \\
 & 12320999424^2 + 5328000^2 = 12321000576^2 \\
 & 1234320999424^2 + 53328000^2 = 1234321000576^2 \quad (5.24)
 \end{aligned}$$

$$\begin{aligned}
 0999159^2 + 58000^2 &= 1000841^2 \\
 12\ 0999159^2 + 638000^2 &= 121\ 000841^2 \\
 1232\ 0999159^2 + 6438000^2 &= 12321\ 000841^2 \\
 123432\ 0999159^2 + 64438000^2 &= 1234321\ 000841^2 \quad (5.29)
 \end{aligned}$$

$$\begin{aligned}
 0999100^2 + 60000^2 &= 1000900^2 \\
 12\ 0999100^2 + 660000^2 &= 121\ 000900^2 \\
 1232\ 0999100^2 + 6660000^2 &= 12321\ 000900^2 \\
 123432\ 0999100^2 + 66660000^2 &= 1234321\ 000900^2 \quad (5.30)
 \end{aligned}$$

$$\begin{aligned}
 0999039^2 + 62000^2 &= 1000961^2 \\
 12\ 0999039^2 + 682000^2 &= 121\ 000961^2 \\
 1232\ 0999039^2 + 6882000^2 &= 12321\ 000961^2 \\
 123432\ 0999039^2 + 68882000^2 &= 1234321\ 000961^2 \quad (5.31)
 \end{aligned}$$

$$\begin{aligned}
 0998976^2 + 64000^2 &= 1001024^2 \\
 12\ 0998976^2 + 704000^2 &= 121\ 001024^2 \\
 1232\ 0998976^2 + 7104000^2 &= 12321\ 001024^2 \\
 123432\ 0998976^2 + 71104000^2 &= 1234321\ 001024^2 \quad (5.32)
 \end{aligned}$$

$$\begin{aligned}
 0998911^2 + 66000^2 &= 1001089^2 \\
 12\ 0998911^2 + 726000^2 &= 121\ 001089^2 \\
 1232\ 0998911^2 + 7326000^2 &= 12321\ 001089^2 \\
 123432\ 0998911^2 + 73326000^2 &= 1234321\ 001089^2 \quad (5.33)
 \end{aligned}$$

$$\begin{aligned}
 0998844^2 + 68000^2 &= 1001156^2 \\
 12\ 0998844^2 + 748000^2 &= 121\ 001156^2 \\
 1232\ 0998844^2 + 7548000^2 &= 12321\ 001156^2 \\
 123432\ 0998844^2 + 75548000^2 &= 1234321\ 001156^2 \quad (5.34)
 \end{aligned}$$

$$\begin{aligned}
 0998775^2 + 70000^2 &= 1001225^2 \\
 12\ 0998775^2 + 770000^2 &= 121\ 001225^2 \\
 1232\ 0998775^2 + 7770000^2 &= 12321\ 001225^2 \\
 123432\ 0998775^2 + 77770000^2 &= 1234321\ 001225^2 \quad (5.35)
 \end{aligned}$$

$$\begin{aligned}
 0998704^2 + 72000^2 &= 1001296^2 \\
 12\ 0998704^2 + 792000^2 &= 121\ 001296^2 \\
 1232\ 0998704^2 + 7992000^2 &= 12321\ 001296^2 \\
 123432\ 0998704^2 + 79992000^2 &= 1234321\ 001296^2 \quad (5.36)
 \end{aligned}$$

$$\begin{aligned}
 0998631^2 + 74000^2 &= 1001369^2 \\
 12\ 0998631^2 + 814000^2 &= 121\ 001369^2 \\
 1232\ 0998631^2 + 8214000^2 &= 12321\ 001369^2 \\
 123432\ 0998631^2 + 82214000^2 &= 1234321\ 001369^2 \quad (5.37)
 \end{aligned}$$

$$\begin{aligned}
 0998556^2 + 76000^2 &= 1001444^2 \\
 12\ 0998556^2 + 836000^2 &= 121\ 001444^2 \\
 1232\ 0998556^2 + 8436000^2 &= 12321\ 001444^2 \\
 123432\ 0998556^2 + 84436000^2 &= 1234321\ 001444^2 \quad (5.38)
 \end{aligned}$$

$$\begin{aligned}
 0998479^2 + 78000^2 &= 1001521^2 \\
 12\ 0998479^2 + 858000^2 &= 121\ 001521^2 \\
 1232\ 0998479^2 + 8658000^2 &= 12321\ 001521^2 \\
 123432\ 0998479^2 + 86658000^2 &= 1234321\ 001521^2 \quad (5.39)
 \end{aligned}$$

$$\begin{aligned}
 0998400^2 + 80000^2 &= 1001600^2 \\
 12\ 0998400^2 + 880000^2 &= 121\ 001600^2 \\
 1232\ 0998400^2 + 8880000^2 &= 12321\ 001600^2 \\
 123432\ 0998400^2 + 88880000^2 &= 1234321\ 001600^2 \quad (5.40)
 \end{aligned}$$

$$\begin{aligned}
 0998319^2 + 82000^2 &= 1001681^2 \\
 12\ 0998319^2 + 902000^2 &= 121\ 001681^2 \\
 1232\ 0998319^2 + 9102000^2 &= 12321\ 001681^2 \\
 123432\ 0998319^2 + 91102000^2 &= 1234321\ 001681^2 \quad (5.41)
 \end{aligned}$$

$$\begin{aligned}
 0998236^2 + 84000^2 &= 1001764^2 \\
 12\ 0998236^2 + 924000^2 &= 121\ 001764^2 \\
 1232\ 0998236^2 + 9324000^2 &= 12321\ 001764^2 \\
 123432\ 0998236^2 + 93324000^2 &= 1234321\ 001764^2 \quad (5.42)
 \end{aligned}$$

$$\begin{aligned}
 0998151^2 + 86000^2 &= 1001849^2 \\
 12\ 0998151^2 + 946000^2 &= 121\ 001849^2 \\
 1232\ 0998151^2 + 9546000^2 &= 12321\ 001849^2 \\
 123432\ 0998151^2 + 95546000^2 &= 1234321\ 001849^2 \quad (5.43)
 \end{aligned}$$

$$\begin{aligned}
 0998064^2 + 88000^2 &= 1001936^2 \\
 12\ 0998064^2 + 968000^2 &= 121\ 001936^2 \\
 1232\ 0998064^2 + 9768000^2 &= 12321\ 001936^2 \\
 123432\ 0998064^2 + 97768000^2 &= 1234321\ 001936^2 \quad (5.44)
 \end{aligned}$$

$$\begin{aligned}
 0997975^2 + 90000^2 &= 1002025^2 \\
 12\ 0997975^2 + 990000^2 &= 121\ 002025^2 \\
 1232\ 0997975^2 + 9990000^2 &= 12321\ 002025^2 \\
 123432\ 0997975^2 + 99990000^2 &= 1234321\ 002025^2 \quad (5.45)
 \end{aligned}$$

$$\begin{aligned} 0997884^2 + 92000^2 &= \textcolor{red}{1} 002116^2 \\ 12\ 0997884^2 + 1012000^2 &= \textcolor{blue}{121} 002116^2 \\ 1232\ 0997884^2 + 10212000^2 &= \textcolor{red}{12321} 002116^2 \\ 123432\ 0997884^2 + 102212000^2 &= \textcolor{blue}{1234321} 002116^2 \quad (5.46) \end{aligned}$$

$$\begin{aligned} 0997791^2 + 94000^2 &= \textcolor{red}{1} 002209^2 \\ 12\ 0997791^2 + 1034000^2 &= \textcolor{blue}{121} 002209^2 \\ 1232\ 0997791^2 + 10434000^2 &= \textcolor{red}{12321} 002209^2 \\ 123432\ 0997791^2 + 104434000^2 &= \textcolor{blue}{1234321} 002209^2 \quad (5.47) \end{aligned}$$

$$\begin{aligned} 0997696^2 + 96000^2 &= \textcolor{red}{1} 002304^2 \\ 12\ 0997696^2 + 1056000^2 &= \textcolor{blue}{121} 002304^2 \\ 1232\ 0997696^2 + 10656000^2 &= \textcolor{red}{12321} 002304^2 \\ 123432\ 0997696^2 + 106656000^2 &= \textcolor{blue}{1234321} 002304^2 \quad (5.48) \end{aligned}$$

$$\begin{aligned} 0997599^2 + 98000^2 &= \textcolor{red}{1} 002401^2 \\ 12\ 0997599^2 + 1078000^2 &= \textcolor{blue}{121} 002401^2 \\ 1232\ 0997599^2 + 10878000^2 &= \textcolor{red}{12321} 002401^2 \\ 123432\ 0997599^2 + 108878000^2 &= \textcolor{blue}{1234321} 002401^2 \quad (5.49) \end{aligned}$$

$$\begin{aligned} 0997500^2 + 100000^2 &= \textcolor{red}{1} 002500^2 \\ 12\ 0997500^2 + 1100000^2 &= \textcolor{blue}{121} 002500^2 \\ 1232\ 0997500^2 + 11100000^2 &= \textcolor{red}{12321} 002500^2 \\ 123432\ 0997500^2 + 111100000^2 &= \textcolor{blue}{1234321} 002500^2 \quad (5.50) \end{aligned}$$

$$\begin{aligned} 0997399^2 + 102000^2 &= \textcolor{red}{1} 002601^2 \\ 12\ 0997399^2 + 1122000^2 &= \textcolor{blue}{121} 002601^2 \\ 1232\ 0997399^2 + 11322000^2 &= \textcolor{red}{12321} 002601^2 \\ 123432\ 0997399^2 + 113322000^2 &= \textcolor{blue}{1234321} 002601^2 \quad (5.51) \end{aligned}$$

$$\begin{aligned} 0997296^2 + 104000^2 &= \textcolor{red}{1} 002704^2 \\ 12\ 0997296^2 + 1144000^2 &= \textcolor{blue}{121} 002704^2 \\ 1232\ 0997296^2 + 11544000^2 &= \textcolor{red}{12321} 002704^2 \\ 123432\ 0997296^2 + 115544000^2 &= \textcolor{blue}{1234321} 002704^2 \quad (5.52) \end{aligned}$$

$$\begin{aligned} 0997191^2 + 106000^2 &= \textcolor{red}{1} 002809^2 \\ 12\ 0997191^2 + 1166000^2 &= \textcolor{blue}{121} 002809^2 \\ 1232\ 0997191^2 + 11766000^2 &= \textcolor{red}{12321} 002809^2 \\ 123432\ 0997191^2 + 117766000^2 &= \textcolor{blue}{1234321} 002809^2 \quad (5.53) \end{aligned}$$

$$\begin{aligned} 0997084^2 + 108000^2 &= \textcolor{red}{1} 002916^2 \\ 12\ 0997084^2 + 1188000^2 &= \textcolor{blue}{121} 002916^2 \\ 1232\ 0997084^2 + 11988000^2 &= \textcolor{red}{12321} 002916^2 \\ 123432\ 0997084^2 + 119988000^2 &= \textcolor{blue}{1234321} 002916^2 \quad (5.54) \end{aligned}$$

$$\begin{aligned} 0996975^2 + 110000^2 &= \textcolor{red}{1} 003025^2 \\ 12\ 0996975^2 + 1210000^2 &= \textcolor{blue}{121} 003025^2 \\ 1232\ 0996975^2 + 12210000^2 &= \textcolor{red}{12321} 003025^2 \\ 123432\ 0996975^2 + 122210000^2 &= \textcolor{blue}{1234321} 003025^2 \quad (5.55) \end{aligned}$$

$$\begin{aligned} 0996864^2 + 112000^2 &= \textcolor{red}{1} 003136^2 \\ 12\ 0996864^2 + 1232000^2 &= \textcolor{blue}{121} 003136^2 \\ 1232\ 0996864^2 + 12432000^2 &= \textcolor{red}{12321} 003136^2 \\ 123432\ 0996864^2 + 124432000^2 &= \textcolor{blue}{1234321} 003136^2 \quad (5.56) \end{aligned}$$

$$\begin{aligned} 0996751^2 + 114000^2 &= \textcolor{red}{1} 003249^2 \\ 12\ 0996751^2 + 1254000^2 &= \textcolor{blue}{121} 003249^2 \\ 1232\ 0996751^2 + 12654000^2 &= \textcolor{red}{12321} 003249^2 \\ 123432\ 0996751^2 + 126654000^2 &= \textcolor{blue}{1234321} 003249^2 \quad (5.57) \end{aligned}$$

$$\begin{aligned} 0996636^2 + 116000^2 &= \textcolor{red}{1} 003364^2 \\ 12\ 0996636^2 + 1276000^2 &= \textcolor{blue}{121} 003364^2 \\ 1232\ 0996636^2 + 12876000^2 &= \textcolor{red}{12321} 003364^2 \\ 123432\ 0996636^2 + 128876000^2 &= \textcolor{blue}{1234321} 003364^2 \quad (5.58) \end{aligned}$$

$$\begin{aligned} 0996519^2 + 118000^2 &= \textcolor{red}{1} 003481^2 \\ 12\ 0996519^2 + 1298000^2 &= \textcolor{blue}{121} 003481^2 \\ 1232\ 0996519^2 + 13098000^2 &= \textcolor{red}{12321} 003481^2 \\ 123432\ 0996519^2 + 131098000^2 &= \textcolor{blue}{1234321} 003481^2 \quad (5.59) \end{aligned}$$

$$\begin{aligned} 0996400^2 + 120000^2 &= \textcolor{red}{1} 003600^2 \\ 12\ 0996400^2 + 1320000^2 &= \textcolor{blue}{121} 003600^2 \\ 1232\ 0996400^2 + 13320000^2 &= \textcolor{red}{12321} 003600^2 \\ 123432\ 0996400^2 + 133320000^2 &= \textcolor{blue}{1234321} 003600^2 \quad (5.60) \end{aligned}$$

$$\begin{aligned} 0996279^2 + 122000^2 &= \textcolor{red}{1} 003721^2 \\ 12\ 0996279^2 + 1342000^2 &= \textcolor{blue}{121} 003721^2 \\ 1232\ 0996279^2 + 13542000^2 &= \textcolor{red}{12321} 003721^2 \\ 123432\ 0996279^2 + 135542000^2 &= \textcolor{blue}{1234321} 003721^2 \quad (5.61) \end{aligned}$$

$$\begin{aligned} 0996156^2 + 124000^2 &= \textcolor{red}{1} 003844^2 \\ 12\ 0996156^2 + 1364000^2 &= \textcolor{blue}{121} 003844^2 \\ 1232\ 0996156^2 + 13764000^2 &= \textcolor{red}{12321} 003844^2 \\ 123432\ 0996156^2 + 137764000^2 &= \textcolor{blue}{1234321} 003844^2 \quad (5.62) \end{aligned}$$

$$\begin{aligned} 0996031^2 + 126000^2 &= \textcolor{red}{1} 003969^2 \\ 12 0996031^2 + 1386000^2 &= \textcolor{blue}{121} 003969^2 \\ 1232 0996031^2 + 13986000^2 &= \textcolor{blue}{12321} 003969^2 \\ 123432 0996031^2 + 139986000^2 &= \textcolor{blue}{1234321} 003969^2 \quad (5.63) \end{aligned}$$

$$\begin{aligned} 0995904^2 + 128000^2 &= \textcolor{red}{1} 004096^2 \\ 12 0995904^2 + 1408000^2 &= \textcolor{blue}{121} 004096^2 \\ 1232 0995904^2 + 14208000^2 &= \textcolor{blue}{12321} 004096^2 \\ 123432 0995904^2 + 142208000^2 &= \textcolor{blue}{1234321} 004096^2 \quad (5.64) \end{aligned}$$

$$\begin{aligned} 0995775^2 + 130000^2 &= \textcolor{red}{1} 004225^2 \\ 12 0995775^2 + 1430000^2 &= \textcolor{blue}{121} 004225^2 \\ 1232 0995775^2 + 14430000^2 &= \textcolor{blue}{12321} 004225^2 \\ 123432 0995775^2 + 144430000^2 &= \textcolor{blue}{1234321} 004225^2 \quad (5.65) \end{aligned}$$

$$\begin{aligned} 0995644^2 + 132000^2 &= \textcolor{red}{1} 004356^2 \\ 12 0995644^2 + 1452000^2 &= \textcolor{blue}{121} 004356^2 \\ 1232 0995644^2 + 14652000^2 &= \textcolor{blue}{12321} 004356^2 \\ 123432 0995644^2 + 146652000^2 &= \textcolor{blue}{1234321} 004356^2 \quad (5.66) \end{aligned}$$

$$\begin{aligned} 0995511^2 + 134000^2 &= \textcolor{red}{1} 004489^2 \\ 12 0995511^2 + 1474000^2 &= \textcolor{blue}{121} 004489^2 \\ 1232 0995511^2 + 14874000^2 &= \textcolor{blue}{12321} 004489^2 \\ 123432 0995511^2 + 148874000^2 &= \textcolor{blue}{1234321} 004489^2 \quad (5.67) \end{aligned}$$

$$\begin{aligned} 0995376^2 + 136000^2 &= \textcolor{red}{1} 004624^2 \\ 12 0995376^2 + 1496000^2 &= \textcolor{blue}{121} 004624^2 \\ 1232 0995376^2 + 15096000^2 &= \textcolor{blue}{12321} 004624^2 \\ 123432 0995376^2 + 151096000^2 &= \textcolor{blue}{1234321} 004624^2 \quad (5.68) \end{aligned}$$

$$\begin{aligned} 0995239^2 + 138000^2 &= \textcolor{red}{1} 004761^2 \\ 12 0995239^2 + 1518000^2 &= \textcolor{blue}{121} 004761^2 \\ 1232 0995239^2 + 15318000^2 &= \textcolor{blue}{12321} 004761^2 \\ 123432 0995239^2 + 153318000^2 &= \textcolor{blue}{1234321} 004761^2 \quad (5.69) \end{aligned}$$

$$\begin{aligned} 0995100^2 + 140000^2 &= \textcolor{red}{1} 004900^2 \\ 12 0995100^2 + 1540000^2 &= \textcolor{blue}{121} 004900^2 \\ 1232 0995100^2 + 15540000^2 &= \textcolor{blue}{12321} 004900^2 \\ 123432 0995100^2 + 155540000^2 &= \textcolor{blue}{1234321} 004900^2 \quad (5.70) \end{aligned}$$

$$\begin{aligned} 0994959^2 + 142000^2 &= \textcolor{red}{1} 005041^2 \\ 12 0994959^2 + 1562000^2 &= \textcolor{blue}{121} 005041^2 \\ 1232 0994959^2 + 15762000^2 &= \textcolor{blue}{12321} 005041^2 \\ 123432 0994959^2 + 157762000^2 &= \textcolor{blue}{1234321} 005041^2 \quad (5.71) \end{aligned}$$

$$\begin{aligned} 0994816^2 + 144000^2 &= \textcolor{red}{1} 005184^2 \\ 12 0994816^2 + 1584000^2 &= \textcolor{blue}{121} 005184^2 \\ 1232 0994816^2 + 15984000^2 &= \textcolor{blue}{12321} 005184^2 \\ 123432 0994816^2 + 159984000^2 &= \textcolor{blue}{1234321} 005184^2 \quad (5.72) \end{aligned}$$

$$\begin{aligned} 0994671^2 + 146000^2 &= \textcolor{red}{1} 005329^2 \\ 12 0994671^2 + 1606000^2 &= \textcolor{blue}{121} 005329^2 \\ 1232 0994671^2 + 16206000^2 &= \textcolor{blue}{12321} 005329^2 \\ 123432 0994671^2 + 162206000^2 &= \textcolor{blue}{1234321} 005329^2 \quad (5.73) \end{aligned}$$

$$\begin{aligned} 0994524^2 + 148000^2 &= \textcolor{red}{1} 005476^2 \\ 12 0994524^2 + 1628000^2 &= \textcolor{blue}{121} 005476^2 \\ 1232 0994524^2 + 16428000^2 &= \textcolor{blue}{12321} 005476^2 \\ 123432 0994524^2 + 164428000^2 &= \textcolor{blue}{1234321} 005476^2 \quad (5.74) \end{aligned}$$

$$\begin{aligned} 0994375^2 + 150000^2 &= \textcolor{red}{1} 005625^2 \\ 12 0994375^2 + 1650000^2 &= \textcolor{blue}{121} 005625^2 \\ 1232 0994375^2 + 16650000^2 &= \textcolor{blue}{12321} 005625^2 \\ 123432 0994375^2 + 166650000^2 &= \textcolor{blue}{1234321} 005625^2 \quad (5.75) \end{aligned}$$

$$\begin{aligned} 0994224^2 + 152000^2 &= \textcolor{red}{1} 005776^2 \\ 12 0994224^2 + 1672000^2 &= \textcolor{blue}{121} 005776^2 \\ 1232 0994224^2 + 16872000^2 &= \textcolor{blue}{12321} 005776^2 \\ 123432 0994224^2 + 168872000^2 &= \textcolor{blue}{1234321} 005776^2 \quad (5.76) \end{aligned}$$

$$\begin{aligned} 0994071^2 + 154000^2 &= \textcolor{red}{1} 005929^2 \\ 12 0994071^2 + 1694000^2 &= \textcolor{blue}{121} 005929^2 \\ 1232 0994071^2 + 17094000^2 &= \textcolor{blue}{12321} 005929^2 \\ 123432 0994071^2 + 171094000^2 &= \textcolor{blue}{1234321} 005929^2 \quad (5.77) \end{aligned}$$

$$\begin{aligned} 0993916^2 + 156000^2 &= \textcolor{red}{1} 006084^2 \\ 12 0993916^2 + 1716000^2 &= \textcolor{blue}{121} 006084^2 \\ 1232 0993916^2 + 17316000^2 &= \textcolor{blue}{12321} 006084^2 \\ 123432 0993916^2 + 173316000^2 &= \textcolor{blue}{1234321} 006084^2 \quad (5.78) \end{aligned}$$

$$\begin{aligned} 0993759^2 + 158000^2 &= \textcolor{red}{1} 006241^2 \\ 12 0993759^2 + 1738000^2 &= \textcolor{blue}{121} 006241^2 \\ 1232 0993759^2 + 17538000^2 &= \textcolor{blue}{12321} 006241^2 \\ 123432 0993759^2 + 175538000^2 &= \textcolor{blue}{1234321} 006241^2 \quad (5.79) \end{aligned}$$

$$\begin{aligned} 0993600^2 + 160000^2 &= \mathbf{1006400}^2 \\ 12\ 0993600^2 + 1760000^2 &= \mathbf{121006400}^2 \\ 1232\ 0993600^2 + 17760000^2 &= \mathbf{12321006400}^2 \\ 123432\ 0993600^2 + 177760000^2 &= \mathbf{1234321006400}^2 \quad (5.80) \end{aligned}$$

$$\begin{aligned} 0993439^2 + 162000^2 &= \mathbf{1006561}^2 \\ 12\ 0993439^2 + 1782000^2 &= \mathbf{121006561}^2 \\ 1232\ 0993439^2 + 17982000^2 &= \mathbf{12321006561}^2 \\ 123432\ 0993439^2 + 179982000^2 &= \mathbf{1234321006561}^2 \quad (5.81) \end{aligned}$$

$$\begin{aligned} 0993276^2 + 164000^2 &= \mathbf{1006724}^2 \\ 12\ 0993276^2 + 1804000^2 &= \mathbf{121006724}^2 \\ 1232\ 0993276^2 + 18204000^2 &= \mathbf{12321006724}^2 \\ 123432\ 0993276^2 + 182204000^2 &= \mathbf{1234321006724}^2 \quad (5.82) \end{aligned}$$

$$\begin{aligned} 0993111^2 + 166000^2 &= \mathbf{1006889}^2 \\ 12\ 0993111^2 + 1826000^2 &= \mathbf{121006889}^2 \\ 1232\ 0993111^2 + 18426000^2 &= \mathbf{12321006889}^2 \\ 123432\ 0993111^2 + 184426000^2 &= \mathbf{1234321006889}^2 \quad (5.83) \end{aligned}$$

$$\begin{aligned} 0992944^2 + 168000^2 &= \mathbf{1007056}^2 \\ 12\ 0992944^2 + 1848000^2 &= \mathbf{121007056}^2 \\ 1232\ 0992944^2 + 18648000^2 &= \mathbf{12321007056}^2 \\ 123432\ 0992944^2 + 186648000^2 &= \mathbf{1234321007056}^2 \quad (5.84) \end{aligned}$$

$$\begin{aligned} 0992775^2 + 170000^2 &= \mathbf{1007225}^2 \\ 12\ 0992775^2 + 1870000^2 &= \mathbf{121007225}^2 \\ 1232\ 0992775^2 + 18870000^2 &= \mathbf{12321007225}^2 \\ 123432\ 0992775^2 + 188870000^2 &= \mathbf{1234321007225}^2 \quad (5.85) \end{aligned}$$

$$\begin{aligned} 0992604^2 + 172000^2 &= \mathbf{1007396}^2 \\ 12\ 0992604^2 + 1892000^2 &= \mathbf{121007396}^2 \\ 1232\ 0992604^2 + 19092000^2 &= \mathbf{12321007396}^2 \\ 123432\ 0992604^2 + 191092000^2 &= \mathbf{1234321007396}^2 \quad (5.86) \end{aligned}$$

$$\begin{aligned} 0992431^2 + 174000^2 &= \mathbf{1007569}^2 \\ 12\ 0992431^2 + 1914000^2 &= \mathbf{121007569}^2 \\ 1232\ 0992431^2 + 19314000^2 &= \mathbf{12321007569}^2 \\ 123432\ 0992431^2 + 193314000^2 &= \mathbf{1234321007569}^2 \quad (5.87) \end{aligned}$$

$$\begin{aligned} 0992256^2 + 176000^2 &= \mathbf{1007744}^2 \\ 12\ 0992256^2 + 1936000^2 &= \mathbf{121007744}^2 \\ 1232\ 0992256^2 + 19536000^2 &= \mathbf{12321007744}^2 \\ 123432\ 0992256^2 + 195536000^2 &= \mathbf{1234321007744}^2 \quad (5.88) \end{aligned}$$

$$\begin{aligned} 0992079^2 + 178000^2 &= \mathbf{1007921}^2 \\ 12\ 0992079^2 + 1958000^2 &= \mathbf{121007921}^2 \\ 1232\ 0992079^2 + 19758000^2 &= \mathbf{12321007921}^2 \\ 123432\ 0992079^2 + 197758000^2 &= \mathbf{1234321007921}^2 \quad (5.89) \end{aligned}$$

$$\begin{aligned} 0991900^2 + 180000^2 &= \mathbf{1008100}^2 \\ 12\ 0991900^2 + 1980000^2 &= \mathbf{121008100}^2 \\ 1232\ 0991900^2 + 19980000^2 &= \mathbf{12321008100}^2 \\ 123432\ 0991900^2 + 199980000^2 &= \mathbf{1234321008100}^2 \quad (5.90) \end{aligned}$$

$$\begin{aligned} 0991719^2 + 182000^2 &= \mathbf{1008281}^2 \\ 12\ 0991719^2 + 2002000^2 &= \mathbf{121008281}^2 \\ 1232\ 0991719^2 + 20202000^2 &= \mathbf{12321008281}^2 \\ 123432\ 0991719^2 + 202202000^2 &= \mathbf{1234321008281}^2 \quad (5.91) \end{aligned}$$

$$\begin{aligned} 0991536^2 + 184000^2 &= \mathbf{1008464}^2 \\ 12\ 0991536^2 + 2024000^2 &= \mathbf{121008464}^2 \\ 1232\ 0991536^2 + 20424000^2 &= \mathbf{12321008464}^2 \\ 123432\ 0991536^2 + 204424000^2 &= \mathbf{1234321008464}^2 \quad (5.92) \end{aligned}$$

$$\begin{aligned} 0991351^2 + 186000^2 &= \mathbf{1008649}^2 \\ 12\ 0991351^2 + 2046000^2 &= \mathbf{121008649}^2 \\ 1232\ 0991351^2 + 20646000^2 &= \mathbf{12321008649}^2 \\ 123432\ 0991351^2 + 206646000^2 &= \mathbf{1234321008649}^2 \quad (5.93) \end{aligned}$$

$$\begin{aligned} 0991164^2 + 188000^2 &= \mathbf{1008836}^2 \\ 12\ 0991164^2 + 2068000^2 &= \mathbf{121008836}^2 \\ 1232\ 0991164^2 + 20868000^2 &= \mathbf{12321008836}^2 \\ 123432\ 0991164^2 + 208868000^2 &= \mathbf{1234321008836}^2 \quad (5.94) \end{aligned}$$

$$\begin{aligned} 0990975^2 + 190000^2 &= \mathbf{1009025}^2 \\ 12\ 0990975^2 + 2090000^2 &= \mathbf{121009025}^2 \\ 1232\ 0990975^2 + 21090000^2 &= \mathbf{12321009025}^2 \\ 123432\ 0990975^2 + 211090000^2 &= \mathbf{1234321009025}^2 \quad (5.95) \end{aligned}$$

$$\begin{aligned} 0990784^2 + 192000^2 &= \mathbf{1009216}^2 \\ 12\ 0990784^2 + 2112000^2 &= \mathbf{121009216}^2 \\ 1232\ 0990784^2 + 21312000^2 &= \mathbf{12321009216}^2 \\ 123432\ 0990784^2 + 213312000^2 &= \mathbf{1234321009216}^2 \quad (5.96) \end{aligned}$$

$$\begin{aligned}
 0990591^2 + 194000^2 &= \mathbf{1} 009409^2 \\
 12\ 0990591^2 + 2134000^2 &= \mathbf{121} 009409^2 \\
 1232\ 0990591^2 + 21534000^2 &= \mathbf{12321} 009409^2 \\
 123432\ 0990591^2 + 215534000^2 &= \mathbf{1234321} 009409^2 \quad (5.97) \\
 \\
 0990396^2 + 196000^2 &= \mathbf{1} 009604^2 \\
 12\ 0990396^2 + 2156000^2 &= \mathbf{121} 009604^2 \\
 1232\ 0990396^2 + 21756000^2 &= \mathbf{12321} 009604^2 \\
 123432\ 0990396^2 + 217756000^2 &= \mathbf{1234321} 009604^2 \quad (5.98)
 \end{aligned}$$

5.2 For $n = 100, 101, 101, \dots, 197, 198, 199$:

Let's consider

$$m = 1000, 11000, 111000, 1111000, 11111000, 111111000, 1111111000, 11111111000$$

in (1.1), then for each value of $n = 100, 101, 101, \dots, 197, 198, 199$; there are 100 *palindromic-type pandigital Pythagorean patterns* given below. In each case, only first four values are written. The other 5 values can be written on similar lines as done in subsection 5.1.1.

$$\begin{aligned}
& 0990000^2 + 200000^2 = \mathbf{1}010000^2 \\
& \mathbf{12}0990000^2 + 2200000^2 = \mathbf{121}010000^2 \\
& \mathbf{1232}0990000^2 + 22200000^2 = \mathbf{12321}010000^2 \\
& \mathbf{123432}0990000^2 + 222200000^2 = \mathbf{1234321}010000^2 \quad (5.100) \\
& \\
& 0989799^2 + 202000^2 = \mathbf{1}010201^2 \\
& \mathbf{12}0989799^2 + 2222000^2 = \mathbf{121}010201^2 \\
& \mathbf{1232}0989799^2 + 22422000^2 = \mathbf{12321}010201^2 \\
& \mathbf{123432}0989799^2 + 224422000^2 = \mathbf{1234321}010201^2 \quad (5.101) \\
& \\
& 0989596^2 + 204000^2 = \mathbf{1}010404^2 \\
& \mathbf{12}0989596^2 + 2244000^2 = \mathbf{121}010404^2 \\
& \mathbf{1232}0989596^2 + 22644000^2 = \mathbf{12321}010404^2 \\
& \mathbf{123432}0989596^2 + 226644000^2 = \mathbf{1234321}010404^2 \quad (5.102) \\
& \\
& 0989391^2 + 206000^2 = \mathbf{1}010609^2 \\
& \mathbf{12}0989391^2 + 2266000^2 = \mathbf{121}010609^2 \\
& \mathbf{1232}0989391^2 + 22866000^2 = \mathbf{12321}010609^2 \\
& \mathbf{123432}0989391^2 + 228866000^2 = \mathbf{1234321}010609^2 \quad (5.103) \\
& \\
& 0989184^2 + 208000^2 = \mathbf{1}010816^2 \\
& \mathbf{12}0989184^2 + 2288000^2 = \mathbf{121}010816^2 \\
& \mathbf{1232}0989184^2 + 23088000^2 = \mathbf{12321}010816^2 \\
& \mathbf{123432}0989184^2 + 231088000^2 = \mathbf{1234321}010816^2 \quad (5.104) \\
& \\
& 0988975^2 + 210000^2 = \mathbf{1}011025^2 \\
& \mathbf{12}0988975^2 + 2310000^2 = \mathbf{121}011025^2 \\
& \mathbf{1232}0988975^2 + 23310000^2 = \mathbf{12321}011025^2 \\
& \mathbf{123432}0988975^2 + 233310000^2 = \mathbf{1234321}011025^2 \quad (5.105) \\
& \\
& 0988764^2 + 212000^2 = \mathbf{1}011236^2 \\
& \mathbf{12}0988764^2 + 2332000^2 = \mathbf{121}011236^2 \\
& \mathbf{1232}0988764^2 + 23532000^2 = \mathbf{12321}011236^2 \\
& \mathbf{123432}0988764^2 + 235532000^2 = \mathbf{1234321}011236^2 \quad (5.106) \\
& \\
& 0988551^2 + 214000^2 = \mathbf{1}011449^2 \\
& \mathbf{12}0988551^2 + 2354000^2 = \mathbf{121}011449^2 \\
& \mathbf{1232}0988551^2 + 23754000^2 = \mathbf{12321}011449^2 \\
& \mathbf{123432}0988551^2 + 237754000^2 = \mathbf{1234321}011449^2 \quad (5.107) \\
& \\
& 0988336^2 + 216000^2 = \mathbf{1}011664^2 \\
& \mathbf{12}0988336^2 + 2376000^2 = \mathbf{121}011664^2 \\
& \mathbf{1232}0988336^2 + 23976000^2 = \mathbf{12321}011664^2 \\
& \mathbf{123432}0988336^2 + 239976000^2 = \mathbf{1234321}011664^2 \quad (5.108) \\
& \\
& 0988119^2 + 218000^2 = \mathbf{1}011881^2 \\
& \mathbf{12}0988119^2 + 2398000^2 = \mathbf{121}011881^2 \\
& \mathbf{1232}0988119^2 + 24198000^2 = \mathbf{12321}011881^2 \\
& \mathbf{123432}0988119^2 + 242198000^2 = \mathbf{1234321}011881^2 \quad (5.109) \\
& \\
& 0987900^2 + 220000^2 = \mathbf{1}012100^2 \\
& \mathbf{12}0987900^2 + 2420000^2 = \mathbf{121}012100^2 \\
& \mathbf{1232}0987900^2 + 24420000^2 = \mathbf{12321}012100^2 \\
& \mathbf{123432}0987900^2 + 244420000^2 = \mathbf{1234321}012100^2 \quad (5.110) \\
& \\
& 0987679^2 + 222000^2 = \mathbf{1}012321^2 \\
& \mathbf{12}0987679^2 + 2442000^2 = \mathbf{121}012321^2 \\
& \mathbf{1232}0987679^2 + 24642000^2 = \mathbf{12321}012321^2 \\
& \mathbf{123432}0987679^2 + 246642000^2 = \mathbf{1234321}012321^2 \quad (5.111) \\
& \\
& 0987456^2 + 224000^2 = \mathbf{1}012544^2 \\
& \mathbf{12}0987456^2 + 2464000^2 = \mathbf{121}012544^2 \\
& \mathbf{1232}0987456^2 + 24864000^2 = \mathbf{12321}012544^2 \\
& \mathbf{123432}0987456^2 + 248864000^2 = \mathbf{1234321}012544^2 \quad (5.112) \\
& \\
& 0987231^2 + 226000^2 = \mathbf{1}012769^2 \\
& \mathbf{12}0987231^2 + 2486000^2 = \mathbf{121}012769^2 \\
& \mathbf{1232}0987231^2 + 25086000^2 = \mathbf{12321}012769^2 \\
& \mathbf{123432}0987231^2 + 251086000^2 = \mathbf{1234321}012769^2 \quad (5.113) \\
& \\
& 0987004^2 + 228000^2 = \mathbf{1}012996^2 \\
& \mathbf{12}0987004^2 + 2508000^2 = \mathbf{121}012996^2 \\
& \mathbf{1232}0987004^2 + 25308000^2 = \mathbf{12321}012996^2 \\
& \mathbf{123432}0987004^2 + 253308000^2 = \mathbf{1234321}012996^2 \quad (5.114) \\
& \\
& 0986775^2 + 230000^2 = \mathbf{1}013225^2 \\
& \mathbf{12}0986775^2 + 2530000^2 = \mathbf{121}013225^2 \\
& \mathbf{1232}0986775^2 + 25530000^2 = \mathbf{12321}013225^2 \\
& \mathbf{123432}0986775^2 + 255530000^2 = \mathbf{1234321}013225^2 \quad (5.115) \\
& \\
& 0986544^2 + 232000^2 = \mathbf{1}013456^2 \\
& \mathbf{12}0986544^2 + 2552000^2 = \mathbf{121}013456^2 \\
& \mathbf{1232}0986544^2 + 25752000^2 = \mathbf{12321}013456^2 \\
& \mathbf{123432}0986544^2 + 257752000^2 = \mathbf{1234321}013456^2 \quad (5.116)
\end{aligned}$$

$$\begin{aligned} 0986311^2 + 234000^2 &= \textcolor{red}{1} 013689^2 \\ 12 0986311^2 + 2574000^2 &= \textcolor{red}{121} 013689^2 \\ 1232 0986311^2 + 25974000^2 &= \textcolor{red}{12321} 013689^2 \\ 123432 0986311^2 + 259974000^2 &= \textcolor{red}{1234321} 013689^2 \quad (5.117) \end{aligned}$$

$$\begin{aligned} 0986076^2 + 236000^2 &= \textcolor{red}{1} 013924^2 \\ 12 0986076^2 + 2596000^2 &= \textcolor{red}{121} 013924^2 \\ 1232 0986076^2 + 26196000^2 &= \textcolor{red}{12321} 013924^2 \\ 123432 0986076^2 + 262196000^2 &= \textcolor{red}{1234321} 013924^2 \quad (5.118) \end{aligned}$$

$$\begin{aligned} 0985839^2 + 238000^2 &= \textcolor{red}{1} 014161^2 \\ 12 0985839^2 + 2618000^2 &= \textcolor{red}{121} 014161^2 \\ 1232 0985839^2 + 26418000^2 &= \textcolor{red}{12321} 014161^2 \\ 123432 0985839^2 + 264418000^2 &= \textcolor{red}{1234321} 014161^2 \quad (5.119) \end{aligned}$$

$$\begin{aligned} 0985600^2 + 240000^2 &= \textcolor{red}{1} 014400^2 \\ 12 0985600^2 + 2640000^2 &= \textcolor{red}{121} 014400^2 \\ 1232 0985600^2 + 26640000^2 &= \textcolor{red}{12321} 014400^2 \\ 123432 0985600^2 + 266640000^2 &= \textcolor{red}{1234321} 014400^2 \quad (5.120) \end{aligned}$$

$$\begin{aligned} 0985359^2 + 242000^2 &= \textcolor{red}{1} 014641^2 \\ 12 0985359^2 + 2662000^2 &= \textcolor{red}{121} 014641^2 \\ 1232 0985359^2 + 26862000^2 &= \textcolor{red}{12321} 014641^2 \\ 123432 0985359^2 + 268862000^2 &= \textcolor{red}{1234321} 014641^2 \quad (5.121) \end{aligned}$$

$$\begin{aligned} 0985116^2 + 244000^2 &= \textcolor{red}{1} 014884^2 \\ 12 0985116^2 + 2684000^2 &= \textcolor{red}{121} 014884^2 \\ 1232 0985116^2 + 27084000^2 &= \textcolor{red}{12321} 014884^2 \\ 123432 0985116^2 + 271084000^2 &= \textcolor{red}{1234321} 014884^2 \quad (5.122) \end{aligned}$$

$$\begin{aligned} 0984871^2 + 246000^2 &= \textcolor{red}{1} 015129^2 \\ 12 0984871^2 + 2706000^2 &= \textcolor{red}{121} 015129^2 \\ 1232 0984871^2 + 27306000^2 &= \textcolor{red}{12321} 015129^2 \\ 123432 0984871^2 + 273306000^2 &= \textcolor{red}{1234321} 015129^2 \quad (5.123) \end{aligned}$$

$$\begin{aligned} 0984624^2 + 248000^2 &= \textcolor{red}{1} 015376^2 \\ 12 0984624^2 + 2728000^2 &= \textcolor{red}{121} 015376^2 \\ 1232 0984624^2 + 27528000^2 &= \textcolor{red}{12321} 015376^2 \\ 123432 0984624^2 + 275528000^2 &= \textcolor{red}{1234321} 015376^2 \quad (5.124) \end{aligned}$$

$$\begin{aligned} 0984375^2 + 250000^2 &= \textcolor{red}{1} 015625^2 \\ 12 0984375^2 + 2750000^2 &= \textcolor{red}{121} 015625^2 \\ 1232 0984375^2 + 27750000^2 &= \textcolor{red}{12321} 015625^2 \\ 123432 0984375^2 + 277750000^2 &= \textcolor{red}{1234321} 015625^2 \quad (5.125) \end{aligned}$$

$$\begin{aligned} 0984124^2 + 252000^2 &= \textcolor{red}{1} 015876^2 \\ 12 0984124^2 + 2772000^2 &= \textcolor{red}{121} 015876^2 \\ 1232 0984124^2 + 27972000^2 &= \textcolor{red}{12321} 015876^2 \\ 123432 0984124^2 + 279972000^2 &= \textcolor{red}{1234321} 015876^2 \quad (5.126) \end{aligned}$$

$$\begin{aligned} 0983871^2 + 254000^2 &= \textcolor{red}{1} 016129^2 \\ 12 0983871^2 + 2794000^2 &= \textcolor{red}{121} 016129^2 \\ 1232 0983871^2 + 28194000^2 &= \textcolor{red}{12321} 016129^2 \\ 123432 0983871^2 + 282194000^2 &= \textcolor{red}{1234321} 016129^2 \quad (5.127) \end{aligned}$$

$$\begin{aligned} 0983616^2 + 256000^2 &= \textcolor{red}{1} 016384^2 \\ 12 0983616^2 + 2816000^2 &= \textcolor{red}{121} 016384^2 \\ 1232 0983616^2 + 28416000^2 &= \textcolor{red}{12321} 016384^2 \\ 123432 0983616^2 + 284416000^2 &= \textcolor{red}{1234321} 016384^2 \quad (5.128) \end{aligned}$$

$$\begin{aligned} 0983359^2 + 258000^2 &= \textcolor{red}{1} 016641^2 \\ 12 0983359^2 + 2838000^2 &= \textcolor{red}{121} 016641^2 \\ 1232 0983359^2 + 28638000^2 &= \textcolor{red}{12321} 016641^2 \\ 123432 0983359^2 + 286638000^2 &= \textcolor{red}{1234321} 016641^2 \quad (5.129) \end{aligned}$$

$$\begin{aligned} 0983100^2 + 260000^2 &= \textcolor{red}{1} 016900^2 \\ 12 0983100^2 + 2860000^2 &= \textcolor{red}{121} 016900^2 \\ 1232 0983100^2 + 28860000^2 &= \textcolor{red}{12321} 016900^2 \\ 123432 0983100^2 + 288860000^2 &= \textcolor{red}{1234321} 016900^2 \quad (5.130) \end{aligned}$$

$$\begin{aligned} 0982839^2 + 262000^2 &= \textcolor{red}{1} 017161^2 \\ 12 0982839^2 + 2882000^2 &= \textcolor{red}{121} 017161^2 \\ 1232 0982839^2 + 29082000^2 &= \textcolor{red}{12321} 017161^2 \\ 123432 0982839^2 + 291082000^2 &= \textcolor{red}{1234321} 017161^2 \quad (5.131) \end{aligned}$$

$$\begin{aligned} 0982576^2 + 264000^2 &= \textcolor{red}{1} 017424^2 \\ 12 0982576^2 + 2904000^2 &= \textcolor{red}{121} 017424^2 \\ 1232 0982576^2 + 29304000^2 &= \textcolor{red}{12321} 017424^2 \\ 123432 0982576^2 + 293304000^2 &= \textcolor{red}{1234321} 017424^2 \quad (5.132) \end{aligned}$$

$$\begin{aligned} 0982311^2 + 266000^2 &= \textcolor{red}{1} 017689^2 \\ 12 0982311^2 + 2926000^2 &= \textcolor{red}{121} 017689^2 \\ 1232 0982311^2 + 29526000^2 &= \textcolor{red}{12321} 017689^2 \\ 123432 0982311^2 + 295526000^2 &= \textcolor{red}{1234321} 017689^2 \quad (5.133) \end{aligned}$$

$$\begin{aligned} 0982044^2 + 268000^2 &= \textcolor{red}{1} 017956^2 \\ 12 0982044^2 + 2948000^2 &= \textcolor{red}{121} 017956^2 \\ 1232 0982044^2 + 29748000^2 &= \textcolor{red}{12321} 017956^2 \\ 123432 0982044^2 + 297748000^2 &= \textcolor{red}{1234321} 017956^2 \quad (5.134) \end{aligned}$$

$$\begin{aligned} 0981775^2 + 270000^2 &= \textcolor{red}{1} 018225^2 \\ 12 0981775^2 + 2970000^2 &= \textcolor{red}{121} 018225^2 \\ 1232 0981775^2 + 29970000^2 &= \textcolor{red}{12321} 018225^2 \\ 123432 0981775^2 + 299970000^2 &= \textcolor{red}{1234321} 018225^2 \quad (5.135) \end{aligned}$$

$$\begin{aligned} 0981504^2 + 272000^2 &= \textcolor{red}{1} 018496^2 \\ 12 0981504^2 + 2992000^2 &= \textcolor{red}{121} 018496^2 \\ 1232 0981504^2 + 30192000^2 &= \textcolor{red}{12321} 018496^2 \\ 123432 0981504^2 + 302192000^2 &= \textcolor{red}{1234321} 018496^2 \quad (5.136) \end{aligned}$$

$$\begin{aligned} 0981231^2 + 274000^2 &= \textcolor{red}{1} 018769^2 \\ 12 0981231^2 + 3014000^2 &= \textcolor{red}{121} 018769^2 \\ 1232 0981231^2 + 30414000^2 &= \textcolor{red}{12321} 018769^2 \\ 123432 0981231^2 + 304414000^2 &= \textcolor{red}{1234321} 018769^2 \quad (5.137) \end{aligned}$$

$$\begin{aligned} 0980956^2 + 276000^2 &= \textcolor{red}{1} 019044^2 \\ 12 0980956^2 + 3036000^2 &= \textcolor{red}{121} 019044^2 \\ 1232 0980956^2 + 30636000^2 &= \textcolor{red}{12321} 019044^2 \\ 123432 0980956^2 + 306636000^2 &= \textcolor{red}{1234321} 019044^2 \quad (5.138) \end{aligned}$$

$$\begin{aligned} 0980679^2 + 278000^2 &= \textcolor{red}{1} 019321^2 \\ 12 0980679^2 + 3058000^2 &= \textcolor{red}{121} 019321^2 \\ 1232 0980679^2 + 30858000^2 &= \textcolor{red}{12321} 019321^2 \\ 123432 0980679^2 + 308858000^2 &= \textcolor{red}{1234321} 019321^2 \quad (5.139) \end{aligned}$$

$$\begin{aligned} 0980400^2 + 280000^2 &= \textcolor{red}{1} 019600^2 \\ 12 0980400^2 + 3080000^2 &= \textcolor{red}{121} 019600^2 \\ 1232 0980400^2 + 31080000^2 &= \textcolor{red}{12321} 019600^2 \\ 123432 0980400^2 + 311080000^2 &= \textcolor{red}{1234321} 019600^2 \quad (5.140) \end{aligned}$$

$$\begin{aligned} 0980119^2 + 282000^2 &= \textcolor{red}{1} 019881^2 \\ 12 0980119^2 + 3102000^2 &= \textcolor{red}{121} 019881^2 \\ 1232 0980119^2 + 31302000^2 &= \textcolor{red}{12321} 019881^2 \\ 123432 0980119^2 + 313302000^2 &= \textcolor{red}{1234321} 019881^2 \quad (5.141) \end{aligned}$$

$$\begin{aligned} 0979836^2 + 284000^2 &= \textcolor{red}{1} 020164^2 \\ 12 0979836^2 + 3124000^2 &= \textcolor{red}{121} 020164^2 \\ 1232 0979836^2 + 31524000^2 &= \textcolor{red}{12321} 020164^2 \\ 123432 0979836^2 + 315524000^2 &= \textcolor{red}{1234321} 020164^2 \quad (5.142) \end{aligned}$$

$$\begin{aligned} 0979551^2 + 286000^2 &= \textcolor{red}{1} 020449^2 \\ 12 0979551^2 + 3146000^2 &= \textcolor{red}{121} 020449^2 \\ 1232 0979551^2 + 31746000^2 &= \textcolor{red}{12321} 020449^2 \\ 123432 0979551^2 + 317746000^2 &= \textcolor{red}{1234321} 020449^2 \quad (5.143) \end{aligned}$$

$$\begin{aligned} 0979264^2 + 288000^2 &= \textcolor{red}{1} 020736^2 \\ 12 0979264^2 + 3168000^2 &= \textcolor{red}{121} 020736^2 \\ 1232 0979264^2 + 31968000^2 &= \textcolor{red}{12321} 020736^2 \\ 123432 0979264^2 + 319968000^2 &= \textcolor{red}{1234321} 020736^2 \quad (5.144) \end{aligned}$$

$$\begin{aligned} 0978975^2 + 290000^2 &= \textcolor{red}{1} 021025^2 \\ 12 0978975^2 + 3190000^2 &= \textcolor{red}{121} 021025^2 \\ 1232 0978975^2 + 32190000^2 &= \textcolor{red}{12321} 021025^2 \\ 123432 0978975^2 + 322190000^2 &= \textcolor{red}{1234321} 021025^2 \quad (5.145) \end{aligned}$$

$$\begin{aligned} 0978684^2 + 292000^2 &= \textcolor{red}{1} 021316^2 \\ 12 0978684^2 + 3212000^2 &= \textcolor{red}{121} 021316^2 \\ 1232 0978684^2 + 32412000^2 &= \textcolor{red}{12321} 021316^2 \\ 123432 0978684^2 + 324412000^2 &= \textcolor{red}{1234321} 021316^2 \quad (5.146) \end{aligned}$$

$$\begin{aligned} 0978391^2 + 294000^2 &= \textcolor{red}{1} 021609^2 \\ 12 0978391^2 + 3234000^2 &= \textcolor{red}{121} 021609^2 \\ 1232 0978391^2 + 32634000^2 &= \textcolor{red}{12321} 021609^2 \\ 123432 0978391^2 + 326634000^2 &= \textcolor{red}{1234321} 021609^2 \quad (5.147) \end{aligned}$$

$$\begin{aligned} 0978096^2 + 296000^2 &= \textcolor{red}{1} 021904^2 \\ 12 0978096^2 + 3256000^2 &= \textcolor{red}{121} 021904^2 \\ 1232 0978096^2 + 32856000^2 &= \textcolor{red}{12321} 021904^2 \\ 123432 0978096^2 + 328856000^2 &= \textcolor{red}{1234321} 021904^2 \quad (5.148) \end{aligned}$$

$$\begin{aligned} 0977799^2 + 298000^2 &= \textcolor{red}{1} 022201^2 \\ 12 0977799^2 + 3278000^2 &= \textcolor{red}{121} 022201^2 \\ 1232 0977799^2 + 33078000^2 &= \textcolor{red}{12321} 022201^2 \\ 123432 0977799^2 + 331078000^2 &= \textcolor{red}{1234321} 022201^2 \quad (5.149) \end{aligned}$$

$$\begin{aligned} 0977500^2 + 300000^2 &= \textcolor{red}{1} 022500^2 \\ 12 0977500^2 + 3300000^2 &= \textcolor{red}{121} 022500^2 \\ 1232 0977500^2 + 33300000^2 &= \textcolor{red}{12321} 022500^2 \\ 123432 0977500^2 + 333300000^2 &= \textcolor{red}{1234321} 022500^2 \quad (5.150) \end{aligned}$$

$$\begin{aligned}
& 0977199^2 + 302000^2 = \mathbf{1} 022801^2 \\
& \mathbf{12} 0977199^2 + 3322000^2 = \mathbf{121} 022801^2 \\
& \mathbf{1232} 0977199^2 + 33522000^2 = \mathbf{12321} 022801^2 \\
& \mathbf{123432} 0977199^2 + 335522000^2 = \mathbf{1234321} 022801^2 \quad (5.151) \\
& \\
& 0976896^2 + 304000^2 = \mathbf{1} 023104^2 \\
& \mathbf{12} 0976896^2 + 3344000^2 = \mathbf{121} 023104^2 \\
& \mathbf{1232} 0976896^2 + 33744000^2 = \mathbf{12321} 023104^2 \\
& \mathbf{123432} 0976896^2 + 337744000^2 = \mathbf{1234321} 023104^2 \quad (5.152) \\
& \\
& 0976591^2 + 306000^2 = \mathbf{1} 023409^2 \\
& \mathbf{12} 0976591^2 + 3366000^2 = \mathbf{121} 023409^2 \\
& \mathbf{1232} 0976591^2 + 33966000^2 = \mathbf{12321} 023409^2 \\
& \mathbf{123432} 0976591^2 + 339966000^2 = \mathbf{1234321} 023409^2 \quad (5.153) \\
& \\
& 0976284^2 + 308000^2 = \mathbf{1} 023716^2 \\
& \mathbf{12} 0976284^2 + 3388000^2 = \mathbf{121} 023716^2 \\
& \mathbf{1232} 0976284^2 + 34188000^2 = \mathbf{12321} 023716^2 \\
& \mathbf{123432} 0976284^2 + 342188000^2 = \mathbf{1234321} 023716^2 \quad (5.154) \\
& \\
& 0975975^2 + 310000^2 = \mathbf{1} 024025^2 \\
& \mathbf{12} 0975975^2 + 3410000^2 = \mathbf{121} 024025^2 \\
& \mathbf{1232} 0975975^2 + 34410000^2 = \mathbf{12321} 024025^2 \\
& \mathbf{123432} 0975975^2 + 344410000^2 = \mathbf{1234321} 024025^2 \quad (5.155) \\
& \\
& 0975664^2 + 312000^2 = \mathbf{1} 024336^2 \\
& \mathbf{12} 0975664^2 + 3432000^2 = \mathbf{121} 024336^2 \\
& \mathbf{1232} 0975664^2 + 34632000^2 = \mathbf{12321} 024336^2 \\
& \mathbf{123432} 0975664^2 + 346632000^2 = \mathbf{1234321} 024336^2 \quad (5.156) \\
& \\
& 0975351^2 + 314000^2 = \mathbf{1} 024649^2 \\
& \mathbf{12} 0975351^2 + 3454000^2 = \mathbf{121} 024649^2 \\
& \mathbf{1232} 0975351^2 + 34854000^2 = \mathbf{12321} 024649^2 \\
& \mathbf{123432} 0975351^2 + 348854000^2 = \mathbf{1234321} 024649^2 \quad (5.157) \\
& \\
& 0975036^2 + 316000^2 = \mathbf{1} 024964^2 \\
& \mathbf{12} 0975036^2 + 3476000^2 = \mathbf{121} 024964^2 \\
& \mathbf{1232} 0975036^2 + 35076000^2 = \mathbf{12321} 024964^2 \\
& \mathbf{123432} 0975036^2 + 351076000^2 = \mathbf{1234321} 024964^2 \quad (5.158) \\
& \\
& 0974719^2 + 318000^2 = \mathbf{1} 025281^2 \\
& \mathbf{12} 0974719^2 + 3498000^2 = \mathbf{121} 025281^2 \\
& \mathbf{1232} 0974719^2 + 35298000^2 = \mathbf{12321} 025281^2 \\
& \mathbf{123432} 0974719^2 + 353298000^2 = \mathbf{1234321} 025281^2 \quad (5.159) \\
& \\
& 0974400^2 + 320000^2 = \mathbf{1} 025600^2 \\
& \mathbf{12} 0974400^2 + 3520000^2 = \mathbf{121} 025600^2 \\
& \mathbf{1232} 0974400^2 + 35520000^2 = \mathbf{12321} 025600^2 \\
& \mathbf{123432} 0974400^2 + 355520000^2 = \mathbf{1234321} 025600^2 \quad (5.160) \\
& \\
& 0974079^2 + 322000^2 = \mathbf{1} 025921^2 \\
& \mathbf{12} 0974079^2 + 3542000^2 = \mathbf{121} 025921^2 \\
& \mathbf{1232} 0974079^2 + 35742000^2 = \mathbf{12321} 025921^2 \\
& \mathbf{123432} 0974079^2 + 357742000^2 = \mathbf{1234321} 025921^2 \quad (5.161) \\
& \\
& 0973756^2 + 324000^2 = \mathbf{1} 026244^2 \\
& \mathbf{12} 0973756^2 + 3564000^2 = \mathbf{121} 026244^2 \\
& \mathbf{1232} 0973756^2 + 35964000^2 = \mathbf{12321} 026244^2 \\
& \mathbf{123432} 0973756^2 + 359964000^2 = \mathbf{1234321} 026244^2 \quad (5.162) \\
& \\
& 0973431^2 + 326000^2 = \mathbf{1} 026569^2 \\
& \mathbf{12} 0973431^2 + 3586000^2 = \mathbf{121} 026569^2 \\
& \mathbf{1232} 0973431^2 + 36186000^2 = \mathbf{12321} 026569^2 \\
& \mathbf{123432} 0973431^2 + 362186000^2 = \mathbf{1234321} 026569^2 \quad (5.163) \\
& \\
& 0973104^2 + 328000^2 = \mathbf{1} 026896^2 \\
& \mathbf{12} 0973104^2 + 3608000^2 = \mathbf{121} 026896^2 \\
& \mathbf{1232} 0973104^2 + 36408000^2 = \mathbf{12321} 026896^2 \\
& \mathbf{123432} 0973104^2 + 364408000^2 = \mathbf{1234321} 026896^2 \quad (5.164) \\
& \\
& 0972775^2 + 330000^2 = \mathbf{1} 027225^2 \\
& \mathbf{12} 0972775^2 + 3630000^2 = \mathbf{121} 027225^2 \\
& \mathbf{1232} 0972775^2 + 36630000^2 = \mathbf{12321} 027225^2 \\
& \mathbf{123432} 0972775^2 + 366630000^2 = \mathbf{1234321} 027225^2 \quad (5.165) \\
& \\
& 0972444^2 + 332000^2 = \mathbf{1} 027556^2 \\
& \mathbf{12} 0972444^2 + 3652000^2 = \mathbf{121} 027556^2 \\
& \mathbf{1232} 0972444^2 + 36852000^2 = \mathbf{12321} 027556^2 \\
& \mathbf{123432} 0972444^2 + 368852000^2 = \mathbf{1234321} 027556^2 \quad (5.166) \\
& \\
& 0972111^2 + 334000^2 = \mathbf{1} 027889^2 \\
& \mathbf{12} 0972111^2 + 3674000^2 = \mathbf{121} 027889^2 \\
& \mathbf{1232} 0972111^2 + 37074000^2 = \mathbf{12321} 027889^2 \\
& \mathbf{123432} 0972111^2 + 371074000^2 = \mathbf{1234321} 027889^2 \quad (5.167)
\end{aligned}$$

$$\begin{aligned}
& 0971776^2 + 336000^2 = \mathbf{1} 028224^2 \\
& \mathbf{12} 0971776^2 + 3696000^2 = \mathbf{121} 028224^2 \\
& \mathbf{1232} 0971776^2 + 37296000^2 = \mathbf{12321} 028224^2 \\
& \mathbf{123432} 0971776^2 + 373296000^2 = \mathbf{1234321} 028224^2 \quad (5.168) \\
& \\
& 0971439^2 + 338000^2 = \mathbf{1} 028561^2 \\
& \mathbf{12} 0971439^2 + 3718000^2 = \mathbf{121} 028561^2 \\
& \mathbf{1232} 0971439^2 + 37518000^2 = \mathbf{12321} 028561^2 \\
& \mathbf{123432} 0971439^2 + 375518000^2 = \mathbf{1234321} 028561^2 \quad (5.169) \\
& \\
& 0971100^2 + 340000^2 = \mathbf{1} 028900^2 \\
& \mathbf{12} 0971100^2 + 3740000^2 = \mathbf{121} 028900^2 \\
& \mathbf{1232} 0971100^2 + 37740000^2 = \mathbf{12321} 028900^2 \\
& \mathbf{123432} 0971100^2 + 377740000^2 = \mathbf{1234321} 028900^2 \quad (5.170) \\
& \\
& 0970759^2 + 342000^2 = \mathbf{1} 029241^2 \\
& \mathbf{12} 0970759^2 + 3762000^2 = \mathbf{121} 029241^2 \\
& \mathbf{1232} 0970759^2 + 37962000^2 = \mathbf{12321} 029241^2 \\
& \mathbf{123432} 0970759^2 + 379962000^2 = \mathbf{1234321} 029241^2 \quad (5.171) \\
& \\
& 0970416^2 + 344000^2 = \mathbf{1} 029584^2 \\
& \mathbf{12} 0970416^2 + 3784000^2 = \mathbf{121} 029584^2 \\
& \mathbf{1232} 0970416^2 + 38184000^2 = \mathbf{12321} 029584^2 \\
& \mathbf{123432} 0970416^2 + 382184000^2 = \mathbf{1234321} 029584^2 \quad (5.172) \\
& \\
& 0970071^2 + 346000^2 = \mathbf{1} 029929^2 \\
& \mathbf{12} 0970071^2 + 3806000^2 = \mathbf{121} 029929^2 \\
& \mathbf{1232} 0970071^2 + 38406000^2 = \mathbf{12321} 029929^2 \\
& \mathbf{123432} 0970071^2 + 384406000^2 = \mathbf{1234321} 029929^2 \quad (5.173) \\
& \\
& 0969724^2 + 348000^2 = \mathbf{1} 030276^2 \\
& \mathbf{12} 0969724^2 + 3828000^2 = \mathbf{121} 030276^2 \\
& \mathbf{1232} 0969724^2 + 38628000^2 = \mathbf{12321} 030276^2 \\
& \mathbf{123432} 0969724^2 + 386628000^2 = \mathbf{1234321} 030276^2 \quad (5.174) \\
& \\
& 0969375^2 + 350000^2 = \mathbf{1} 030625^2 \\
& \mathbf{12} 0969375^2 + 3850000^2 = \mathbf{121} 030625^2 \\
& \mathbf{1232} 0969375^2 + 38850000^2 = \mathbf{12321} 030625^2 \\
& \mathbf{123432} 0969375^2 + 388850000^2 = \mathbf{1234321} 030625^2 \quad (5.175) \\
& \\
& 0969024^2 + 352000^2 = \mathbf{1} 030976^2 \\
& \mathbf{12} 0969024^2 + 3872000^2 = \mathbf{121} 030976^2 \\
& \mathbf{1232} 0969024^2 + 39072000^2 = \mathbf{12321} 030976^2 \\
& \mathbf{123432} 0969024^2 + 391072000^2 = \mathbf{1234321} 030976^2 \quad (5.176) \\
& \\
& 0968671^2 + 354000^2 = \mathbf{1} 031329^2 \\
& \mathbf{12} 0968671^2 + 3894000^2 = \mathbf{121} 031329^2 \\
& \mathbf{1232} 0968671^2 + 39294000^2 = \mathbf{12321} 031329^2 \\
& \mathbf{123432} 0968671^2 + 393294000^2 = \mathbf{1234321} 031329^2 \quad (5.177) \\
& \\
& 0968316^2 + 356000^2 = \mathbf{1} 031684^2 \\
& \mathbf{12} 0968316^2 + 3916000^2 = \mathbf{121} 031684^2 \\
& \mathbf{1232} 0968316^2 + 39516000^2 = \mathbf{12321} 031684^2 \\
& \mathbf{123432} 0968316^2 + 395516000^2 = \mathbf{1234321} 031684^2 \quad (5.178) \\
& \\
& 0967959^2 + 358000^2 = \mathbf{1} 032041^2 \\
& \mathbf{12} 0967959^2 + 3938000^2 = \mathbf{121} 032041^2 \\
& \mathbf{1232} 0967959^2 + 39738000^2 = \mathbf{12321} 032041^2 \\
& \mathbf{123432} 0967959^2 + 397738000^2 = \mathbf{1234321} 032041^2 \quad (5.179) \\
& \\
& 0967600^2 + 360000^2 = \mathbf{1} 032400^2 \\
& \mathbf{12} 0967600^2 + 3960000^2 = \mathbf{121} 032400^2 \\
& \mathbf{1232} 0967600^2 + 39960000^2 = \mathbf{12321} 032400^2 \\
& \mathbf{123432} 0967600^2 + 399960000^2 = \mathbf{1234321} 032400^2 \quad (5.180) \\
& \\
& 0967239^2 + 362000^2 = \mathbf{1} 032761^2 \\
& \mathbf{12} 0967239^2 + 3982000^2 = \mathbf{121} 032761^2 \\
& \mathbf{1232} 0967239^2 + 40182000^2 = \mathbf{12321} 032761^2 \\
& \mathbf{123432} 0967239^2 + 402182000^2 = \mathbf{1234321} 032761^2 \quad (5.181) \\
& \\
& 0966876^2 + 364000^2 = \mathbf{1} 033124^2 \\
& \mathbf{12} 0966876^2 + 4004000^2 = \mathbf{121} 033124^2 \\
& \mathbf{1232} 0966876^2 + 40404000^2 = \mathbf{12321} 033124^2 \\
& \mathbf{123432} 0966876^2 + 404404000^2 = \mathbf{1234321} 033124^2 \quad (5.182) \\
& \\
& 0966511^2 + 366000^2 = \mathbf{1} 033489^2 \\
& \mathbf{12} 0966511^2 + 4026000^2 = \mathbf{121} 033489^2 \\
& \mathbf{1232} 0966511^2 + 40626000^2 = \mathbf{12321} 033489^2 \\
& \mathbf{123432} 0966511^2 + 406626000^2 = \mathbf{1234321} 033489^2 \quad (5.183) \\
& \\
& 0966144^2 + 368000^2 = \mathbf{1} 033856^2 \\
& \mathbf{12} 0966144^2 + 4048000^2 = \mathbf{121} 033856^2 \\
& \mathbf{1232} 0966144^2 + 40848000^2 = \mathbf{12321} 033856^2 \\
& \mathbf{123432} 0966144^2 + 408848000^2 = \mathbf{1234321} 033856^2 \quad (5.184)
\end{aligned}$$

$$\begin{aligned}
& 0965775^2 + 370000^2 = \mathbf{1} 034225^2 \\
& \mathbf{12} 0965775^2 + 4070000^2 = \mathbf{121} 034225^2 \\
& \mathbf{1232} 0965775^2 + 41070000^2 = \mathbf{12321} 034225^2 \\
& \mathbf{123432} 0965775^2 + 411070000^2 = \mathbf{1234321} 034225^2 \quad (5.185) \\
& \\
& 0965404^2 + 372000^2 = \mathbf{1} 034596^2 \\
& \mathbf{12} 0965404^2 + 4092000^2 = \mathbf{121} 034596^2 \\
& \mathbf{1232} 0965404^2 + 41292000^2 = \mathbf{12321} 034596^2 \\
& \mathbf{123432} 0965404^2 + 413292000^2 = \mathbf{1234321} 034596^2 \quad (5.186) \\
& \\
& 0965031^2 + 374000^2 = \mathbf{1} 034969^2 \\
& \mathbf{12} 0965031^2 + 4114000^2 = \mathbf{121} 034969^2 \\
& \mathbf{1232} 0965031^2 + 41514000^2 = \mathbf{12321} 034969^2 \\
& \mathbf{123432} 0965031^2 + 415514000^2 = \mathbf{1234321} 034969^2 \quad (5.187) \\
& \\
& 0964656^2 + 376000^2 = \mathbf{1} 035344^2 \\
& \mathbf{12} 0964656^2 + 4136000^2 = \mathbf{121} 035344^2 \\
& \mathbf{1232} 0964656^2 + 41736000^2 = \mathbf{12321} 035344^2 \\
& \mathbf{123432} 0964656^2 + 417736000^2 = \mathbf{1234321} 035344^2 \quad (5.188) \\
& \\
& 0964279^2 + 378000^2 = \mathbf{1} 035721^2 \\
& \mathbf{12} 0964279^2 + 4158000^2 = \mathbf{121} 035721^2 \\
& \mathbf{1232} 0964279^2 + 41958000^2 = \mathbf{12321} 035721^2 \\
& \mathbf{123432} 0964279^2 + 419958000^2 = \mathbf{1234321} 035721^2 \quad (5.189) \\
& \\
& 0963900^2 + 380000^2 = \mathbf{1} 036100^2 \\
& \mathbf{12} 0963900^2 + 4180000^2 = \mathbf{121} 036100^2 \\
& \mathbf{1232} 0963900^2 + 42180000^2 = \mathbf{12321} 036100^2 \\
& \mathbf{123432} 0963900^2 + 422180000^2 = \mathbf{1234321} 036100^2 \quad (5.190) \\
& \\
& 0963519^2 + 382000^2 = \mathbf{1} 036481^2 \\
& \mathbf{12} 0963519^2 + 4202000^2 = \mathbf{121} 036481^2 \\
& \mathbf{1232} 0963519^2 + 42402000^2 = \mathbf{12321} 036481^2 \\
& \mathbf{123432} 0963519^2 + 424402000^2 = \mathbf{1234321} 036481^2 \quad (5.191) \\
& \\
& 0963136^2 + 384000^2 = \mathbf{1} 036864^2 \\
& \mathbf{12} 0963136^2 + 4224000^2 = \mathbf{121} 036864^2 \\
& \mathbf{1232} 0963136^2 + 42624000^2 = \mathbf{12321} 036864^2 \\
& \mathbf{123432} 0963136^2 + 426624000^2 = \mathbf{1234321} 036864^2 \quad (5.192)
\end{aligned}$$

5.3 For $n = 200, 201, 201, \dots, 297, 298, 299$:

Let's consider

$$m = 1000, 11000, 111000, 1111000, 11111000, 111111000, 1111111000, 11111111000, 111111111000$$

in (1.1), then for each value of $n = 200, 201, 201, \dots, 297, 298, 299$; there are 100 *palindromic-type pandigital Pythagorean patterns* given below. In each case, only first four values are written. The other 5 values can be written on similar lines as done in subsection 5.1.1.

$0960000^2 + 400000^2 = 1040000^2$	$0956736^2 + 416000^2 = 1043264^2$
$120960000^2 + 4400000^2 = 121040000^2$	$120956736^2 + 4576000^2 = 121043264^2$
$12320960000^2 + 44400000^2 = 12321040000^2$	$12320956736^2 + 46176000^2 = 12321043264^2$
$1234320960000^2 + 444400000^2 = 1234321040000^2 \quad (5.200)$	$1234320956736^2 + 462176000^2 = 1234321043264^2 \quad (5.208)$
$0959599^2 + 402000^2 = 1040401^2$	$0956319^2 + 418000^2 = 1043681^2$
$120959599^2 + 4422000^2 = 121040401^2$	$120956319^2 + 4598000^2 = 121043681^2$
$12320959599^2 + 44622000^2 = 12321040401^2$	$12320956319^2 + 46398000^2 = 12321043681^2$
$1234320959599^2 + 446622000^2 = 1234321040401^2 \quad (5.201)$	$1234320956319^2 + 464398000^2 = 1234321043681^2 \quad (5.209)$
$0959196^2 + 404000^2 = 1040804^2$	$0955900^2 + 420000^2 = 1044100^2$
$120959196^2 + 4444000^2 = 121040804^2$	$120955900^2 + 4620000^2 = 121044100^2$
$12320959196^2 + 44844000^2 = 12321040804^2$	$12320955900^2 + 46620000^2 = 12321044100^2$
$1234320959196^2 + 448844000^2 = 1234321040804^2 \quad (5.202)$	$1234320955900^2 + 466620000^2 = 1234321044100^2 \quad (5.210)$
$0958791^2 + 406000^2 = 1041209^2$	$0955479^2 + 422000^2 = 1044521^2$
$120958791^2 + 4466000^2 = 121041209^2$	$120955479^2 + 4642000^2 = 121044521^2$
$12320958791^2 + 45066000^2 = 12321041209^2$	$12320955479^2 + 46842000^2 = 12321044521^2$
$1234320958791^2 + 451066000^2 = 1234321041209^2 \quad (5.203)$	$1234320955479^2 + 468842000^2 = 1234321044521^2 \quad (5.211)$
$0958384^2 + 408000^2 = 1041616^2$	$0955056^2 + 424000^2 = 1044944^2$
$120958384^2 + 4488000^2 = 121041616^2$	$120955056^2 + 4664000^2 = 121044944^2$
$12320958384^2 + 45288000^2 = 12321041616^2$	$12320955056^2 + 47064000^2 = 12321044944^2$
$1234320958384^2 + 453288000^2 = 1234321041616^2 \quad (5.204)$	$1234320955056^2 + 471064000^2 = 1234321044944^2 \quad (5.212)$
$0957975^2 + 410000^2 = 1042025^2$	$0954631^2 + 426000^2 = 1045369^2$
$120957975^2 + 4510000^2 = 121042025^2$	$120954631^2 + 4686000^2 = 121045369^2$
$12320957975^2 + 45510000^2 = 12321042025^2$	$12320954631^2 + 47286000^2 = 12321045369^2$
$1234320957975^2 + 455510000^2 = 1234321042025^2 \quad (5.205)$	$1234320954631^2 + 473286000^2 = 1234321045369^2 \quad (5.213)$
$0957564^2 + 412000^2 = 1042436^2$	$0954204^2 + 428000^2 = 1045796^2$
$120957564^2 + 4532000^2 = 121042436^2$	$120954204^2 + 4708000^2 = 121045796^2$
$12320957564^2 + 45732000^2 = 12321042436^2$	$12320954204^2 + 47508000^2 = 12321045796^2$
$1234320957564^2 + 457732000^2 = 1234321042436^2 \quad (5.206)$	$1234320954204^2 + 475508000^2 = 1234321045796^2 \quad (5.214)$
$0957151^2 + 414000^2 = 1042849^2$	$0953775^2 + 430000^2 = 1046225^2$
$120957151^2 + 4554000^2 = 121042849^2$	$120953775^2 + 4730000^2 = 121046225^2$
$12320957151^2 + 45954000^2 = 12321042849^2$	$12320953775^2 + 47730000^2 = 12321046225^2$
$1234320957151^2 + 459954000^2 = 1234321042849^2 \quad (5.207)$	$1234320953775^2 + 477730000^2 = 1234321046225^2 \quad (5.215)$

$$\begin{aligned}
& 0953344^2 + 432000^2 = \mathbf{1} 046656^2 \\
& \mathbf{12} 0953344^2 + 4752000^2 = \mathbf{121} 046656^2 \\
& \mathbf{1232} 0953344^2 + 47952000^2 = \mathbf{12321} 046656^2 \\
& \mathbf{123432} 0953344^2 + 479952000^2 = \mathbf{1234321} 046656^2 \quad (5.216) \\
& 0952911^2 + 434000^2 = \mathbf{1} 047089^2 \\
& \mathbf{12} 0952911^2 + 4774000^2 = \mathbf{121} 047089^2 \\
& \mathbf{1232} 0952911^2 + 48174000^2 = \mathbf{12321} 047089^2 \\
& \mathbf{123432} 0952911^2 + 482174000^2 = \mathbf{1234321} 047089^2 \quad (5.217) \\
& 0952476^2 + 436000^2 = \mathbf{1} 047524^2 \\
& \mathbf{12} 0952476^2 + 4796000^2 = \mathbf{121} 047524^2 \\
& \mathbf{1232} 0952476^2 + 48396000^2 = \mathbf{12321} 047524^2 \\
& \mathbf{123432} 0952476^2 + 484396000^2 = \mathbf{1234321} 047524^2 \quad (5.218) \\
& 0952039^2 + 438000^2 = \mathbf{1} 047961^2 \\
& \mathbf{12} 0952039^2 + 4818000^2 = \mathbf{121} 047961^2 \\
& \mathbf{1232} 0952039^2 + 48618000^2 = \mathbf{12321} 047961^2 \\
& \mathbf{123432} 0952039^2 + 486618000^2 = \mathbf{1234321} 047961^2 \quad (5.219) \\
& 0951600^2 + 440000^2 = \mathbf{1} 048400^2 \\
& \mathbf{12} 0951600^2 + 4840000^2 = \mathbf{121} 048400^2 \\
& \mathbf{1232} 0951600^2 + 48840000^2 = \mathbf{12321} 048400^2 \\
& \mathbf{123432} 0951600^2 + 488840000^2 = \mathbf{1234321} 048400^2 \quad (5.220) \\
& 0951159^2 + 442000^2 = \mathbf{1} 048841^2 \\
& \mathbf{12} 0951159^2 + 4862000^2 = \mathbf{121} 048841^2 \\
& \mathbf{1232} 0951159^2 + 49062000^2 = \mathbf{12321} 048841^2 \\
& \mathbf{123432} 0951159^2 + 491062000^2 = \mathbf{1234321} 048841^2 \quad (5.221) \\
& 0950716^2 + 444000^2 = \mathbf{1} 049284^2 \\
& \mathbf{12} 0950716^2 + 4884000^2 = \mathbf{121} 049284^2 \\
& \mathbf{1232} 0950716^2 + 49284000^2 = \mathbf{12321} 049284^2 \\
& \mathbf{123432} 0950716^2 + 493284000^2 = \mathbf{1234321} 049284^2 \quad (5.222) \\
& 0950271^2 + 446000^2 = \mathbf{1} 049729^2 \\
& \mathbf{12} 0950271^2 + 4906000^2 = \mathbf{121} 049729^2 \\
& \mathbf{1232} 0950271^2 + 49506000^2 = \mathbf{12321} 049729^2 \\
& \mathbf{123432} 0950271^2 + 495506000^2 = \mathbf{1234321} 049729^2 \quad (5.223) \\
& 0949824^2 + 448000^2 = \mathbf{1} 050176^2 \\
& \mathbf{12} 0949824^2 + 4928000^2 = \mathbf{121} 050176^2 \\
& \mathbf{1232} 0949824^2 + 49728000^2 = \mathbf{12321} 050176^2 \\
& \mathbf{123432} 0949824^2 + 497728000^2 = \mathbf{1234321} 050176^2 \quad (5.224) \\
& 0949375^2 + 450000^2 = \mathbf{1} 050625^2 \\
& \mathbf{12} 0949375^2 + 4950000^2 = \mathbf{121} 050625^2 \\
& \mathbf{1232} 0949375^2 + 49950000^2 = \mathbf{12321} 050625^2 \\
& \mathbf{123432} 0949375^2 + 499950000^2 = \mathbf{1234321} 050625^2 \quad (5.225) \\
& 0948924^2 + 452000^2 = \mathbf{1} 051076^2 \\
& \mathbf{12} 0948924^2 + 4972000^2 = \mathbf{121} 051076^2 \\
& \mathbf{1232} 0948924^2 + 50172000^2 = \mathbf{12321} 051076^2 \\
& \mathbf{123432} 0948924^2 + 502172000^2 = \mathbf{1234321} 051076^2 \quad (5.226) \\
& 0948471^2 + 454000^2 = \mathbf{1} 051529^2 \\
& \mathbf{12} 0948471^2 + 4994000^2 = \mathbf{121} 051529^2 \\
& \mathbf{1232} 0948471^2 + 50394000^2 = \mathbf{12321} 051529^2 \\
& \mathbf{123432} 0948471^2 + 504394000^2 = \mathbf{1234321} 051529^2 \quad (5.227) \\
& 0948016^2 + 456000^2 = \mathbf{1} 051984^2 \\
& \mathbf{12} 0948016^2 + 5016000^2 = \mathbf{121} 051984^2 \\
& \mathbf{1232} 0948016^2 + 50616000^2 = \mathbf{12321} 051984^2 \\
& \mathbf{123432} 0948016^2 + 506616000^2 = \mathbf{1234321} 051984^2 \quad (5.228) \\
& 0947559^2 + 458000^2 = \mathbf{1} 052441^2 \\
& \mathbf{12} 0947559^2 + 5038000^2 = \mathbf{121} 052441^2 \\
& \mathbf{1232} 0947559^2 + 50838000^2 = \mathbf{12321} 052441^2 \\
& \mathbf{123432} 0947559^2 + 508838000^2 = \mathbf{1234321} 052441^2 \quad (5.229) \\
& 0947100^2 + 460000^2 = \mathbf{1} 052900^2 \\
& \mathbf{12} 0947100^2 + 5060000^2 = \mathbf{121} 052900^2 \\
& \mathbf{1232} 0947100^2 + 51060000^2 = \mathbf{12321} 052900^2 \\
& \mathbf{123432} 0947100^2 + 511060000^2 = \mathbf{1234321} 052900^2 \quad (5.230) \\
& 0946639^2 + 462000^2 = \mathbf{1} 053361^2 \\
& \mathbf{12} 0946639^2 + 5082000^2 = \mathbf{121} 053361^2 \\
& \mathbf{1232} 0946639^2 + 51282000^2 = \mathbf{12321} 053361^2 \\
& \mathbf{123432} 0946639^2 + 513282000^2 = \mathbf{1234321} 053361^2 \quad (5.231) \\
& 0946176^2 + 464000^2 = \mathbf{1} 053824^2 \\
& \mathbf{12} 0946176^2 + 5104000^2 = \mathbf{121} 053824^2 \\
& \mathbf{1232} 0946176^2 + 51504000^2 = \mathbf{12321} 053824^2 \\
& \mathbf{123432} 0946176^2 + 515504000^2 = \mathbf{1234321} 053824^2 \quad (5.232)
\end{aligned}$$

$$\begin{aligned}
 0945711^2 + 466000^2 &= \mathbf{1}054289^2 \\
 12\,0945711^2 + 5126000^2 &= \mathbf{121}\,054289^2 \\
 \mathbf{1232}\,0945711^2 + 51726000^2 &= \mathbf{12321}\,054289^2 \\
 \mathbf{123432}\,0945711^2 + 517726000^2 &= \mathbf{1234321}\,054289^2 \quad (5.233)
 \end{aligned}$$

$$\begin{aligned}
 0941436^2 + 484000^2 &= 1058564^2 \\
 12\,0941436^2 + 5324000^2 &= 121\,058564^2 \\
 1232\,0941436^2 + 53724000^2 &= 12321\,058564^2 \\
 123432\,0941436^2 + 537724000^2 &= 1234321\,058564^2 \quad (5.242)
 \end{aligned}$$

$$\begin{aligned}
 0945244^2 + 468000^2 &= \mathbf{1054756}^2 \\
 12\,0945244^2 + 5148000^2 &= \mathbf{121\,054756}^2 \\
 \mathbf{1232\,0945244}^2 + 51948000^2 &= \mathbf{12321\,054756}^2 \\
 \mathbf{123432\,0945244}^2 + 519948000^2 &= \mathbf{1234321\,054756}^2 \quad (5.234)
 \end{aligned}$$

$$\begin{aligned}
 0940951^2 + 486000^2 &= 1059049^2 \\
 12\,0940951^2 + 5346000^2 &= 121\,059049^2 \\
 1232\,0940951^2 + 53946000^2 &= 12321\,059049^2 \\
 123432\,0940951^2 + 539946000^2 &= 1234321\,059049^2 \quad (5.243)
 \end{aligned}$$

$$\begin{aligned}
 0944775^2 + 470000^2 &= 1\,055225^2 \\
 12\,0944775^2 + 5170000^2 &= 121\,055225^2 \\
 1232\,0944775^2 + 52170000^2 &= 12321\,055225^2 \\
 123432\,0944775^2 + 522170000^2 &= 1234321\,055225^2 \quad (5.235)
 \end{aligned}$$

$$\begin{aligned} 0940464^2 + 488000^2 &= 1059536^2 \\ 12\,0940464^2 + 5368000^2 &= 121\,059536^2 \\ 1232\,0940464^2 + 54168000^2 &= 12321\,059536^2 \\ 12322\,0940464^2 + 542168000^2 &= 123221\,059536^2 \quad (5,241) \end{aligned}$$

$$\begin{aligned}
 0944304^2 + 472000^2 &= 1055696^2 \\
 12\,0944304^2 + 5192000^2 &= 121\,055696^2 \\
 1232\,0944304^2 + 52392000^2 &= 12321\,055696^2 \\
 123432\,0944304^2 + 524392000^2 &= 1234321\,055696^2 \quad (5.236)
 \end{aligned}$$

$$\begin{aligned}
 0939975^2 + 490000^2 &= 1060025^2 \\
 12\,0939975^2 + 5390000^2 &= 121\,060025^2 \\
 1232\,0939975^2 + 54390000^2 &= 12321\,060025^2 \\
 123432\,0939975^2 + 544390000^2 &= 1234321\,060025^2 \quad (5.245)
 \end{aligned}$$

$$\begin{aligned}
 0943831^2 + 474000^2 &= 1056169^2 \\
 12\,0943831^2 + 5214000^2 &= 121\,056169^2 \\
 1232\,0943831^2 + 52614000^2 &= 12321\,056169^2 \\
 123432\,0943831^2 + 526614000^2 &= 1234321\,056169^2 \quad (5.237)
 \end{aligned}$$

$$\begin{aligned}
 0939484^2 + 492000^2 &= 1060516^2 \\
 12\,0939484^2 + 5412000^2 &= 121\,060516^2 \\
 1232\,0939484^2 + 54612000^2 &= 12321\,060516^2 \\
 123432\,0939484^2 + 546612000^2 &= 1234321\,060516^2 \quad (5.246)
 \end{aligned}$$

$$\begin{aligned}
 0943356^2 + 476000^2 &= \mathbf{1056644}^2 \\
 12\,0943356^2 + 5236000^2 &= \mathbf{121\,056644}^2 \\
 1232\,0943356^2 + 52836000^2 &= \mathbf{12321\,056644}^2 \\
 123432\,0943356^2 + 528836000^2 &= \mathbf{1234321\,056644}^2 \quad (5.238)
 \end{aligned}$$

$$\begin{aligned}
 0938991^2 + 494000^2 &= 1061009^2 \\
 12\,0938991^2 + 5434000^2 &= 121\,061009^2 \\
 1232\,0938991^2 + 54834000^2 &= 12321\,061009^2 \\
 123432\,0938991^2 + 548834000^2 &= 1234321\,061009^2 \quad (5.247)
 \end{aligned}$$

$$\begin{aligned}
 0942879^2 + 478000^2 &= \mathbf{1}057121^2 \\
 12\,0942879^2 + 5258000^2 &= \mathbf{121}057121^2 \\
 1232\,0942879^2 + 53058000^2 &= \mathbf{12321}057121^2 \\
 123432\,0942879^2 + 531058000^2 &= \mathbf{1234321}057121^2 \quad (5.239)
 \end{aligned}$$

$$\begin{aligned} 0938496^2 + 496000^2 &= 1061504^2 \\ 12\,0938496^2 + 5456000^2 &= 121\,061504^2 \\ 1232\,0938496^2 + 55056000^2 &= 12321\,061504^2 \\ 123432\,0938496^2 + 551056000^2 &= 1234321\,061504^2 \quad (5.248) \end{aligned}$$

$$\begin{aligned}0942400^2 + 480000^2 &= \mathbf{1\,057\,600}^2 \\12\,094\,2400^2 + 5280000^2 &= \mathbf{121\,057\,600}^2 \\1232\,094\,2400^2 + 53280000^2 &= \mathbf{123\,21\,057\,600}^2 \\123432\,094\,2400^2 + 533280000^2 &= \mathbf{123\,432\,1\,057\,600}^2 \quad (5,240)\end{aligned}$$

$$\begin{aligned}
 0937999^2 + 498000^2 &= 1062001^2 \\
 12\,0937999^2 + 5478000^2 &= 121\,062001^2 \\
 1232\,0937999^2 + 55278000^2 &= 12321\,062001^2 \\
 123432\,0937999^2 + 553278000^2 &= 1234321\,062001^2 \quad (5.249)
 \end{aligned}$$

$$\begin{aligned} 0941919^2 + 482000^2 &= \textcolor{blue}{1} 058081^2 \\ 12\ 0941919^2 + 5302000^2 &= \textcolor{red}{121} 058081^2 \\ 1232\ 0941919^2 + 53502000^2 &= \textcolor{red}{12321} 058081^2 \\ 123432\ 0941919^2 + 535502000^2 &= \textcolor{red}{1234321} 058081^2 \quad (5.241) \end{aligned}$$

$$\begin{aligned}
& 0937500^2 + 500000^2 = \mathbf{1} 062500^2 \\
& \mathbf{12} 0937500^2 + 5500000^2 = \mathbf{121} 062500^2 \\
& \mathbf{1232} 0937500^2 + 55500000^2 = \mathbf{12321} 062500^2 \\
& \mathbf{123432} 0937500^2 + 555500000^2 = \mathbf{1234321} 062500^2 \quad (5.250) \\
& \\
& 0936999^2 + 502000^2 = \mathbf{1} 063001^2 \\
& \mathbf{12} 0936999^2 + 5522000^2 = \mathbf{121} 063001^2 \\
& \mathbf{1232} 0936999^2 + 55722000^2 = \mathbf{12321} 063001^2 \\
& \mathbf{123432} 0936999^2 + 557722000^2 = \mathbf{1234321} 063001^2 \quad (5.251) \\
& \\
& 0936496^2 + 504000^2 = \mathbf{1} 063504^2 \\
& \mathbf{12} 0936496^2 + 5544000^2 = \mathbf{121} 063504^2 \\
& \mathbf{1232} 0936496^2 + 55944000^2 = \mathbf{12321} 063504^2 \\
& \mathbf{123432} 0936496^2 + 559944000^2 = \mathbf{1234321} 063504^2 \quad (5.252) \\
& \\
& 0935991^2 + 506000^2 = \mathbf{1} 064009^2 \\
& \mathbf{12} 0935991^2 + 5566000^2 = \mathbf{121} 064009^2 \\
& \mathbf{1232} 0935991^2 + 56166000^2 = \mathbf{12321} 064009^2 \\
& \mathbf{123432} 0935991^2 + 562166000^2 = \mathbf{1234321} 064009^2 \quad (5.253) \\
& \\
& 0935484^2 + 508000^2 = \mathbf{1} 064516^2 \\
& \mathbf{12} 0935484^2 + 5588000^2 = \mathbf{121} 064516^2 \\
& \mathbf{1232} 0935484^2 + 56388000^2 = \mathbf{12321} 064516^2 \\
& \mathbf{123432} 0935484^2 + 564388000^2 = \mathbf{1234321} 064516^2 \quad (5.254) \\
& \\
& 0934975^2 + 510000^2 = \mathbf{1} 065025^2 \\
& \mathbf{12} 0934975^2 + 5610000^2 = \mathbf{121} 065025^2 \\
& \mathbf{1232} 0934975^2 + 56610000^2 = \mathbf{12321} 065025^2 \\
& \mathbf{123432} 0934975^2 + 566610000^2 = \mathbf{1234321} 065025^2 \quad (5.255) \\
& \\
& 0934464^2 + 512000^2 = \mathbf{1} 065536^2 \\
& \mathbf{12} 0934464^2 + 5632000^2 = \mathbf{121} 065536^2 \\
& \mathbf{1232} 0934464^2 + 56832000^2 = \mathbf{12321} 065536^2 \\
& \mathbf{123432} 0934464^2 + 568832000^2 = \mathbf{1234321} 065536^2 \quad (5.256) \\
& \\
& 0933951^2 + 514000^2 = \mathbf{1} 066049^2 \\
& \mathbf{12} 0933951^2 + 5654000^2 = \mathbf{121} 066049^2 \\
& \mathbf{1232} 0933951^2 + 57054000^2 = \mathbf{12321} 066049^2 \\
& \mathbf{123432} 0933951^2 + 571054000^2 = \mathbf{1234321} 066049^2 \quad (5.257) \\
& \\
& 0933436^2 + 516000^2 = \mathbf{1} 066564^2 \\
& \mathbf{12} 0933436^2 + 5676000^2 = \mathbf{121} 066564^2 \\
& \mathbf{1232} 0933436^2 + 57276000^2 = \mathbf{12321} 066564^2 \\
& \mathbf{123432} 0933436^2 + 573276000^2 = \mathbf{1234321} 066564^2 \quad (5.258)
\end{aligned}$$

$$\begin{aligned}
& 0932919^2 + 518000^2 = \mathbf{1} 067081^2 \\
& \mathbf{12} 0932919^2 + 5698000^2 = \mathbf{121} 067081^2 \\
& \mathbf{1232} 0932919^2 + 57498000^2 = \mathbf{12321} 067081^2 \\
& \mathbf{123432} 0932919^2 + 575498000^2 = \mathbf{1234321} 067081^2 \quad (5.259) \\
& \\
& 0932400^2 + 520000^2 = \mathbf{1} 067600^2 \\
& \mathbf{12} 0932400^2 + 5720000^2 = \mathbf{121} 067600^2 \\
& \mathbf{1232} 0932400^2 + 57720000^2 = \mathbf{12321} 067600^2 \\
& \mathbf{123432} 0932400^2 + 577720000^2 = \mathbf{1234321} 067600^2 \quad (5.260) \\
& \\
& 0931879^2 + 522000^2 = \mathbf{1} 068121^2 \\
& \mathbf{12} 0931879^2 + 5742000^2 = \mathbf{121} 068121^2 \\
& \mathbf{1232} 0931879^2 + 57942000^2 = \mathbf{12321} 068121^2 \\
& \mathbf{123432} 0931879^2 + 579942000^2 = \mathbf{1234321} 068121^2 \quad (5.261) \\
& \\
& 0931356^2 + 524000^2 = \mathbf{1} 068644^2 \\
& \mathbf{12} 0931356^2 + 5764000^2 = \mathbf{121} 068644^2 \\
& \mathbf{1232} 0931356^2 + 58164000^2 = \mathbf{12321} 068644^2 \\
& \mathbf{123432} 0931356^2 + 582164000^2 = \mathbf{1234321} 068644^2 \quad (5.262) \\
& \\
& 0930831^2 + 526000^2 = \mathbf{1} 069169^2 \\
& \mathbf{12} 0930831^2 + 5786000^2 = \mathbf{121} 069169^2 \\
& \mathbf{1232} 0930831^2 + 58386000^2 = \mathbf{12321} 069169^2 \\
& \mathbf{123432} 0930831^2 + 584386000^2 = \mathbf{1234321} 069169^2 \quad (5.263) \\
& \\
& 0930304^2 + 528000^2 = \mathbf{1} 069696^2 \\
& \mathbf{12} 0930304^2 + 5808000^2 = \mathbf{121} 069696^2 \\
& \mathbf{1232} 0930304^2 + 58608000^2 = \mathbf{12321} 069696^2 \\
& \mathbf{123432} 0930304^2 + 586608000^2 = \mathbf{1234321} 069696^2 \quad (5.264) \\
& \\
& 0929775^2 + 530000^2 = \mathbf{1} 070225^2 \\
& \mathbf{12} 0929775^2 + 5830000^2 = \mathbf{121} 070225^2 \\
& \mathbf{1232} 0929775^2 + 58830000^2 = \mathbf{12321} 070225^2 \\
& \mathbf{123432} 0929775^2 + 588830000^2 = \mathbf{1234321} 070225^2 \quad (5.265) \\
& \\
& 0929244^2 + 532000^2 = \mathbf{1} 070756^2 \\
& \mathbf{12} 0929244^2 + 5852000^2 = \mathbf{121} 070756^2 \\
& \mathbf{1232} 0929244^2 + 59052000^2 = \mathbf{12321} 070756^2 \\
& \mathbf{123432} 0929244^2 + 591052000^2 = \mathbf{1234321} 070756^2 \quad (5.266)
\end{aligned}$$

$$\begin{aligned}
 0928711^2 + 534000^2 &= 1071289^2 \\
 12\,0928711^2 + 5874000^2 &= 121\,071289^2 \\
 1232\,0928711^2 + 59274000^2 &= 12321\,071289^2 \\
 123432\,0928711^2 + 593274000^2 &= 1234321\,071289^2 \quad (5.267)
 \end{aligned}$$

$$\begin{aligned}
 0923824^2 + 552000^2 &= 1076176^2 \\
 12\,0923824^2 + 6072000^2 &= 121\,076176^2 \\
 1232\,0923824^2 + 61272000^2 &= 12321\,076176^2 \\
 123432\,0923824^2 + 613272000^2 &= 1234321\,076176^2 \quad (5.276)
 \end{aligned}$$

$$\begin{aligned}
 0928176^2 + 536000^2 &= \mathbf{1}071824^2 \\
 12\,0928176^2 + 5896000^2 &= \mathbf{121}\,071824^2 \\
 \mathbf{1232}\,0928176^2 + 59496000^2 &= \mathbf{12321}\,071824^2 \\
 \mathbf{123432}\,0928176^2 + 595496000^2 &= \mathbf{1234321}\,071824^2 \quad (5.268)
 \end{aligned}$$

$$\begin{aligned}
 0923271^2 + 554000^2 &= 1076729^2 \\
 12\,0923271^2 + 6094000^2 &= 121\,076729^2 \\
 1232\,0923271^2 + 61494000^2 &= 12321\,076729^2 \\
 123432\,0923271^2 + 615494000^2 &= 1234321\,076729^2 \quad (5.277)
 \end{aligned}$$

$$\begin{aligned}
 0927639^2 + 538000^2 &= 1072361^2 \\
 12\,0927639^2 + 5918000^2 &= 121\,072361^2 \\
 1232\,0927639^2 + 59718000^2 &= 12321\,072361^2 \\
 123432\,0927639^2 + 597718000^2 &= 1234321\,072361^2 \quad (5.269)
 \end{aligned}$$

$$\begin{aligned}
 0922716^2 + 556000^2 &= 1077284^2 \\
 12\,0922716^2 + 6116000^2 &= 121\,077284^2 \\
 1232\,0922716^2 + 61716000^2 &= 12321\,077284^2 \\
 123432\,0922716^2 + 617716000^2 &= 1234321\,077284^2 \quad (5.278)
 \end{aligned}$$

$$\begin{aligned}
 0927100^2 + 540000^2 &= 1072900^2 \\
 12\,0927100^2 + 5940000^2 &= 121\,072900^2 \\
 1232\,0927100^2 + 59940000^2 &= 12321\,072900^2 \\
 123432\,0927100^2 + 599940000^2 &= 1234321\,072900^2 \quad (5.270)
 \end{aligned}$$

$$\begin{aligned}
 0922159^2 + 558000^2 &= 1077841^2 \\
 12\,0922159^2 + 6138000^2 &= 121\,077841^2 \\
 1232\,0922159^2 + 61938000^2 &= 12321\,077841^2 \\
 123432\,0922159^2 + 619938000^2 &= 1234321\,077841^2 \quad (5.279)
 \end{aligned}$$

$$\begin{aligned}
 0926559^2 + 542000^2 &= 1073441^2 \\
 12\,0926559^2 + 5962000^2 &= 121\,073441^2 \\
 1232\,0926559^2 + 60162000^2 &= 12321\,073441^2 \\
 123432\,0926559^2 + 602162000^2 &= 1234321\,073441^2 \quad (5.271)
 \end{aligned}$$

$$\begin{aligned} 0921600^2 + 560000^2 &= 1078400^2 \\ 12\,0921600^2 + 6160000^2 &= 121\,078400^2 \\ 1232\,0921600^2 + 62160000^2 &= 12321\,078400^2 \\ 123432\,0921600^2 + 622160000^2 &= 1234321\,078400^2 \quad (5.280) \end{aligned}$$

$$\begin{aligned}
 0926016^2 + 544000^2 &= 1073984^2 \\
 12\,0926016^2 + 5984000^2 &= 121\,073984^2 \\
 1232\,0926016^2 + 60384000^2 &= 12321\,073984^2 \\
 123432\,0926016^2 + 604384000^2 &= 1234321\,073984^2 \quad (5.272)
 \end{aligned}$$

$$\begin{aligned} 0921039^2 + 562000^2 &= 1078961^2 \\ 12\,0921039^2 + 6182000^2 &= 121\,078961^2 \\ 1232\,0921039^2 + 62382000^2 &= 12321\,078961^2 \\ 123432\,0921039^2 + 624382000^2 &= 1234321\,078961^2 \quad (5.281) \end{aligned}$$

$$\begin{aligned}
 0925471^2 + 546000^2 &= \textcolor{red}{1} 074529^2 \\
 12 \, 0925471^2 + 6006000^2 &= \textcolor{red}{121} 074529^2 \\
 \textcolor{blue}{1232} \, 0925471^2 + 60606000^2 &= \textcolor{red}{12321} 074529^2 \\
 \textcolor{blue}{123432} \, 0925471^2 + 606606000^2 &= \textcolor{red}{1234321} 074529^2 \quad (5.273)
 \end{aligned}$$

$$\begin{aligned}
 0920476^2 + 564000^2 &= 1079524^2 \\
 12\,0920476^2 + 6204000^2 &= 121\,079524^2 \\
 1232\,0920476^2 + 62604000^2 &= 12321\,079524^2 \\
 123432\,0920476^2 + 626604000^2 &= 1234321\,079524^2 \quad (5.282)
 \end{aligned}$$

$$\begin{aligned}
 0924924^2 + 548000^2 &= 1075076^2 \\
 12\,0924924^2 + 6028000^2 &= 121\,075076^2 \\
 1232\,0924924^2 + 60828000^2 &= 12321\,075076^2 \\
 123432\,0924924^2 + 608828000^2 &= 1234321\,075076^2 \quad (5.274)
 \end{aligned}$$

$$\begin{aligned}
 0919911^2 + 566000^2 &= 1080089^2 \\
 12\,0919911^2 + 6226000^2 &= 121\,080089^2 \\
 1232\,0919911^2 + 62826000^2 &= 12321\,080089^2 \\
 123432\,0919911^2 + 628826000^2 &= 1234321\,080089^2 \quad (5.283)
 \end{aligned}$$

$$\begin{aligned} 0924375^2 + 550000^2 &= \mathbf{1075625^2} \\ 12\,0924375^2 + 6050000^2 &= \mathbf{121\,075625^2} \\ 1232\,0924375^2 + 61050000^2 &= \mathbf{12321\,075625^2} \\ 123432\,0924375^2 + 611050000^2 &= \mathbf{1234321\,075625^2} \quad (5.275) \end{aligned}$$

$0919344^2 + 568000^2 = \textcolor{red}{1} 080656^2$	$0914736^2 + 584000^2 = \textcolor{red}{1} 085264^2$
$12 0919344^2 + 6248000^2 = \textcolor{blue}{121} 080656^2$	$12 0914736^2 + 6424000^2 = \textcolor{blue}{121} 085264^2$
$1232 0919344^2 + 63048000^2 = \textcolor{blue}{12321} 080656^2$	$1232 0914736^2 + 64824000^2 = \textcolor{blue}{12321} 085264^2$
$123432 0919344^2 + 631048000^2 = \textcolor{blue}{1234321} 080656^2 \quad (5.284)$	$123432 0914736^2 + 648824000^2 = \textcolor{blue}{1234321} 085264^2 \quad (5.292)$
$0918775^2 + 570000^2 = \textcolor{red}{1} 081225^2$	$0914151^2 + 586000^2 = \textcolor{red}{1} 085849^2$
$12 0918775^2 + 6270000^2 = \textcolor{blue}{121} 081225^2$	$12 0914151^2 + 6446000^2 = \textcolor{blue}{121} 085849^2$
$1232 0918775^2 + 63270000^2 = \textcolor{blue}{12321} 081225^2$	$1232 0914151^2 + 65046000^2 = \textcolor{blue}{12321} 085849^2$
$123432 0918775^2 + 633270000^2 = \textcolor{blue}{1234321} 081225^2 \quad (5.285)$	$123432 0914151^2 + 651046000^2 = \textcolor{blue}{1234321} 085849^2 \quad (5.293)$
$0918204^2 + 572000^2 = \textcolor{red}{1} 081796^2$	$0913564^2 + 588000^2 = \textcolor{red}{1} 086436^2$
$12 0918204^2 + 6292000^2 = \textcolor{blue}{121} 081796^2$	$12 0913564^2 + 6468000^2 = \textcolor{blue}{121} 086436^2$
$1232 0918204^2 + 63492000^2 = \textcolor{blue}{12321} 081796^2$	$1232 0913564^2 + 65268000^2 = \textcolor{blue}{12321} 086436^2$
$123432 0918204^2 + 635492000^2 = \textcolor{blue}{1234321} 081796^2 \quad (5.286)$	$123432 0913564^2 + 653268000^2 = \textcolor{blue}{1234321} 086436^2 \quad (5.294)$
$0917631^2 + 574000^2 = \textcolor{red}{1} 082369^2$	$0912975^2 + 590000^2 = \textcolor{red}{1} 087025^2$
$12 0917631^2 + 6314000^2 = \textcolor{blue}{121} 082369^2$	$12 0912975^2 + 6490000^2 = \textcolor{blue}{121} 087025^2$
$1232 0917631^2 + 63714000^2 = \textcolor{blue}{12321} 082369^2$	$1232 0912975^2 + 65490000^2 = \textcolor{blue}{12321} 087025^2$
$123432 0917631^2 + 637714000^2 = \textcolor{blue}{1234321} 082369^2 \quad (5.287)$	$123432 0912975^2 + 655490000^2 = \textcolor{blue}{1234321} 087025^2 \quad (5.295)$
$0917056^2 + 576000^2 = \textcolor{red}{1} 082944^2$	$0912384^2 + 592000^2 = \textcolor{red}{1} 087616^2$
$12 0917056^2 + 6336000^2 = \textcolor{blue}{121} 082944^2$	$12 0912384^2 + 6512000^2 = \textcolor{blue}{121} 087616^2$
$1232 0917056^2 + 63936000^2 = \textcolor{blue}{12321} 082944^2$	$1232 0912384^2 + 65712000^2 = \textcolor{blue}{12321} 087616^2$
$123432 0917056^2 + 639936000^2 = \textcolor{blue}{1234321} 082944^2 \quad (5.288)$	$123432 0912384^2 + 657712000^2 = \textcolor{blue}{1234321} 087616^2 \quad (5.296)$
$0916479^2 + 578000^2 = \textcolor{red}{1} 083521^2$	$0911791^2 + 594000^2 = \textcolor{red}{1} 088209^2$
$12 0916479^2 + 6358000^2 = \textcolor{blue}{121} 083521^2$	$12 0911791^2 + 6534000^2 = \textcolor{blue}{121} 088209^2$
$1232 0916479^2 + 64158000^2 = \textcolor{blue}{12321} 083521^2$	$1232 0911791^2 + 65934000^2 = \textcolor{blue}{12321} 088209^2$
$123432 0916479^2 + 642158000^2 = \textcolor{blue}{1234321} 083521^2 \quad (5.289)$	$123432 0911791^2 + 659934000^2 = \textcolor{blue}{1234321} 088209^2 \quad (5.297)$
$0915900^2 + 580000^2 = \textcolor{red}{1} 084100^2$	$0911196^2 + 596000^2 = \textcolor{red}{1} 088804^2$
$12 0915900^2 + 6380000^2 = \textcolor{blue}{121} 084100^2$	$12 0911196^2 + 6556000^2 = \textcolor{blue}{121} 088804^2$
$1232 0915900^2 + 64380000^2 = \textcolor{blue}{12321} 084100^2$	$1232 0911196^2 + 66156000^2 = \textcolor{blue}{12321} 088804^2$
$123432 0915900^2 + 644380000^2 = \textcolor{blue}{1234321} 084100^2 \quad (5.290)$	$123432 0911196^2 + 662156000^2 = \textcolor{blue}{1234321} 088804^2 \quad (5.298)$
$0915319^2 + 582000^2 = \textcolor{red}{1} 084681^2$	$0910599^2 + 598000^2 = \textcolor{red}{1} 089401^2$
$12 0915319^2 + 6402000^2 = \textcolor{blue}{121} 084681^2$	$12 0910599^2 + 6578000^2 = \textcolor{blue}{121} 089401^2$
$1232 0915319^2 + 64602000^2 = \textcolor{blue}{12321} 084681^2$	$1232 0910599^2 + 66378000^2 = \textcolor{blue}{12321} 089401^2$
$123432 0915319^2 + 646602000^2 = \textcolor{blue}{1234321} 084681^2 \quad (5.291)$	$123432 0910599^2 + 664378000^2 = \textcolor{blue}{1234321} 089401^2 \quad (5.299)$

5.4 For $n = 300, 301, 301, \dots, 397, 398, 399$:

Let's consider

$$m = 1000, 11000, 111000, 1111000, 11111000, 111111000, 1111111000, 11111111000$$

in (1.1), then for each value of $n = 300, 301, 301, \dots, 397, 398, 399$; there are 100 *palindromic-type pandigital Pythagorean patterns* given below. In each case, only first four values are written. The other 5 values can be written on similar lines as done in subsection 5.1.1.

$0910000^2 + 600000^2 = 1090000^2$	$0905751^2 + 614000^2 = 1094249^2$
$12\ 0910000^2 + 6600000^2 = 121\ 090000^2$	$12\ 0905751^2 + 6754000^2 = 121\ 094249^2$
$1232\ 0910000^2 + 66600000^2 = 12321\ 090000^2$	$1232\ 0905751^2 + 68154000^2 = 12321\ 094249^2$
$123432\ 0910000^2 + 666600000^2 = 1234321\ 090000^2 \quad (5.300)$	$123432\ 0905751^2 + 682154000^2 = 1234321\ 094249^2 \quad (5.307)$
$0909399^2 + 602000^2 = 1090601^2$	$0905136^2 + 616000^2 = 1094864^2$
$12\ 0909399^2 + 6622000^2 = 121\ 090601^2$	$12\ 0905136^2 + 6776000^2 = 121\ 094864^2$
$1232\ 0909399^2 + 66822000^2 = 12321\ 090601^2$	$1232\ 0905136^2 + 68376000^2 = 12321\ 094864^2$
$123432\ 0909399^2 + 668822000^2 = 1234321\ 090601^2 \quad (5.301)$	$123432\ 0905136^2 + 684376000^2 = 1234321\ 094864^2 \quad (5.308)$
$0908796^2 + 604000^2 = 1091204^2$	$0904519^2 + 618000^2 = 1095481^2$
$12\ 0908796^2 + 6644000^2 = 121\ 091204^2$	$12\ 0904519^2 + 6798000^2 = 121\ 095481^2$
$1232\ 0908796^2 + 67044000^2 = 12321\ 091204^2$	$1232\ 0904519^2 + 68598000^2 = 12321\ 095481^2$
$123432\ 0908796^2 + 671044000^2 = 1234321\ 091204^2 \quad (5.302)$	$123432\ 0904519^2 + 686598000^2 = 1234321\ 095481^2 \quad (5.309)$
$0908191^2 + 606000^2 = 1091809^2$	$0903900^2 + 620000^2 = 1096100^2$
$12\ 0908191^2 + 6666000^2 = 121\ 091809^2$	$12\ 0903900^2 + 6820000^2 = 121\ 096100^2$
$1232\ 0908191^2 + 67266000^2 = 12321\ 091809^2$	$1232\ 0903900^2 + 68820000^2 = 12321\ 096100^2$
$123432\ 0908191^2 + 673266000^2 = 1234321\ 091809^2 \quad (5.303)$	$123432\ 0903900^2 + 688820000^2 = 1234321\ 096100^2 \quad (5.310)$
$0907584^2 + 608000^2 = 1092416^2$	$0903279^2 + 622000^2 = 1096721^2$
$12\ 0907584^2 + 6688000^2 = 121\ 092416^2$	$12\ 0903279^2 + 6842000^2 = 121\ 096721^2$
$1232\ 0907584^2 + 67488000^2 = 12321\ 092416^2$	$1232\ 0903279^2 + 69042000^2 = 12321\ 096721^2$
$123432\ 0907584^2 + 675488000^2 = 1234321\ 092416^2 \quad (5.304)$	$123432\ 0903279^2 + 691042000^2 = 1234321\ 096721^2 \quad (5.311)$
$0906975^2 + 610000^2 = 1093025^2$	$0902656^2 + 624000^2 = 1097344^2$
$12\ 0906975^2 + 6710000^2 = 121\ 093025^2$	$12\ 0902656^2 + 6864000^2 = 121\ 097344^2$
$1232\ 0906975^2 + 67710000^2 = 12321\ 093025^2$	$1232\ 0902656^2 + 69264000^2 = 12321\ 097344^2$
$123432\ 0906975^2 + 677710000^2 = 1234321\ 093025^2 \quad (5.305)$	$123432\ 0902656^2 + 693264000^2 = 1234321\ 097344^2 \quad (5.312)$
$0906364^2 + 612000^2 = 1093636^2$	$0902031^2 + 626000^2 = 1097969^2$
$12\ 0906364^2 + 6732000^2 = 121\ 093636^2$	$12\ 0902031^2 + 6886000^2 = 121\ 097969^2$
$1232\ 0906364^2 + 67932000^2 = 12321\ 093636^2$	$1232\ 0902031^2 + 69486000^2 = 12321\ 097969^2$
$123432\ 0906364^2 + 679932000^2 = 1234321\ 093636^2 \quad (5.306)$	$123432\ 0902031^2 + 695486000^2 = 1234321\ 097969^2 \quad (5.313)$

$$\begin{aligned}
& 0901404^2 + 628000^2 = \mathbf{1} 098596^2 \\
& \mathbf{12} 0901404^2 + 6908000^2 = \mathbf{121} 098596^2 \\
& \mathbf{1232} 0901404^2 + 69708000^2 = \mathbf{12321} 098596^2 \\
& \mathbf{123432} 0901404^2 + 697708000^2 = \mathbf{1234321} 098596^2 \quad (5.314)
\end{aligned}$$

$$\begin{aligned}
& 0900775^2 + 630000^2 = \mathbf{1} 099225^2 \\
& \mathbf{12} 0900775^2 + 6930000^2 = \mathbf{121} 099225^2 \\
& \mathbf{1232} 0900775^2 + 69930000^2 = \mathbf{12321} 099225^2 \\
& \mathbf{123432} 0900775^2 + 699930000^2 = \mathbf{1234321} 099225^2 \quad (5.315)
\end{aligned}$$

$$\begin{aligned}
& 0900144^2 + 632000^2 = \mathbf{1} 099856^2 \\
& \mathbf{12} 0900144^2 + 6952000^2 = \mathbf{121} 099856^2 \\
& \mathbf{1232} 0900144^2 + 70152000^2 = \mathbf{12321} 099856^2 \\
& \mathbf{123432} 0900144^2 + 702152000^2 = \mathbf{1234321} 099856^2 \quad (5.316)
\end{aligned}$$

$$\begin{aligned}
& 0899511^2 + 634000^2 = \mathbf{1} 100489^2 \\
& \mathbf{12} 0899511^2 + 6974000^2 = \mathbf{121} 100489^2 \\
& \mathbf{1232} 0899511^2 + 70374000^2 = \mathbf{12321} 100489^2 \\
& \mathbf{123432} 0899511^2 + 704374000^2 = \mathbf{1234321} 100489^2 \quad (5.317)
\end{aligned}$$

$$\begin{aligned}
& 0898876^2 + 636000^2 = \mathbf{1} 101124^2 \\
& \mathbf{12} 0898876^2 + 6996000^2 = \mathbf{121} 101124^2 \\
& \mathbf{1232} 0898876^2 + 70596000^2 = \mathbf{12321} 101124^2 \\
& \mathbf{123432} 0898876^2 + 706596000^2 = \mathbf{1234321} 101124^2 \quad (5.318)
\end{aligned}$$

$$\begin{aligned}
& 0898239^2 + 638000^2 = \mathbf{1} 101761^2 \\
& \mathbf{12} 0898239^2 + 7018000^2 = \mathbf{121} 101761^2 \\
& \mathbf{1232} 0898239^2 + 70818000^2 = \mathbf{12321} 101761^2 \\
& \mathbf{123432} 0898239^2 + 708818000^2 = \mathbf{1234321} 101761^2 \quad (5.319)
\end{aligned}$$

$$\begin{aligned}
& 0897600^2 + 640000^2 = \mathbf{1} 102400^2 \\
& \mathbf{12} 0897600^2 + 7040000^2 = \mathbf{121} 102400^2 \\
& \mathbf{1232} 0897600^2 + 71040000^2 = \mathbf{12321} 102400^2 \\
& \mathbf{123432} 0897600^2 + 711040000^2 = \mathbf{1234321} 102400^2 \quad (5.320)
\end{aligned}$$

$$\begin{aligned}
& 0896959^2 + 642000^2 = \mathbf{1} 103041^2 \\
& \mathbf{12} 0896959^2 + 7062000^2 = \mathbf{121} 103041^2 \\
& \mathbf{1232} 0896959^2 + 71262000^2 = \mathbf{12321} 103041^2 \\
& \mathbf{123432} 0896959^2 + 713262000^2 = \mathbf{1234321} 103041^2 \quad (5.321)
\end{aligned}$$

$$\begin{aligned}
& 0896316^2 + 644000^2 = \mathbf{1} 103684^2 \\
& \mathbf{12} 0896316^2 + 7084000^2 = \mathbf{121} 103684^2 \\
& \mathbf{1232} 0896316^2 + 71484000^2 = \mathbf{12321} 103684^2 \\
& \mathbf{123432} 0896316^2 + 715484000^2 = \mathbf{1234321} 103684^2 \quad (5.322)
\end{aligned}$$

$$\begin{aligned}
& 0895671^2 + 646000^2 = \mathbf{1} 104329^2 \\
& \mathbf{12} 0895671^2 + 7106000^2 = \mathbf{121} 104329^2 \\
& \mathbf{1232} 0895671^2 + 71706000^2 = \mathbf{12321} 104329^2 \\
& \mathbf{123432} 0895671^2 + 717706000^2 = \mathbf{1234321} 104329^2 \quad (5.323)
\end{aligned}$$

$$\begin{aligned}
& 0895024^2 + 648000^2 = \mathbf{1} 104976^2 \\
& \mathbf{12} 0895024^2 + 7128000^2 = \mathbf{121} 104976^2 \\
& \mathbf{1232} 0895024^2 + 71928000^2 = \mathbf{12321} 104976^2 \\
& \mathbf{123432} 0895024^2 + 719928000^2 = \mathbf{1234321} 104976^2 \quad (5.324)
\end{aligned}$$

$$\begin{aligned}
& 0894375^2 + 650000^2 = \mathbf{1} 105625^2 \\
& \mathbf{12} 0894375^2 + 7150000^2 = \mathbf{121} 105625^2 \\
& \mathbf{1232} 0894375^2 + 72150000^2 = \mathbf{12321} 105625^2 \\
& \mathbf{123432} 0894375^2 + 722150000^2 = \mathbf{1234321} 105625^2 \quad (5.325)
\end{aligned}$$

$$\begin{aligned}
& 0893724^2 + 652000^2 = \mathbf{1} 106276^2 \\
& \mathbf{12} 0893724^2 + 7172000^2 = \mathbf{121} 106276^2 \\
& \mathbf{1232} 0893724^2 + 72372000^2 = \mathbf{12321} 106276^2 \\
& \mathbf{123432} 0893724^2 + 724372000^2 = \mathbf{1234321} 106276^2 \quad (5.326)
\end{aligned}$$

$$\begin{aligned}
& 0893071^2 + 654000^2 = \mathbf{1} 106929^2 \\
& \mathbf{12} 0893071^2 + 7194000^2 = \mathbf{121} 106929^2 \\
& \mathbf{1232} 0893071^2 + 72594000^2 = \mathbf{12321} 106929^2 \\
& \mathbf{123432} 0893071^2 + 726594000^2 = \mathbf{1234321} 106929^2 \quad (5.327)
\end{aligned}$$

$$\begin{aligned}
& 0892416^2 + 656000^2 = \mathbf{1} 107584^2 \\
& \mathbf{12} 0892416^2 + 7216000^2 = \mathbf{121} 107584^2 \\
& \mathbf{1232} 0892416^2 + 72816000^2 = \mathbf{12321} 107584^2 \\
& \mathbf{123432} 0892416^2 + 728816000^2 = \mathbf{1234321} 107584^2 \quad (5.328)
\end{aligned}$$

$$\begin{aligned}
& 0891759^2 + 658000^2 = \mathbf{1} 108241^2 \\
& \mathbf{12} 0891759^2 + 7238000^2 = \mathbf{121} 108241^2 \\
& \mathbf{1232} 0891759^2 + 73038000^2 = \mathbf{12321} 108241^2 \\
& \mathbf{123432} 0891759^2 + 731038000^2 = \mathbf{1234321} 108241^2 \quad (5.329)
\end{aligned}$$

$$\begin{aligned}
& 0891100^2 + 660000^2 = \mathbf{1} 108900^2 \\
& \mathbf{12} 0891100^2 + 7260000^2 = \mathbf{121} 108900^2 \\
& \mathbf{1232} 0891100^2 + 73260000^2 = \mathbf{12321} 108900^2 \\
& \mathbf{123432} 0891100^2 + 733260000^2 = \mathbf{1234321} 108900^2 \quad (5.330)
\end{aligned}$$

$$\begin{aligned}
& 0890439^2 + 662000^2 = \mathbf{1} 109561^2 \\
& \mathbf{12} 0890439^2 + 7282000^2 = \mathbf{121} 109561^2 \\
& \mathbf{1232} 0890439^2 + 73482000^2 = \mathbf{12321} 109561^2 \\
& \mathbf{123432} 0890439^2 + 735482000^2 = \mathbf{1234321} 109561^2 \quad (5.331)
\end{aligned}$$

$$\begin{aligned}
& 0889776^2 + 664000^2 = \mathbf{1} 110224^2 \\
& \mathbf{12} 0889776^2 + 7304000^2 = \mathbf{121} 110224^2 \\
& \mathbf{1232} 0889776^2 + 73704000^2 = \mathbf{12321} 110224^2 \\
& \mathbf{123432} 0889776^2 + 737704000^2 = \mathbf{1234321} 110224^2 \quad (5.332)
\end{aligned}$$

$$\begin{aligned}
& 0889111^2 + 666000^2 = \mathbf{1} 110889^2 \\
& \mathbf{12} 0889111^2 + 7326000^2 = \mathbf{121} 110889^2 \\
& \mathbf{1232} 0889111^2 + 73926000^2 = \mathbf{12321} 110889^2 \\
& \mathbf{123432} 0889111^2 + 739926000^2 = \mathbf{1234321} 110889^2 \quad (5.333)
\end{aligned}$$

$$\begin{aligned}
& 0888444^2 + 668000^2 = \mathbf{1} 111556^2 \\
& \mathbf{12} 0888444^2 + 7348000^2 = \mathbf{121} 111556^2 \\
& \mathbf{1232} 0888444^2 + 74148000^2 = \mathbf{12321} 111556^2 \\
& \mathbf{123432} 0888444^2 + 742148000^2 = \mathbf{1234321} 111556^2 \quad (5.334)
\end{aligned}$$

$$\begin{aligned}
& 0887775^2 + 670000^2 = \mathbf{1} 112225^2 \\
& \mathbf{12} 0887775^2 + 7370000^2 = \mathbf{121} 112225^2 \\
& \mathbf{1232} 0887775^2 + 74370000^2 = \mathbf{12321} 112225^2 \\
& \mathbf{123432} 0887775^2 + 744370000^2 = \mathbf{1234321} 112225^2 \quad (5.335)
\end{aligned}$$

$$\begin{aligned}
& 0887104^2 + 672000^2 = \mathbf{1} 112896^2 \\
& \mathbf{12} 0887104^2 + 7392000^2 = \mathbf{121} 112896^2 \\
& \mathbf{1232} 0887104^2 + 74592000^2 = \mathbf{12321} 112896^2 \\
& \mathbf{123432} 0887104^2 + 746592000^2 = \mathbf{1234321} 112896^2 \quad (5.336)
\end{aligned}$$

$$\begin{aligned}
& 0886431^2 + 674000^2 = \mathbf{1} 113569^2 \\
& \mathbf{12} 0886431^2 + 7414000^2 = \mathbf{121} 113569^2 \\
& \mathbf{1232} 0886431^2 + 74814000^2 = \mathbf{12321} 113569^2 \\
& \mathbf{123432} 0886431^2 + 748814000^2 = \mathbf{1234321} 113569^2 \quad (5.337)
\end{aligned}$$

$$\begin{aligned}
& 0885756^2 + 676000^2 = \mathbf{1} 114244^2 \\
& \mathbf{12} 0885756^2 + 7436000^2 = \mathbf{121} 114244^2 \\
& \mathbf{1232} 0885756^2 + 75036000^2 = \mathbf{12321} 114244^2 \\
& \mathbf{123432} 0885756^2 + 751036000^2 = \mathbf{1234321} 114244^2 \quad (5.338)
\end{aligned}$$

$$\begin{aligned}
& 0885079^2 + 678000^2 = \mathbf{1} 114921^2 \\
& \mathbf{12} 0885079^2 + 7458000^2 = \mathbf{121} 114921^2 \\
& \mathbf{1232} 0885079^2 + 75258000^2 = \mathbf{12321} 114921^2 \\
& \mathbf{123432} 0885079^2 + 753258000^2 = \mathbf{1234321} 114921^2 \quad (5.339)
\end{aligned}$$

$$\begin{aligned}
& 0884400^2 + 680000^2 = \mathbf{1} 115600^2 \\
& \mathbf{12} 0884400^2 + 7480000^2 = \mathbf{121} 115600^2 \\
& \mathbf{1232} 0884400^2 + 75480000^2 = \mathbf{12321} 115600^2 \\
& \mathbf{123432} 0884400^2 + 755480000^2 = \mathbf{1234321} 115600^2 \quad (5.340)
\end{aligned}$$

$$\begin{aligned}
& 0883719^2 + 682000^2 = \mathbf{1} 116281^2 \\
& \mathbf{12} 0883719^2 + 7502000^2 = \mathbf{121} 116281^2 \\
& \mathbf{1232} 0883719^2 + 75702000^2 = \mathbf{12321} 116281^2 \\
& \mathbf{123432} 0883719^2 + 757702000^2 = \mathbf{1234321} 116281^2 \quad (5.341)
\end{aligned}$$

$$\begin{aligned}
& 0883036^2 + 684000^2 = \mathbf{1} 116964^2 \\
& \mathbf{12} 0883036^2 + 7524000^2 = \mathbf{121} 116964^2 \\
& \mathbf{1232} 0883036^2 + 75924000^2 = \mathbf{12321} 116964^2 \\
& \mathbf{123432} 0883036^2 + 759924000^2 = \mathbf{1234321} 116964^2 \quad (5.342)
\end{aligned}$$

$$\begin{aligned}
& 0882351^2 + 686000^2 = \mathbf{1} 117649^2 \\
& \mathbf{12} 0882351^2 + 7546000^2 = \mathbf{121} 117649^2 \\
& \mathbf{1232} 0882351^2 + 76146000^2 = \mathbf{12321} 117649^2 \\
& \mathbf{123432} 0882351^2 + 762146000^2 = \mathbf{1234321} 117649^2 \quad (5.343)
\end{aligned}$$

$$\begin{aligned}
& 0881664^2 + 688000^2 = \mathbf{1} 118336^2 \\
& \mathbf{12} 0881664^2 + 7568000^2 = \mathbf{121} 118336^2 \\
& \mathbf{1232} 0881664^2 + 76368000^2 = \mathbf{12321} 118336^2 \\
& \mathbf{123432} 0881664^2 + 764368000^2 = \mathbf{1234321} 118336^2 \quad (5.344)
\end{aligned}$$

$$\begin{aligned}
& 0880975^2 + 690000^2 = \mathbf{1} 119025^2 \\
& \mathbf{12} 0880975^2 + 7590000^2 = \mathbf{121} 119025^2 \\
& \mathbf{1232} 0880975^2 + 76590000^2 = \mathbf{12321} 119025^2 \\
& \mathbf{123432} 0880975^2 + 766590000^2 = \mathbf{1234321} 119025^2 \quad (5.345)
\end{aligned}$$

$$\begin{aligned}
& 0880284^2 + 692000^2 = \mathbf{1} 119716^2 \\
& \mathbf{12} 0880284^2 + 7612000^2 = \mathbf{121} 119716^2 \\
& \mathbf{1232} 0880284^2 + 76812000^2 = \mathbf{12321} 119716^2 \\
& \mathbf{123432} 0880284^2 + 768812000^2 = \mathbf{1234321} 119716^2 \quad (5.346)
\end{aligned}$$

$$\begin{aligned}
& 0879591^2 + 694000^2 = \mathbf{1} 120409^2 \\
& \mathbf{12} 0879591^2 + 7634000^2 = \mathbf{121} 120409^2 \\
& \mathbf{1232} 0879591^2 + 77034000^2 = \mathbf{12321} 120409^2 \\
& \mathbf{123432} 0879591^2 + 771034000^2 = \mathbf{1234321} 120409^2 \quad (5.347)
\end{aligned}$$

$$\begin{aligned}
& 0878896^2 + 696000^2 = \mathbf{1} \ 121104^2 \\
& \mathbf{12} \ 0878896^2 + 7656000^2 = \mathbf{121} \ 121104^2 \\
& \mathbf{1232} \ 0878896^2 + 77256000^2 = \mathbf{12321} \ 121104^2 \\
& \mathbf{123432} \ 0878896^2 + 773256000^2 = \mathbf{1234321} \ 121104^2 \quad (5.348)
\end{aligned}$$

$$\begin{aligned}
& 0878199^2 + 698000^2 = \mathbf{1} \ 121801^2 \\
& \mathbf{12} \ 0878199^2 + 7678000^2 = \mathbf{121} \ 121801^2 \\
& \mathbf{1232} \ 0878199^2 + 77478000^2 = \mathbf{12321} \ 121801^2 \\
& \mathbf{123432} \ 0878199^2 + 775478000^2 = \mathbf{1234321} \ 121801^2 \quad (5.349)
\end{aligned}$$

$$\begin{aligned}
& 0877500^2 + 700000^2 = \mathbf{1} \ 122500^2 \\
& \mathbf{12} \ 0877500^2 + 7700000^2 = \mathbf{121} \ 122500^2 \\
& \mathbf{1232} \ 0877500^2 + 77700000^2 = \mathbf{12321} \ 122500^2 \\
& \mathbf{123432} \ 0877500^2 + 777700000^2 = \mathbf{1234321} \ 122500^2 \quad (5.350)
\end{aligned}$$

$$\begin{aligned}
& 0876799^2 + 702000^2 = \mathbf{1} \ 123201^2 \\
& \mathbf{12} \ 0876799^2 + 7722000^2 = \mathbf{121} \ 123201^2 \\
& \mathbf{1232} \ 0876799^2 + 77922000^2 = \mathbf{12321} \ 123201^2 \\
& \mathbf{123432} \ 0876799^2 + 779922000^2 = \mathbf{1234321} \ 123201^2 \quad (5.351)
\end{aligned}$$

$$\begin{aligned}
& 0876096^2 + 704000^2 = \mathbf{1} \ 123904^2 \\
& \mathbf{12} \ 0876096^2 + 7744000^2 = \mathbf{121} \ 123904^2 \\
& \mathbf{1232} \ 0876096^2 + 78144000^2 = \mathbf{12321} \ 123904^2 \\
& \mathbf{123432} \ 0876096^2 + 782144000^2 = \mathbf{1234321} \ 123904^2 \quad (5.352)
\end{aligned}$$

$$\begin{aligned}
& 0875391^2 + 706000^2 = \mathbf{1} \ 124609^2 \\
& \mathbf{12} \ 0875391^2 + 7766000^2 = \mathbf{121} \ 124609^2 \\
& \mathbf{1232} \ 0875391^2 + 78366000^2 = \mathbf{12321} \ 124609^2 \\
& \mathbf{123432} \ 0875391^2 + 784366000^2 = \mathbf{1234321} \ 124609^2 \quad (5.353)
\end{aligned}$$

$$\begin{aligned}
& 0874684^2 + 708000^2 = \mathbf{1} \ 125316^2 \\
& \mathbf{12} \ 0874684^2 + 7788000^2 = \mathbf{121} \ 125316^2 \\
& \mathbf{1232} \ 0874684^2 + 78588000^2 = \mathbf{12321} \ 125316^2 \\
& \mathbf{123432} \ 0874684^2 + 786588000^2 = \mathbf{1234321} \ 125316^2 \quad (5.354)
\end{aligned}$$

$$\begin{aligned}
& 0873975^2 + 710000^2 = \mathbf{1} \ 126025^2 \\
& \mathbf{12} \ 0873975^2 + 7810000^2 = \mathbf{121} \ 126025^2 \\
& \mathbf{1232} \ 0873975^2 + 78810000^2 = \mathbf{12321} \ 126025^2 \\
& \mathbf{123432} \ 0873975^2 + 788810000^2 = \mathbf{1234321} \ 126025^2 \quad (5.355)
\end{aligned}$$

$$\begin{aligned}
& 0873264^2 + 712000^2 = \mathbf{1} \ 126736^2 \\
& \mathbf{12} \ 0873264^2 + 7832000^2 = \mathbf{121} \ 126736^2 \\
& \mathbf{1232} \ 0873264^2 + 79032000^2 = \mathbf{12321} \ 126736^2 \\
& \mathbf{123432} \ 0873264^2 + 791032000^2 = \mathbf{1234321} \ 126736^2 \quad (5.356)
\end{aligned}$$

$$\begin{aligned}
& 0872551^2 + 714000^2 = \mathbf{1} \ 127449^2 \\
& \mathbf{12} \ 0872551^2 + 7854000^2 = \mathbf{121} \ 127449^2 \\
& \mathbf{1232} \ 0872551^2 + 79254000^2 = \mathbf{12321} \ 127449^2 \\
& \mathbf{123432} \ 0872551^2 + 793254000^2 = \mathbf{1234321} \ 127449^2 \quad (5.357)
\end{aligned}$$

$$\begin{aligned}
& 0871836^2 + 716000^2 = \mathbf{1} \ 128164^2 \\
& \mathbf{12} \ 0871836^2 + 7876000^2 = \mathbf{121} \ 128164^2 \\
& \mathbf{1232} \ 0871836^2 + 79476000^2 = \mathbf{12321} \ 128164^2 \\
& \mathbf{123432} \ 0871836^2 + 795476000^2 = \mathbf{1234321} \ 128164^2 \quad (5.358)
\end{aligned}$$

$$\begin{aligned}
& 0871119^2 + 718000^2 = \mathbf{1} \ 128881^2 \\
& \mathbf{12} \ 0871119^2 + 7898000^2 = \mathbf{121} \ 128881^2 \\
& \mathbf{1232} \ 0871119^2 + 79698000^2 = \mathbf{12321} \ 128881^2 \\
& \mathbf{123432} \ 0871119^2 + 797698000^2 = \mathbf{1234321} \ 128881^2 \quad (5.359)
\end{aligned}$$

$$\begin{aligned}
& 0870400^2 + 720000^2 = \mathbf{1} \ 129600^2 \\
& \mathbf{12} \ 0870400^2 + 7920000^2 = \mathbf{121} \ 129600^2 \\
& \mathbf{1232} \ 0870400^2 + 79920000^2 = \mathbf{12321} \ 129600^2 \\
& \mathbf{123432} \ 0870400^2 + 799920000^2 = \mathbf{1234321} \ 129600^2 \quad (5.360)
\end{aligned}$$

$$\begin{aligned}
& 0869679^2 + 722000^2 = \mathbf{1} \ 130321^2 \\
& \mathbf{12} \ 0869679^2 + 7942000^2 = \mathbf{121} \ 130321^2 \\
& \mathbf{1232} \ 0869679^2 + 80142000^2 = \mathbf{12321} \ 130321^2 \\
& \mathbf{123432} \ 0869679^2 + 802142000^2 = \mathbf{1234321} \ 130321^2 \quad (5.361)
\end{aligned}$$

$$\begin{aligned}
& 0868956^2 + 724000^2 = \mathbf{1} \ 131044^2 \\
& \mathbf{12} \ 0868956^2 + 7964000^2 = \mathbf{121} \ 131044^2 \\
& \mathbf{1232} \ 0868956^2 + 80364000^2 = \mathbf{12321} \ 131044^2 \\
& \mathbf{123432} \ 0868956^2 + 804364000^2 = \mathbf{1234321} \ 131044^2 \quad (5.362)
\end{aligned}$$

$$\begin{aligned}
& 0868231^2 + 726000^2 = \mathbf{1} \ 131769^2 \\
& \mathbf{12} \ 0868231^2 + 7986000^2 = \mathbf{121} \ 131769^2 \\
& \mathbf{1232} \ 0868231^2 + 80586000^2 = \mathbf{12321} \ 131769^2 \\
& \mathbf{123432} \ 0868231^2 + 806586000^2 = \mathbf{1234321} \ 131769^2 \quad (5.363)
\end{aligned}$$

$$\begin{aligned}
& 0867504^2 + 728000^2 = \mathbf{1} \ 132496^2 \\
& \mathbf{12} \ 0867504^2 + 8008000^2 = \mathbf{121} \ 132496^2 \\
& \mathbf{1232} \ 0867504^2 + 80808000^2 = \mathbf{12321} \ 132496^2 \\
& \mathbf{123432} \ 0867504^2 + 808808000^2 = \mathbf{1234321} \ 132496^2 \quad (5.364)
\end{aligned}$$

$$\begin{aligned}
& 0866775^2 + 730000^2 = \mathbf{1} \ 133225^2 \\
& \mathbf{12} \ 0866775^2 + 8030000^2 = \mathbf{121} \ 133225^2 \\
& \mathbf{1232} \ 0866775^2 + 81030000^2 = \mathbf{12321} \ 133225^2 \\
& \mathbf{123432} \ 0866775^2 + 811030000^2 = \mathbf{1234321} \ 133225^2 \quad (5.365) \\
& \\
& 0866044^2 + 732000^2 = \mathbf{1} \ 133956^2 \\
& \mathbf{12} \ 0866044^2 + 8052000^2 = \mathbf{121} \ 133956^2 \\
& \mathbf{1232} \ 0866044^2 + 81252000^2 = \mathbf{12321} \ 133956^2 \\
& \mathbf{123432} \ 0866044^2 + 813252000^2 = \mathbf{1234321} \ 133956^2 \quad (5.366) \\
& \\
& 0865311^2 + 734000^2 = \mathbf{1} \ 134689^2 \\
& \mathbf{12} \ 0865311^2 + 8074000^2 = \mathbf{121} \ 134689^2 \\
& \mathbf{1232} \ 0865311^2 + 81474000^2 = \mathbf{12321} \ 134689^2 \\
& \mathbf{123432} \ 0865311^2 + 815474000^2 = \mathbf{1234321} \ 134689^2 \quad (5.367) \\
& \\
& 0864576^2 + 736000^2 = \mathbf{1} \ 135424^2 \\
& \mathbf{12} \ 0864576^2 + 8096000^2 = \mathbf{121} \ 135424^2 \\
& \mathbf{1232} \ 0864576^2 + 81696000^2 = \mathbf{12321} \ 135424^2 \\
& \mathbf{123432} \ 0864576^2 + 817696000^2 = \mathbf{1234321} \ 135424^2 \quad (5.368) \\
& \\
& 0863839^2 + 738000^2 = \mathbf{1} \ 136161^2 \\
& \mathbf{12} \ 0863839^2 + 8118000^2 = \mathbf{121} \ 136161^2 \\
& \mathbf{1232} \ 0863839^2 + 81918000^2 = \mathbf{12321} \ 136161^2 \\
& \mathbf{123432} \ 0863839^2 + 819918000^2 = \mathbf{1234321} \ 136161^2 \quad (5.369) \\
& \\
& 0863100^2 + 740000^2 = \mathbf{1} \ 136900^2 \\
& \mathbf{12} \ 0863100^2 + 8140000^2 = \mathbf{121} \ 136900^2 \\
& \mathbf{1232} \ 0863100^2 + 82140000^2 = \mathbf{12321} \ 136900^2 \\
& \mathbf{123432} \ 0863100^2 + 822140000^2 = \mathbf{1234321} \ 136900^2 \quad (5.370) \\
& \\
& 0862359^2 + 742000^2 = \mathbf{1} \ 137641^2 \\
& \mathbf{12} \ 0862359^2 + 8162000^2 = \mathbf{121} \ 137641^2 \\
& \mathbf{1232} \ 0862359^2 + 82362000^2 = \mathbf{12321} \ 137641^2 \\
& \mathbf{123432} \ 0862359^2 + 824362000^2 = \mathbf{1234321} \ 137641^2 \quad (5.371) \\
& \\
& 0861616^2 + 744000^2 = \mathbf{1} \ 138384^2 \\
& \mathbf{12} \ 0861616^2 + 8184000^2 = \mathbf{121} \ 138384^2 \\
& \mathbf{1232} \ 0861616^2 + 82584000^2 = \mathbf{12321} \ 138384^2 \\
& \mathbf{123432} \ 0861616^2 + 826584000^2 = \mathbf{1234321} \ 138384^2 \quad (5.372) \\
& \\
& 0860871^2 + 746000^2 = \mathbf{1} \ 139129^2 \\
& \mathbf{12} \ 0860871^2 + 8206000^2 = \mathbf{121} \ 139129^2 \\
& \mathbf{1232} \ 0860871^2 + 82806000^2 = \mathbf{12321} \ 139129^2 \\
& \mathbf{123432} \ 0860871^2 + 828806000^2 = \mathbf{1234321} \ 139129^2 \quad (5.373) \\
& \\
& 0860124^2 + 748000^2 = \mathbf{1} \ 139876^2 \\
& \mathbf{12} \ 0860124^2 + 8228000^2 = \mathbf{121} \ 139876^2 \\
& \mathbf{1232} \ 0860124^2 + 83028000^2 = \mathbf{12321} \ 139876^2 \\
& \mathbf{123432} \ 0860124^2 + 831028000^2 = \mathbf{1234321} \ 139876^2 \quad (5.374) \\
& \\
& 0859375^2 + 750000^2 = \mathbf{1} \ 140625^2 \\
& \mathbf{12} \ 0859375^2 + 8250000^2 = \mathbf{121} \ 140625^2 \\
& \mathbf{1232} \ 0859375^2 + 83250000^2 = \mathbf{12321} \ 140625^2 \\
& \mathbf{123432} \ 0859375^2 + 833250000^2 = \mathbf{1234321} \ 140625^2 \quad (5.375) \\
& \\
& 0858624^2 + 752000^2 = \mathbf{1} \ 141376^2 \\
& \mathbf{12} \ 0858624^2 + 8272000^2 = \mathbf{121} \ 141376^2 \\
& \mathbf{1232} \ 0858624^2 + 83472000^2 = \mathbf{12321} \ 141376^2 \\
& \mathbf{123432} \ 0858624^2 + 835472000^2 = \mathbf{1234321} \ 141376^2 \quad (5.376) \\
& \\
& 0857871^2 + 754000^2 = \mathbf{1} \ 142129^2 \\
& \mathbf{12} \ 0857871^2 + 8294000^2 = \mathbf{121} \ 142129^2 \\
& \mathbf{1232} \ 0857871^2 + 83694000^2 = \mathbf{12321} \ 142129^2 \\
& \mathbf{123432} \ 0857871^2 + 837694000^2 = \mathbf{1234321} \ 142129^2 \quad (5.377) \\
& \\
& 0857116^2 + 756000^2 = \mathbf{1} \ 142884^2 \\
& \mathbf{12} \ 0857116^2 + 8316000^2 = \mathbf{121} \ 142884^2 \\
& \mathbf{1232} \ 0857116^2 + 83916000^2 = \mathbf{12321} \ 142884^2 \\
& \mathbf{123432} \ 0857116^2 + 839916000^2 = \mathbf{1234321} \ 142884^2 \quad (5.378) \\
& \\
& 0856359^2 + 758000^2 = \mathbf{1} \ 143641^2 \\
& \mathbf{12} \ 0856359^2 + 8338000^2 = \mathbf{121} \ 143641^2 \\
& \mathbf{1232} \ 0856359^2 + 84138000^2 = \mathbf{12321} \ 143641^2 \\
& \mathbf{123432} \ 0856359^2 + 842138000^2 = \mathbf{1234321} \ 143641^2 \quad (5.379) \\
& \\
& 0855600^2 + 760000^2 = \mathbf{1} \ 144400^2 \\
& \mathbf{12} \ 0855600^2 + 8360000^2 = \mathbf{121} \ 144400^2 \\
& \mathbf{1232} \ 0855600^2 + 84360000^2 = \mathbf{12321} \ 144400^2 \\
& \mathbf{123432} \ 0855600^2 + 844360000^2 = \mathbf{1234321} \ 144400^2 \quad (5.380) \\
& \\
& 0854839^2 + 762000^2 = \mathbf{1} \ 145161^2 \\
& \mathbf{12} \ 0854839^2 + 8382000^2 = \mathbf{121} \ 145161^2 \\
& \mathbf{1232} \ 0854839^2 + 84582000^2 = \mathbf{12321} \ 145161^2 \\
& \mathbf{123432} \ 0854839^2 + 846582000^2 = \mathbf{1234321} \ 145161^2 \quad (5.381)
\end{aligned}$$

$0854076^2 + 764000^2 = \textcolor{red}{1} \textcolor{blue}{145924}^2$	$0847119^2 + 782000^2 = \textcolor{red}{1} \textcolor{blue}{152881}^2$
$12 \cdot 0854076^2 + 8404000^2 = \textcolor{red}{121} \textcolor{blue}{145924}^2$	$12 \cdot 0847119^2 + 8602000^2 = \textcolor{red}{121} \textcolor{blue}{152881}^2$
$1232 \cdot 0854076^2 + 84804000^2 = \textcolor{red}{12321} \textcolor{blue}{145924}^2$	$1232 \cdot 0847119^2 + 86802000^2 = \textcolor{red}{12321} \textcolor{blue}{152881}^2$
$123432 \cdot 0854076^2 + 848804000^2 = \textcolor{red}{1234321} \textcolor{blue}{145924}^2 \quad (5.382)$	$123432 \cdot 0847119^2 + 868802000^2 = \textcolor{red}{1234321} \textcolor{blue}{152881}^2 \quad (5.391)$
$0853311^2 + 766000^2 = \textcolor{red}{1} \textcolor{blue}{146689}^2$	$0846336^2 + 784000^2 = \textcolor{red}{1} \textcolor{blue}{153664}^2$
$12 \cdot 0853311^2 + 8426000^2 = \textcolor{red}{121} \textcolor{blue}{146689}^2$	$12 \cdot 0846336^2 + 8624000^2 = \textcolor{red}{121} \textcolor{blue}{153664}^2$
$1232 \cdot 0853311^2 + 85026000^2 = \textcolor{red}{12321} \textcolor{blue}{146689}^2$	$1232 \cdot 0846336^2 + 87024000^2 = \textcolor{red}{12321} \textcolor{blue}{153664}^2$
$123432 \cdot 0853311^2 + 851026000^2 = \textcolor{red}{1234321} \textcolor{blue}{146689}^2 \quad (5.383)$	$123432 \cdot 0846336^2 + 871024000^2 = \textcolor{red}{1234321} \textcolor{blue}{153664}^2 \quad (5.392)$
$0852544^2 + 768000^2 = \textcolor{red}{1} \textcolor{blue}{147456}^2$	$0845551^2 + 786000^2 = \textcolor{red}{1} \textcolor{blue}{154449}^2$
$12 \cdot 0852544^2 + 8448000^2 = \textcolor{red}{121} \textcolor{blue}{147456}^2$	$12 \cdot 0845551^2 + 8646000^2 = \textcolor{red}{121} \textcolor{blue}{154449}^2$
$1232 \cdot 0852544^2 + 85248000^2 = \textcolor{red}{12321} \textcolor{blue}{147456}^2$	$1232 \cdot 0845551^2 + 87246000^2 = \textcolor{red}{12321} \textcolor{blue}{154449}^2$
$123432 \cdot 0852544^2 + 853248000^2 = \textcolor{red}{1234321} \textcolor{blue}{147456}^2 \quad (5.384)$	$123432 \cdot 0845551^2 + 873246000^2 = \textcolor{red}{1234321} \textcolor{blue}{154449}^2 \quad (5.393)$
$0851775^2 + 770000^2 = \textcolor{red}{1} \textcolor{blue}{148225}^2$	$0844764^2 + 788000^2 = \textcolor{red}{1} \textcolor{blue}{155236}^2$
$12 \cdot 0851775^2 + 8470000^2 = \textcolor{red}{121} \textcolor{blue}{148225}^2$	$12 \cdot 0844764^2 + 8668000^2 = \textcolor{red}{121} \textcolor{blue}{155236}^2$
$1232 \cdot 0851775^2 + 85470000^2 = \textcolor{red}{12321} \textcolor{blue}{148225}^2$	$1232 \cdot 0844764^2 + 87468000^2 = \textcolor{red}{12321} \textcolor{blue}{155236}^2$
$123432 \cdot 0851775^2 + 855470000^2 = \textcolor{red}{1234321} \textcolor{blue}{148225}^2 \quad (5.385)$	$123432 \cdot 0844764^2 + 875468000^2 = \textcolor{red}{1234321} \textcolor{blue}{155236}^2 \quad (5.394)$
$0851004^2 + 772000^2 = \textcolor{red}{1} \textcolor{blue}{148996}^2$	$0843975^2 + 790000^2 = \textcolor{red}{1} \textcolor{blue}{156025}^2$
$12 \cdot 0851004^2 + 8492000^2 = \textcolor{red}{121} \textcolor{blue}{148996}^2$	$12 \cdot 0843975^2 + 8690000^2 = \textcolor{red}{121} \textcolor{blue}{156025}^2$
$1232 \cdot 0851004^2 + 85692000^2 = \textcolor{red}{12321} \textcolor{blue}{148996}^2$	$1232 \cdot 0843975^2 + 87690000^2 = \textcolor{red}{12321} \textcolor{blue}{156025}^2$
$123432 \cdot 0851004^2 + 857692000^2 = \textcolor{red}{1234321} \textcolor{blue}{148996}^2 \quad (5.386)$	$123432 \cdot 0843975^2 + 877690000^2 = \textcolor{red}{1234321} \textcolor{blue}{156025}^2 \quad (5.395)$
$0850231^2 + 774000^2 = \textcolor{red}{1} \textcolor{blue}{149769}^2$	$0843184^2 + 792000^2 = \textcolor{red}{1} \textcolor{blue}{156816}^2$
$12 \cdot 0850231^2 + 8514000^2 = \textcolor{red}{121} \textcolor{blue}{149769}^2$	$12 \cdot 0843184^2 + 8712000^2 = \textcolor{red}{121} \textcolor{blue}{156816}^2$
$1232 \cdot 0850231^2 + 85914000^2 = \textcolor{red}{12321} \textcolor{blue}{149769}^2$	$1232 \cdot 0843184^2 + 87912000^2 = \textcolor{red}{12321} \textcolor{blue}{156816}^2$
$123432 \cdot 0850231^2 + 859914000^2 = \textcolor{red}{1234321} \textcolor{blue}{149769}^2 \quad (5.387)$	$123432 \cdot 0843184^2 + 879912000^2 = \textcolor{red}{1234321} \textcolor{blue}{156816}^2 \quad (5.396)$
$0849456^2 + 776000^2 = \textcolor{red}{1} \textcolor{blue}{150544}^2$	$0842391^2 + 794000^2 = \textcolor{red}{1} \textcolor{blue}{157609}^2$
$12 \cdot 0849456^2 + 8536000^2 = \textcolor{red}{121} \textcolor{blue}{150544}^2$	$12 \cdot 0842391^2 + 8734000^2 = \textcolor{red}{121} \textcolor{blue}{157609}^2$
$1232 \cdot 0849456^2 + 86136000^2 = \textcolor{red}{12321} \textcolor{blue}{150544}^2$	$1232 \cdot 0842391^2 + 88134000^2 = \textcolor{red}{12321} \textcolor{blue}{157609}^2$
$123432 \cdot 0849456^2 + 862136000^2 = \textcolor{red}{1234321} \textcolor{blue}{150544}^2 \quad (5.388)$	$123432 \cdot 0842391^2 + 882134000^2 = \textcolor{red}{1234321} \textcolor{blue}{157609}^2 \quad (5.397)$
$0848679^2 + 778000^2 = \textcolor{red}{1} \textcolor{blue}{151321}^2$	$0841596^2 + 796000^2 = \textcolor{red}{1} \textcolor{blue}{158404}^2$
$12 \cdot 0848679^2 + 8558000^2 = \textcolor{red}{121} \textcolor{blue}{151321}^2$	$12 \cdot 0841596^2 + 8756000^2 = \textcolor{red}{121} \textcolor{blue}{158404}^2$
$1232 \cdot 0848679^2 + 86358000^2 = \textcolor{red}{12321} \textcolor{blue}{151321}^2$	$1232 \cdot 0841596^2 + 88356000^2 = \textcolor{red}{12321} \textcolor{blue}{158404}^2$
$123432 \cdot 0848679^2 + 864358000^2 = \textcolor{red}{1234321} \textcolor{blue}{151321}^2 \quad (5.389)$	$123432 \cdot 0841596^2 + 884356000^2 = \textcolor{red}{1234321} \textcolor{blue}{158404}^2 \quad (5.398)$
$0847900^2 + 780000^2 = \textcolor{red}{1} \textcolor{blue}{152100}^2$	$0840799^2 + 798000^2 = \textcolor{red}{1} \textcolor{blue}{159201}^2$
$12 \cdot 0847900^2 + 8580000^2 = \textcolor{red}{121} \textcolor{blue}{152100}^2$	$12 \cdot 0840799^2 + 8778000^2 = \textcolor{red}{121} \textcolor{blue}{159201}^2$
$1232 \cdot 0847900^2 + 86580000^2 = \textcolor{red}{12321} \textcolor{blue}{152100}^2$	$1232 \cdot 0840799^2 + 88578000^2 = \textcolor{red}{12321} \textcolor{blue}{159201}^2$
$123432 \cdot 0847900^2 + 866580000^2 = \textcolor{red}{1234321} \textcolor{blue}{152100}^2 \quad (5.390)$	$123432 \cdot 0840799^2 + 886578000^2 = \textcolor{red}{1234321} \textcolor{blue}{159201}^2 \quad (5.399)$

5.5 For $n = 400, 401, 401, \dots, 497, 498, 499$:

Let's consider

$$m = 1000, 11000, 111000, 1111000, 11111000, 111111000, 1111111000, 11111111000$$

in (1.1), then for each value of $n = 400, 401, 401, \dots, 497, 498, 499$; there are 100 *palindromic-type pandigital Pythagorean patterns* given below. In each case, only first four values are written. The other 5 values can be written on similar lines as done in subsection 5.1.1.

$0840000^2 + 800000^2 = 1160000^2$	$0834351^2 + 814000^2 = 1165649^2$
$120840000^2 + 8800000^2 = 121160000^2$	$120834351^2 + 8954000^2 = 121165649^2$
$12320840000^2 + 88800000^2 = 12321160000^2$	$12320834351^2 + 90354000^2 = 12321165649^2$
$1234320840000^2 + 888800000^2 = 1234321160000^2 \quad (5.400)$	$1234320834351^2 + 904354000^2 = 1234321165649^2 \quad (5.407)$
$0839199^2 + 802000^2 = 1160801^2$	$0833536^2 + 816000^2 = 1166464^2$
$120839199^2 + 8822000^2 = 121160801^2$	$120833536^2 + 8976000^2 = 121166464^2$
$12320839199^2 + 89022000^2 = 12321160801^2$	$12320833536^2 + 90576000^2 = 12321166464^2$
$1234320839199^2 + 891022000^2 = 1234321160801^2 \quad (5.401)$	$1234320833536^2 + 906576000^2 = 1234321166464^2 \quad (5.408)$
$0838396^2 + 804000^2 = 1161604^2$	$0832719^2 + 818000^2 = 1167281^2$
$120838396^2 + 8844000^2 = 121161604^2$	$120832719^2 + 8998000^2 = 121167281^2$
$12320838396^2 + 89244000^2 = 12321161604^2$	$12320832719^2 + 90798000^2 = 12321167281^2$
$1234320838396^2 + 893244000^2 = 1234321161604^2 \quad (5.402)$	$1234320832719^2 + 908798000^2 = 1234321167281^2 \quad (5.409)$
$0837591^2 + 806000^2 = 1162409^2$	$0831900^2 + 820000^2 = 1168100^2$
$120837591^2 + 8866000^2 = 121162409^2$	$120831900^2 + 9020000^2 = 121168100^2$
$12320837591^2 + 89466000^2 = 12321162409^2$	$12320831900^2 + 91020000^2 = 12321168100^2$
$1234320837591^2 + 895466000^2 = 1234321162409^2 \quad (5.403)$	$1234320831900^2 + 911020000^2 = 1234321168100^2 \quad (5.410)$
$0836784^2 + 808000^2 = 1163216^2$	$0831079^2 + 822000^2 = 1168921^2$
$120836784^2 + 8888000^2 = 121163216^2$	$120831079^2 + 9042000^2 = 121168921^2$
$12320836784^2 + 89688000^2 = 12321163216^2$	$12320831079^2 + 91242000^2 = 12321168921^2$
$1234320836784^2 + 897688000^2 = 1234321163216^2 \quad (5.404)$	$1234320831079^2 + 913242000^2 = 1234321168921^2 \quad (5.411)$
$0835975^2 + 810000^2 = 1164025^2$	$0830256^2 + 824000^2 = 1169744^2$
$120835975^2 + 8910000^2 = 121164025^2$	$120830256^2 + 9064000^2 = 121169744^2$
$12320835975^2 + 89910000^2 = 12321164025^2$	$12320830256^2 + 91464000^2 = 12321169744^2$
$1234320835975^2 + 899910000^2 = 1234321164025^2 \quad (5.405)$	$1234320830256^2 + 915464000^2 = 1234321169744^2 \quad (5.412)$
$0835164^2 + 812000^2 = 1164836^2$	$0829431^2 + 826000^2 = 1170569^2$
$120835164^2 + 8932000^2 = 121164836^2$	$120829431^2 + 9086000^2 = 121170569^2$
$12320835164^2 + 90132000^2 = 12321164836^2$	$12320829431^2 + 91686000^2 = 12321170569^2$
$1234320835164^2 + 902132000^2 = 1234321164836^2 \quad (5.406)$	$1234320829431^2 + 917686000^2 = 1234321170569^2 \quad (5.413)$

$$\begin{aligned}
& 0828604^2 + 828000^2 = \mathbf{1} 171396^2 \\
& \mathbf{12} 0828604^2 + 9108000^2 = \mathbf{121} 171396^2 \\
& \mathbf{1232} 0828604^2 + 91908000^2 = \mathbf{12321} 171396^2 \\
& \mathbf{123432} 0828604^2 + 919908000^2 = \mathbf{1234321} 171396^2 \quad (5.414)
\end{aligned}$$

$$\begin{aligned}
& 0827775^2 + 830000^2 = \mathbf{1} 172225^2 \\
& \mathbf{12} 0827775^2 + 9130000^2 = \mathbf{121} 172225^2 \\
& \mathbf{1232} 0827775^2 + 92130000^2 = \mathbf{12321} 172225^2 \\
& \mathbf{123432} 0827775^2 + 922130000^2 = \mathbf{1234321} 172225^2 \quad (5.415)
\end{aligned}$$

$$\begin{aligned}
& 0826944^2 + 832000^2 = \mathbf{1} 173056^2 \\
& \mathbf{12} 0826944^2 + 9152000^2 = \mathbf{121} 173056^2 \\
& \mathbf{1232} 0826944^2 + 92352000^2 = \mathbf{12321} 173056^2 \\
& \mathbf{123432} 0826944^2 + 924352000^2 = \mathbf{1234321} 173056^2 \quad (5.416)
\end{aligned}$$

$$\begin{aligned}
& 0826111^2 + 834000^2 = \mathbf{1} 173889^2 \\
& \mathbf{12} 0826111^2 + 9174000^2 = \mathbf{121} 173889^2 \\
& \mathbf{1232} 0826111^2 + 92574000^2 = \mathbf{12321} 173889^2 \\
& \mathbf{123432} 0826111^2 + 926574000^2 = \mathbf{1234321} 173889^2 \quad (5.417)
\end{aligned}$$

$$\begin{aligned}
& 0825276^2 + 836000^2 = \mathbf{1} 174724^2 \\
& \mathbf{12} 0825276^2 + 9196000^2 = \mathbf{121} 174724^2 \\
& \mathbf{1232} 0825276^2 + 92796000^2 = \mathbf{12321} 174724^2 \\
& \mathbf{123432} 0825276^2 + 928796000^2 = \mathbf{1234321} 174724^2 \quad (5.418)
\end{aligned}$$

$$\begin{aligned}
& 0824439^2 + 838000^2 = \mathbf{1} 175561^2 \\
& \mathbf{12} 0824439^2 + 9218000^2 = \mathbf{121} 175561^2 \\
& \mathbf{1232} 0824439^2 + 93018000^2 = \mathbf{12321} 175561^2 \\
& \mathbf{123432} 0824439^2 + 931018000^2 = \mathbf{1234321} 175561^2 \quad (5.419)
\end{aligned}$$

$$\begin{aligned}
& 0823600^2 + 840000^2 = \mathbf{1} 176400^2 \\
& \mathbf{12} 0823600^2 + 9240000^2 = \mathbf{121} 176400^2 \\
& \mathbf{1232} 0823600^2 + 93240000^2 = \mathbf{12321} 176400^2 \\
& \mathbf{123432} 0823600^2 + 933240000^2 = \mathbf{1234321} 176400^2 \quad (5.420)
\end{aligned}$$

$$\begin{aligned}
& 0822759^2 + 842000^2 = \mathbf{1} 177241^2 \\
& \mathbf{12} 0822759^2 + 9262000^2 = \mathbf{121} 177241^2 \\
& \mathbf{1232} 0822759^2 + 93462000^2 = \mathbf{12321} 177241^2 \\
& \mathbf{123432} 0822759^2 + 935462000^2 = \mathbf{1234321} 177241^2 \quad (5.421)
\end{aligned}$$

$$\begin{aligned}
& 0821916^2 + 844000^2 = \mathbf{1} 178084^2 \\
& \mathbf{12} 0821916^2 + 9284000^2 = \mathbf{121} 178084^2 \\
& \mathbf{1232} 0821916^2 + 93684000^2 = \mathbf{12321} 178084^2 \\
& \mathbf{123432} 0821916^2 + 937684000^2 = \mathbf{1234321} 178084^2 \quad (5.422)
\end{aligned}$$

$$\begin{aligned}
& 0821071^2 + 846000^2 = \mathbf{1} 178929^2 \\
& \mathbf{12} 0821071^2 + 9306000^2 = \mathbf{121} 178929^2 \\
& \mathbf{1232} 0821071^2 + 93906000^2 = \mathbf{12321} 178929^2 \\
& \mathbf{123432} 0821071^2 + 939906000^2 = \mathbf{1234321} 178929^2 \quad (5.423)
\end{aligned}$$

$$\begin{aligned}
& 0820224^2 + 848000^2 = \mathbf{1} 179776^2 \\
& \mathbf{12} 0820224^2 + 9328000^2 = \mathbf{121} 179776^2 \\
& \mathbf{1232} 0820224^2 + 94128000^2 = \mathbf{12321} 179776^2 \\
& \mathbf{123432} 0820224^2 + 942128000^2 = \mathbf{1234321} 179776^2 \quad (5.424)
\end{aligned}$$

$$\begin{aligned}
& 0819375^2 + 850000^2 = \mathbf{1} 180625^2 \\
& \mathbf{12} 0819375^2 + 9350000^2 = \mathbf{121} 180625^2 \\
& \mathbf{1232} 0819375^2 + 94350000^2 = \mathbf{12321} 180625^2 \\
& \mathbf{123432} 0819375^2 + 944350000^2 = \mathbf{1234321} 180625^2 \quad (5.425)
\end{aligned}$$

$$\begin{aligned}
& 0818524^2 + 852000^2 = \mathbf{1} 181476^2 \\
& \mathbf{12} 0818524^2 + 9372000^2 = \mathbf{121} 181476^2 \\
& \mathbf{1232} 0818524^2 + 94572000^2 = \mathbf{12321} 181476^2 \\
& \mathbf{123432} 0818524^2 + 946572000^2 = \mathbf{1234321} 181476^2 \quad (5.426)
\end{aligned}$$

$$\begin{aligned}
& 0817671^2 + 854000^2 = \mathbf{1} 182329^2 \\
& \mathbf{12} 0817671^2 + 9394000^2 = \mathbf{121} 182329^2 \\
& \mathbf{1232} 0817671^2 + 94794000^2 = \mathbf{12321} 182329^2 \\
& \mathbf{123432} 0817671^2 + 948794000^2 = \mathbf{1234321} 182329^2 \quad (5.427)
\end{aligned}$$

$$\begin{aligned}
& 0816816^2 + 856000^2 = \mathbf{1} 183184^2 \\
& \mathbf{12} 0816816^2 + 9416000^2 = \mathbf{121} 183184^2 \\
& \mathbf{1232} 0816816^2 + 95016000^2 = \mathbf{12321} 183184^2 \\
& \mathbf{123432} 0816816^2 + 951016000^2 = \mathbf{1234321} 183184^2 \quad (5.428)
\end{aligned}$$

$$\begin{aligned}
& 0815959^2 + 858000^2 = \mathbf{1} 184041^2 \\
& \mathbf{12} 0815959^2 + 9438000^2 = \mathbf{121} 184041^2 \\
& \mathbf{1232} 0815959^2 + 95238000^2 = \mathbf{12321} 184041^2 \\
& \mathbf{123432} 0815959^2 + 953238000^2 = \mathbf{1234321} 184041^2 \quad (5.429)
\end{aligned}$$

$$\begin{aligned}
& 0815100^2 + 860000^2 = \mathbf{1} 184900^2 \\
& \mathbf{12} 0815100^2 + 9460000^2 = \mathbf{121} 184900^2 \\
& \mathbf{1232} 0815100^2 + 95460000^2 = \mathbf{12321} 184900^2 \\
& \mathbf{123432} 0815100^2 + 955460000^2 = \mathbf{1234321} 184900^2 \quad (5.430)
\end{aligned}$$

$$\begin{aligned}
& 0814239^2 + 862000^2 = \mathbf{1} 185761^2 \\
& \mathbf{12} 0814239^2 + 9482000^2 = \mathbf{121} 185761^2 \\
& \mathbf{1232} 0814239^2 + 95682000^2 = \mathbf{12321} 185761^2 \\
& \mathbf{123432} 0814239^2 + 957682000^2 = \mathbf{1234321} 185761^2 \quad (5.431)
\end{aligned}$$

$$\begin{aligned}
& 0813376^2 + 864000^2 = \mathbf{1} 186624^2 \\
& \mathbf{12} 0813376^2 + 9504000^2 = \mathbf{121} 186624^2 \\
& \mathbf{1232} 0813376^2 + 95904000^2 = \mathbf{12321} 186624^2 \\
& \mathbf{123432} 0813376^2 + 959904000^2 = \mathbf{1234321} 186624^2 \quad (5.432)
\end{aligned}$$

$$\begin{aligned}
& 0812511^2 + 866000^2 = \mathbf{1} 187489^2 \\
& \mathbf{12} 0812511^2 + 9526000^2 = \mathbf{121} 187489^2 \\
& \mathbf{1232} 0812511^2 + 96126000^2 = \mathbf{12321} 187489^2 \\
& \mathbf{123432} 0812511^2 + 962126000^2 = \mathbf{1234321} 187489^2 \quad (5.433)
\end{aligned}$$

$$\begin{aligned}
& 0811644^2 + 868000^2 = \mathbf{1} 188356^2 \\
& \mathbf{12} 0811644^2 + 9548000^2 = \mathbf{121} 188356^2 \\
& \mathbf{1232} 0811644^2 + 96348000^2 = \mathbf{12321} 188356^2 \\
& \mathbf{123432} 0811644^2 + 964348000^2 = \mathbf{1234321} 188356^2 \quad (5.434)
\end{aligned}$$

$$\begin{aligned}
& 0810775^2 + 870000^2 = \mathbf{1} 189225^2 \\
& \mathbf{12} 0810775^2 + 9570000^2 = \mathbf{121} 189225^2 \\
& \mathbf{1232} 0810775^2 + 96570000^2 = \mathbf{12321} 189225^2 \\
& \mathbf{123432} 0810775^2 + 966570000^2 = \mathbf{1234321} 189225^2 \quad (5.435)
\end{aligned}$$

$$\begin{aligned}
& 0809904^2 + 872000^2 = \mathbf{1} 190096^2 \\
& \mathbf{12} 0809904^2 + 9592000^2 = \mathbf{121} 190096^2 \\
& \mathbf{1232} 0809904^2 + 96792000^2 = \mathbf{12321} 190096^2 \\
& \mathbf{123432} 0809904^2 + 968792000^2 = \mathbf{1234321} 190096^2 \quad (5.436)
\end{aligned}$$

$$\begin{aligned}
& 0809031^2 + 874000^2 = \mathbf{1} 190969^2 \\
& \mathbf{12} 0809031^2 + 9614000^2 = \mathbf{121} 190969^2 \\
& \mathbf{1232} 0809031^2 + 97014000^2 = \mathbf{12321} 190969^2 \\
& \mathbf{123432} 0809031^2 + 971014000^2 = \mathbf{1234321} 190969^2 \quad (5.437)
\end{aligned}$$

$$\begin{aligned}
& 0808156^2 + 876000^2 = \mathbf{1} 191844^2 \\
& \mathbf{12} 0808156^2 + 9636000^2 = \mathbf{121} 191844^2 \\
& \mathbf{1232} 0808156^2 + 97236000^2 = \mathbf{12321} 191844^2 \\
& \mathbf{123432} 0808156^2 + 973236000^2 = \mathbf{1234321} 191844^2 \quad (5.438)
\end{aligned}$$

$$\begin{aligned}
& 0807279^2 + 878000^2 = \mathbf{1} 192721^2 \\
& \mathbf{12} 0807279^2 + 9658000^2 = \mathbf{121} 192721^2 \\
& \mathbf{1232} 0807279^2 + 97458000^2 = \mathbf{12321} 192721^2 \\
& \mathbf{123432} 0807279^2 + 975458000^2 = \mathbf{1234321} 192721^2 \quad (5.439)
\end{aligned}$$

$$\begin{aligned}
& 0806400^2 + 880000^2 = \mathbf{1} 193600^2 \\
& \mathbf{12} 0806400^2 + 9680000^2 = \mathbf{121} 193600^2 \\
& \mathbf{1232} 0806400^2 + 97680000^2 = \mathbf{12321} 193600^2 \\
& \mathbf{123432} 0806400^2 + 977680000^2 = \mathbf{1234321} 193600^2 \quad (5.440)
\end{aligned}$$

$$\begin{aligned}
& 0805519^2 + 882000^2 = \mathbf{1} 194481^2 \\
& \mathbf{12} 0805519^2 + 9702000^2 = \mathbf{121} 194481^2 \\
& \mathbf{1232} 0805519^2 + 97902000^2 = \mathbf{12321} 194481^2 \\
& \mathbf{123432} 0805519^2 + 979902000^2 = \mathbf{1234321} 194481^2 \quad (5.441)
\end{aligned}$$

$$\begin{aligned}
& 0804636^2 + 884000^2 = \mathbf{1} 195364^2 \\
& \mathbf{12} 0804636^2 + 9724000^2 = \mathbf{121} 195364^2 \\
& \mathbf{1232} 0804636^2 + 98124000^2 = \mathbf{12321} 195364^2 \\
& \mathbf{123432} 0804636^2 + 982124000^2 = \mathbf{1234321} 195364^2 \quad (5.442)
\end{aligned}$$

$$\begin{aligned}
& 0803751^2 + 886000^2 = \mathbf{1} 196249^2 \\
& \mathbf{12} 0803751^2 + 9746000^2 = \mathbf{121} 196249^2 \\
& \mathbf{1232} 0803751^2 + 98346000^2 = \mathbf{12321} 196249^2 \\
& \mathbf{123432} 0803751^2 + 984346000^2 = \mathbf{1234321} 196249^2 \quad (5.443)
\end{aligned}$$

$$\begin{aligned}
& 0802864^2 + 888000^2 = \mathbf{1} 197136^2 \\
& \mathbf{12} 0802864^2 + 9768000^2 = \mathbf{121} 197136^2 \\
& \mathbf{1232} 0802864^2 + 98568000^2 = \mathbf{12321} 197136^2 \\
& \mathbf{123432} 0802864^2 + 986568000^2 = \mathbf{1234321} 197136^2 \quad (5.444)
\end{aligned}$$

$$\begin{aligned}
& 0801975^2 + 890000^2 = \mathbf{1} 198025^2 \\
& \mathbf{12} 0801975^2 + 9790000^2 = \mathbf{121} 198025^2 \\
& \mathbf{1232} 0801975^2 + 98790000^2 = \mathbf{12321} 198025^2 \\
& \mathbf{123432} 0801975^2 + 988790000^2 = \mathbf{1234321} 198025^2 \quad (5.445)
\end{aligned}$$

$$\begin{aligned}
& 0801084^2 + 892000^2 = \mathbf{1} 198916^2 \\
& \mathbf{12} 0801084^2 + 9812000^2 = \mathbf{121} 198916^2 \\
& \mathbf{1232} 0801084^2 + 99012000^2 = \mathbf{12321} 198916^2 \\
& \mathbf{123432} 0801084^2 + 991012000^2 = \mathbf{1234321} 198916^2 \quad (5.446)
\end{aligned}$$

$$\begin{aligned}
& 0800191^2 + 894000^2 = \mathbf{1} 199809^2 \\
& \mathbf{12} 0800191^2 + 9834000^2 = \mathbf{121} 199809^2 \\
& \mathbf{1232} 0800191^2 + 99234000^2 = \mathbf{12321} 199809^2 \\
& \mathbf{123432} 0800191^2 + 993234000^2 = \mathbf{1234321} 199809^2 \quad (5.447)
\end{aligned}$$

$$\begin{aligned}
& 0799296^2 + 896000^2 = \mathbf{1} 200704^2 \\
& \mathbf{12} 0799296^2 + 9856000^2 = \mathbf{121} 200704^2 \\
& \mathbf{1232} 0799296^2 + 99456000^2 = \mathbf{12321} 200704^2 \\
& \mathbf{123432} 0799296^2 + 995456000^2 = \mathbf{1234321} 200704^2 \quad (5.448) \\
& \\
& 0798399^2 + 898000^2 = \mathbf{1} 201601^2 \\
& \mathbf{12} 0798399^2 + 9878000^2 = \mathbf{121} 201601^2 \\
& \mathbf{1232} 0798399^2 + 99678000^2 = \mathbf{12321} 201601^2 \\
& \mathbf{123432} 0798399^2 + 997678000^2 = \mathbf{1234321} 201601^2 \quad (5.449) \\
& \\
& 0797500^2 + 900000^2 = \mathbf{1} 202500^2 \\
& \mathbf{12} 0797500^2 + 9900000^2 = \mathbf{121} 202500^2 \\
& \mathbf{1232} 0797500^2 + 99900000^2 = \mathbf{12321} 202500^2 \\
& \mathbf{123432} 0797500^2 + 999900000^2 = \mathbf{1234321} 202500^2 \quad (5.450) \\
& \\
& 0796599^2 + 902000^2 = \mathbf{1} 203401^2 \\
& \mathbf{12} 0796599^2 + 9922000^2 = \mathbf{121} 203401^2 \\
& \mathbf{1232} 0796599^2 + 100122000^2 = \mathbf{12321} 203401^2 \\
& \mathbf{123432} 0796599^2 + 1002122000^2 = \mathbf{1234321} 203401^2 \quad (5.451) \\
& \\
& 0795696^2 + 904000^2 = \mathbf{1} 204304^2 \\
& \mathbf{12} 0795696^2 + 9944000^2 = \mathbf{121} 204304^2 \\
& \mathbf{1232} 0795696^2 + 100344000^2 = \mathbf{12321} 204304^2 \\
& \mathbf{123432} 0795696^2 + 1004344000^2 = \mathbf{1234321} 204304^2 \quad (5.452) \\
& \\
& 0794791^2 + 906000^2 = \mathbf{1} 205209^2 \\
& \mathbf{12} 0794791^2 + 9966000^2 = \mathbf{121} 205209^2 \\
& \mathbf{1232} 0794791^2 + 100566000^2 = \mathbf{12321} 205209^2 \\
& \mathbf{123432} 0794791^2 + 1006566000^2 = \mathbf{1234321} 205209^2 \quad (5.453) \\
& \\
& 0793884^2 + 908000^2 = \mathbf{1} 206116^2 \\
& \mathbf{12} 0793884^2 + 9988000^2 = \mathbf{121} 206116^2 \\
& \mathbf{1232} 0793884^2 + 100788000^2 = \mathbf{12321} 206116^2 \\
& \mathbf{123432} 0793884^2 + 1008788000^2 = \mathbf{1234321} 206116^2 \quad (5.454) \\
& \\
& 0792975^2 + 910000^2 = \mathbf{1} 207025^2 \\
& \mathbf{12} 0792975^2 + 10010000^2 = \mathbf{121} 207025^2 \\
& \mathbf{1232} 0792975^2 + 101010000^2 = \mathbf{12321} 207025^2 \\
& \mathbf{123432} 0792975^2 + 1011010000^2 = \mathbf{1234321} 207025^2 \quad (5.455) \\
& \\
& 0792064^2 + 912000^2 = \mathbf{1} 207936^2 \\
& \mathbf{12} 0792064^2 + 10032000^2 = \mathbf{121} 207936^2 \\
& \mathbf{1232} 0792064^2 + 101232000^2 = \mathbf{12321} 207936^2 \\
& \mathbf{123432} 0792064^2 + 1013232000^2 = \mathbf{1234321} 207936^2 \quad (5.456)
\end{aligned}$$

$0791151^2 + 914000^2 = \mathbf{1} 208849^2$
 $\mathbf{12} 0791151^2 + 10054000^2 = \mathbf{121} 208849^2$
 $\mathbf{1232} 0791151^2 + 101454000^2 = \mathbf{12321} 208849^2$
 $\mathbf{123432} 0791151^2 + 1015454000^2 = \mathbf{1234321} 208849^2 \quad (5.457)$

$0790236^2 + 916000^2 = \mathbf{1} 209764^2$
 $\mathbf{12} 0790236^2 + 10076000^2 = \mathbf{121} 209764^2$
 $\mathbf{1232} 0790236^2 + 101676000^2 = \mathbf{12321} 209764^2$
 $\mathbf{123432} 0790236^2 + 1017676000^2 = \mathbf{1234321} 209764^2 \quad (5.458)$

$0789319^2 + 918000^2 = \mathbf{1} 210681^2$
 $\mathbf{12} 0789319^2 + 10098000^2 = \mathbf{121} 210681^2$
 $\mathbf{1232} 0789319^2 + 101898000^2 = \mathbf{12321} 210681^2$
 $\mathbf{123432} 0789319^2 + 1019898000^2 = \mathbf{1234321} 210681^2 \quad (5.459)$

$0788400^2 + 920000^2 = \mathbf{1} 211600^2$
 $\mathbf{12} 0788400^2 + 10120000^2 = \mathbf{121} 211600^2$
 $\mathbf{1232} 0788400^2 + 102120000^2 = \mathbf{12321} 211600^2$
 $\mathbf{123432} 0788400^2 + 1022120000^2 = \mathbf{1234321} 211600^2 \quad (5.460)$

$0787479^2 + 922000^2 = \mathbf{1} 212521^2$
 $\mathbf{12} 0787479^2 + 10142000^2 = \mathbf{121} 212521^2$
 $\mathbf{1232} 0787479^2 + 102342000^2 = \mathbf{12321} 212521^2$
 $\mathbf{123432} 0787479^2 + 1024342000^2 = \mathbf{1234321} 212521^2 \quad (5.461)$

$0786556^2 + 924000^2 = \mathbf{1} 213444^2$
 $\mathbf{12} 0786556^2 + 10164000^2 = \mathbf{121} 213444^2$
 $\mathbf{1232} 0786556^2 + 102564000^2 = \mathbf{12321} 213444^2$
 $\mathbf{123432} 0786556^2 + 1026564000^2 = \mathbf{1234321} 213444^2 \quad (5.462)$

$0785631^2 + 926000^2 = \mathbf{1} 214369^2$
 $\mathbf{12} 0785631^2 + 10186000^2 = \mathbf{121} 214369^2$
 $\mathbf{1232} 0785631^2 + 102786000^2 = \mathbf{12321} 214369^2$
 $\mathbf{123432} 0785631^2 + 1028786000^2 = \mathbf{1234321} 214369^2 \quad (5.463)$

$0784704^2 + 928000^2 = \mathbf{1} 215296^2$
 $\mathbf{12} 0784704^2 + 10208000^2 = \mathbf{121} 215296^2$
 $\mathbf{1232} 0784704^2 + 103008000^2 = \mathbf{12321} 215296^2$
 $\mathbf{123432} 0784704^2 + 1031008000^2 = \mathbf{1234321} 215296^2 \quad (5.464)$

$$\begin{aligned}
& 0783775^2 + 930000^2 = \mathbf{1} 216225^2 \\
& \mathbf{12} 0783775^2 + 10230000^2 = \mathbf{121} 216225^2 \\
& \mathbf{1232} 0783775^2 + 103230000^2 = \mathbf{12321} 216225^2 \\
& \mathbf{123432} 0783775^2 + 1033230000^2 = \mathbf{1234321} 216225^2 \quad (5.465) \\
& \\
& 0782844^2 + 932000^2 = \mathbf{1} 217156^2 \\
& \mathbf{12} 0782844^2 + 10252000^2 = \mathbf{121} 217156^2 \\
& \mathbf{1232} 0782844^2 + 103452000^2 = \mathbf{12321} 217156^2 \\
& \mathbf{123432} 0782844^2 + 1035452000^2 = \mathbf{1234321} 217156^2 \quad (5.466) \\
& \\
& 0781911^2 + 934000^2 = \mathbf{1} 218089^2 \\
& \mathbf{12} 0781911^2 + 10274000^2 = \mathbf{121} 218089^2 \\
& \mathbf{1232} 0781911^2 + 103674000^2 = \mathbf{12321} 218089^2 \\
& \mathbf{123432} 0781911^2 + 1037674000^2 = \mathbf{1234321} 218089^2 \quad (5.467) \\
& \\
& 0780976^2 + 936000^2 = \mathbf{1} 219024^2 \\
& \mathbf{12} 0780976^2 + 10296000^2 = \mathbf{121} 219024^2 \\
& \mathbf{1232} 0780976^2 + 103896000^2 = \mathbf{12321} 219024^2 \\
& \mathbf{123432} 0780976^2 + 1039896000^2 = \mathbf{1234321} 219024^2 \quad (5.468) \\
& \\
& 0780039^2 + 938000^2 = \mathbf{1} 219961^2 \\
& \mathbf{12} 0780039^2 + 10318000^2 = \mathbf{121} 219961^2 \\
& \mathbf{1232} 0780039^2 + 104118000^2 = \mathbf{12321} 219961^2 \\
& \mathbf{123432} 0780039^2 + 1042118000^2 = \mathbf{1234321} 219961^2 \quad (5.469) \\
& \\
& 0779100^2 + 940000^2 = \mathbf{1} 220900^2 \\
& \mathbf{12} 0779100^2 + 10340000^2 = \mathbf{121} 220900^2 \\
& \mathbf{1232} 0779100^2 + 104340000^2 = \mathbf{12321} 220900^2 \\
& \mathbf{123432} 0779100^2 + 1044340000^2 = \mathbf{1234321} 220900^2 \quad (5.470) \\
& \\
& 0778159^2 + 942000^2 = \mathbf{1} 221841^2 \\
& \mathbf{12} 0778159^2 + 10362000^2 = \mathbf{121} 221841^2 \\
& \mathbf{1232} 0778159^2 + 104562000^2 = \mathbf{12321} 221841^2 \\
& \mathbf{123432} 0778159^2 + 1046562000^2 = \mathbf{1234321} 221841^2 \quad (5.471) \\
& \\
& 0777216^2 + 944000^2 = \mathbf{1} 222784^2 \\
& \mathbf{12} 0777216^2 + 10384000^2 = \mathbf{121} 222784^2 \\
& \mathbf{1232} 0777216^2 + 104784000^2 = \mathbf{12321} 222784^2 \\
& \mathbf{123432} 0777216^2 + 1048784000^2 = \mathbf{1234321} 222784^2 \quad (5.472) \\
& \\
& 0776271^2 + 946000^2 = \mathbf{1} 223729^2 \\
& \mathbf{12} 0776271^2 + 10406000^2 = \mathbf{121} 223729^2 \\
& \mathbf{1232} 0776271^2 + 105006000^2 = \mathbf{12321} 223729^2 \\
& \mathbf{123432} 0776271^2 + 1051006000^2 = \mathbf{1234321} 223729^2 \quad (5.473) \\
& \\
& 0775324^2 + 948000^2 = \mathbf{1} 224676^2 \\
& \mathbf{12} 0775324^2 + 10428000^2 = \mathbf{121} 224676^2 \\
& \mathbf{1232} 0775324^2 + 105228000^2 = \mathbf{12321} 224676^2 \\
& \mathbf{123432} 0775324^2 + 1053228000^2 = \mathbf{1234321} 224676^2 \quad (5.474) \\
& \\
& 0774375^2 + 950000^2 = \mathbf{1} 225625^2 \\
& \mathbf{12} 0774375^2 + 10450000^2 = \mathbf{121} 225625^2 \\
& \mathbf{1232} 0774375^2 + 105450000^2 = \mathbf{12321} 225625^2 \\
& \mathbf{123432} 0774375^2 + 1055450000^2 = \mathbf{1234321} 225625^2 \quad (5.475) \\
& \\
& 0773424^2 + 952000^2 = \mathbf{1} 226576^2 \\
& \mathbf{12} 0773424^2 + 10472000^2 = \mathbf{121} 226576^2 \\
& \mathbf{1232} 0773424^2 + 105672000^2 = \mathbf{12321} 226576^2 \\
& \mathbf{123432} 0773424^2 + 1057672000^2 = \mathbf{1234321} 226576^2 \quad (5.476) \\
& \\
& 0772471^2 + 954000^2 = \mathbf{1} 227529^2 \\
& \mathbf{12} 0772471^2 + 10494000^2 = \mathbf{121} 227529^2 \\
& \mathbf{1232} 0772471^2 + 105894000^2 = \mathbf{12321} 227529^2 \\
& \mathbf{123432} 0772471^2 + 1059894000^2 = \mathbf{1234321} 227529^2 \quad (5.477) \\
& \\
& 0771516^2 + 956000^2 = \mathbf{1} 228484^2 \\
& \mathbf{12} 0771516^2 + 10516000^2 = \mathbf{121} 228484^2 \\
& \mathbf{1232} 0771516^2 + 106116000^2 = \mathbf{12321} 228484^2 \\
& \mathbf{123432} 0771516^2 + 1062116000^2 = \mathbf{1234321} 228484^2 \quad (5.478) \\
& \\
& 0770559^2 + 958000^2 = \mathbf{1} 229441^2 \\
& \mathbf{12} 0770559^2 + 10538000^2 = \mathbf{121} 229441^2 \\
& \mathbf{1232} 0770559^2 + 106338000^2 = \mathbf{12321} 229441^2 \\
& \mathbf{123432} 0770559^2 + 1064338000^2 = \mathbf{1234321} 229441^2 \quad (5.479) \\
& \\
& 0769600^2 + 960000^2 = \mathbf{1} 230400^2 \\
& \mathbf{12} 0769600^2 + 10560000^2 = \mathbf{121} 230400^2 \\
& \mathbf{1232} 0769600^2 + 106560000^2 = \mathbf{12321} 230400^2 \\
& \mathbf{123432} 0769600^2 + 1066560000^2 = \mathbf{1234321} 230400^2 \quad (5.480) \\
& \\
& 0768639^2 + 962000^2 = \mathbf{1} 231361^2 \\
& \mathbf{12} 0768639^2 + 10582000^2 = \mathbf{121} 231361^2 \\
& \mathbf{1232} 0768639^2 + 106782000^2 = \mathbf{12321} 231361^2 \\
& \mathbf{123432} 0768639^2 + 1068782000^2 = \mathbf{1234321} 231361^2 \quad (5.481)
\end{aligned}$$

$0767676^2 + 964000^2 = \textcolor{red}{1} \textcolor{blue}{2}32324^2$	$0758919^2 + 982000^2 = \textcolor{red}{1} \textcolor{blue}{2}41081^2$
$12 \cdot 0767676^2 + 10604000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}32324^2$	$12 \cdot 0758919^2 + 10802000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}41081^2$
$1232 \cdot 0767676^2 + 107004000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}32324^2$	$1232 \cdot 0758919^2 + 109002000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}41081^2$
$123432 \cdot 0767676^2 + 1071004000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}32324^2 \quad (5.482)$	$123432 \cdot 0758919^2 + 1091002000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}41081^2 \quad (5.491)$
$0766711^2 + 966000^2 = \textcolor{red}{1} \textcolor{blue}{2}33289^2$	$0757936^2 + 984000^2 = \textcolor{red}{1} \textcolor{blue}{2}42064^2$
$12 \cdot 0766711^2 + 10626000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}33289^2$	$12 \cdot 0757936^2 + 10824000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}42064^2$
$1232 \cdot 0766711^2 + 107226000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}33289^2$	$1232 \cdot 0757936^2 + 109224000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}42064^2$
$123432 \cdot 0766711^2 + 1073226000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}33289^2 \quad (5.483)$	$123432 \cdot 0757936^2 + 1093224000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}42064^2 \quad (5.492)$
$0765744^2 + 968000^2 = \textcolor{red}{1} \textcolor{blue}{2}34256^2$	$0756951^2 + 986000^2 = \textcolor{red}{1} \textcolor{blue}{2}43049^2$
$12 \cdot 0765744^2 + 10648000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}34256^2$	$12 \cdot 0756951^2 + 10846000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}43049^2$
$1232 \cdot 0765744^2 + 107448000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}34256^2$	$1232 \cdot 0756951^2 + 109446000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}43049^2$
$123432 \cdot 0765744^2 + 1075448000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}34256^2 \quad (5.484)$	$123432 \cdot 0756951^2 + 1095446000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}43049^2 \quad (5.493)$
$0764775^2 + 970000^2 = \textcolor{red}{1} \textcolor{blue}{2}35225^2$	$0755964^2 + 988000^2 = \textcolor{red}{1} \textcolor{blue}{2}44036^2$
$12 \cdot 0764775^2 + 10670000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}35225^2$	$12 \cdot 0755964^2 + 10868000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}44036^2$
$1232 \cdot 0764775^2 + 107670000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}35225^2$	$1232 \cdot 0755964^2 + 109668000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}44036^2$
$123432 \cdot 0764775^2 + 1077670000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}35225^2 \quad (5.485)$	$123432 \cdot 0755964^2 + 1097668000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}44036^2 \quad (5.494)$
$0763804^2 + 972000^2 = \textcolor{red}{1} \textcolor{blue}{2}36196^2$	$0754975^2 + 990000^2 = \textcolor{red}{1} \textcolor{blue}{2}45025^2$
$12 \cdot 0763804^2 + 10692000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}36196^2$	$12 \cdot 0754975^2 + 10890000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}45025^2$
$1232 \cdot 0763804^2 + 107892000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}36196^2$	$1232 \cdot 0754975^2 + 109890000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}45025^2$
$123432 \cdot 0763804^2 + 1079892000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}36196^2 \quad (5.486)$	$123432 \cdot 0754975^2 + 1099890000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}45025^2 \quad (5.495)$
$0762831^2 + 974000^2 = \textcolor{red}{1} \textcolor{blue}{2}37169^2$	$0753984^2 + 992000^2 = \textcolor{red}{1} \textcolor{blue}{2}46016^2$
$12 \cdot 0762831^2 + 10714000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}37169^2$	$12 \cdot 0753984^2 + 10912000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}46016^2$
$1232 \cdot 0762831^2 + 108114000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}37169^2$	$1232 \cdot 0753984^2 + 110112000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}46016^2$
$123432 \cdot 0762831^2 + 1082114000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}37169^2 \quad (5.487)$	$123432 \cdot 0753984^2 + 1102112000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}46016^2 \quad (5.496)$
$0761856^2 + 976000^2 = \textcolor{red}{1} \textcolor{blue}{2}38144^2$	$0752991^2 + 994000^2 = \textcolor{red}{1} \textcolor{blue}{2}47009^2$
$12 \cdot 0761856^2 + 10736000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}38144^2$	$12 \cdot 0752991^2 + 10934000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}47009^2$
$1232 \cdot 0761856^2 + 108336000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}38144^2$	$1232 \cdot 0752991^2 + 110334000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}47009^2$
$123432 \cdot 0761856^2 + 1084336000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}38144^2 \quad (5.488)$	$123432 \cdot 0752991^2 + 1104334000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}47009^2 \quad (5.497)$
$0760879^2 + 978000^2 = \textcolor{red}{1} \textcolor{blue}{2}39121^2$	$0751996^2 + 996000^2 = \textcolor{red}{1} \textcolor{blue}{2}48004^2$
$12 \cdot 0760879^2 + 10758000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}39121^2$	$12 \cdot 0751996^2 + 10956000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}48004^2$
$1232 \cdot 0760879^2 + 108558000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}39121^2$	$1232 \cdot 0751996^2 + 110556000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}48004^2$
$123432 \cdot 0760879^2 + 1086558000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}39121^2 \quad (5.489)$	$123432 \cdot 0751996^2 + 1106556000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}48004^2 \quad (5.498)$
$0759900^2 + 980000^2 = \textcolor{red}{1} \textcolor{blue}{2}40100^2$	$0750992^2 + 998000^2 = \textcolor{red}{1} \textcolor{blue}{2}49001^2$
$12 \cdot 0759900^2 + 10780000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}40100^2$	$12 \cdot 0750992^2 + 10978000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{2}49001^2$
$1232 \cdot 0759900^2 + 108780000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}40100^2$	$1232 \cdot 0750992^2 + 110778000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \textcolor{blue}{2}49001^2$
$123432 \cdot 0759900^2 + 1088780000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}40100^2 \quad (5.490)$	$123432 \cdot 0750992^2 + 1108778000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \textcolor{blue}{2}49001^2 \quad (5.499)$

5.6 For $n = 500, 501, 501, \dots, 597, 598, 599$:

Let's consider

$$m = 1000, 11000, 111000, 1111000, 11111000, 111111000, 1111111000, 11111111000$$

in (1.1), then for each value of $n = 500, 501, 501, \dots, 597, 598, 599$; there are 100 *palindromic-type pandigital Pythagorean patterns* given below. In each case, only first four values are written. The other 5 values can be written on similar lines as done in subsection 5.1.

$0750000^2 + 1000000^2 = 1250000^2$	$0742951^2 + 1014000^2 = 1257049^2$
$120750000^2 + 11000000^2 = 121250000^2$	$120742951^2 + 11154000^2 = 121257049^2$
$12320750000^2 + 111000000^2 = 12321250000^2$	$12320742951^2 + 112554000^2 = 12321257049^2$
$1234320750000^2 + 1111000000^2 = 1234321250000^2 \quad (5.500)$	$1234320742951^2 + 1126554000^2 = 1234321257049^2 \quad (5.507)$
$0748999^2 + 1002000^2 = 1251001^2$	$0741936^2 + 1016000^2 = 1258064^2$
$120748999^2 + 11022000^2 = 121251001^2$	$120741936^2 + 11176000^2 = 121258064^2$
$12320748999^2 + 111222000^2 = 12321251001^2$	$12320741936^2 + 112776000^2 = 12321258064^2$
$1234320748999^2 + 1113222000^2 = 1234321251001^2 \quad (5.501)$	$1234320741936^2 + 1128776000^2 = 1234321258064^2 \quad (5.508)$
$0747996^2 + 1004000^2 = 1252004^2$	$0740919^2 + 1018000^2 = 1259081^2$
$120747996^2 + 11044000^2 = 121252004^2$	$120740919^2 + 11198000^2 = 121259081^2$
$12320747996^2 + 111444000^2 = 12321252004^2$	$12320740919^2 + 112998000^2 = 12321259081^2$
$1234320747996^2 + 1115444000^2 = 1234321252004^2 \quad (5.502)$	$1234320740919^2 + 1130998000^2 = 1234321259081^2 \quad (5.509)$
$0746991^2 + 1006000^2 = 1253009^2$	$0739900^2 + 1020000^2 = 1260100^2$
$120746991^2 + 11066000^2 = 121253009^2$	$120739900^2 + 11220000^2 = 121260100^2$
$12320746991^2 + 111666000^2 = 12321253009^2$	$12320739900^2 + 113220000^2 = 12321260100^2$
$1234320746991^2 + 1117666000^2 = 1234321253009^2 \quad (5.503)$	$1234320739900^2 + 1133220000^2 = 1234321260100^2 \quad (5.510)$
$0745984^2 + 1008000^2 = 1254016^2$	$0738879^2 + 1022000^2 = 1261121^2$
$120745984^2 + 11088000^2 = 121254016^2$	$120738879^2 + 11242000^2 = 121261121^2$
$12320745984^2 + 111888000^2 = 12321254016^2$	$12320738879^2 + 113442000^2 = 12321261121^2$
$1234320745984^2 + 1119888000^2 = 1234321254016^2 \quad (5.504)$	$1234320738879^2 + 1135442000^2 = 1234321261121^2 \quad (5.511)$
$0744975^2 + 1010000^2 = 1255025^2$	$0737856^2 + 1024000^2 = 1262144^2$
$120744975^2 + 11110000^2 = 121255025^2$	$120737856^2 + 11264000^2 = 121262144^2$
$12320744975^2 + 112110000^2 = 12321255025^2$	$12320737856^2 + 113664000^2 = 12321262144^2$
$1234320744975^2 + 1122110000^2 = 1234321255025^2 \quad (5.505)$	$1234320737856^2 + 1137664000^2 = 1234321262144^2 \quad (5.512)$
$0743964^2 + 1012000^2 = 1256036^2$	$0736831^2 + 1026000^2 = 1263169^2$
$120743964^2 + 11132000^2 = 121256036^2$	$120736831^2 + 11286000^2 = 121263169^2$
$12320743964^2 + 112332000^2 = 12321256036^2$	$12320736831^2 + 113886000^2 = 12321263169^2$
$1234320743964^2 + 1124332000^2 = 1234321256036^2 \quad (5.506)$	$1234320736831^2 + 1139886000^2 = 1234321263169^2 \quad (5.513)$

$$\begin{aligned}
& 0735804^2 + 1028000^2 = \mathbf{1} 264196^2 \\
& \mathbf{12} 0735804^2 + 11308000^2 = \mathbf{121} 264196^2 \\
& \mathbf{1232} 0735804^2 + 114108000^2 = \mathbf{12321} 264196^2 \\
& \mathbf{123432} 0735804^2 + 1142108000^2 = \mathbf{1234321} 264196^2 \quad (5.514) \\
& \\
& 0734775^2 + 1030000^2 = \mathbf{1} 265225^2 \\
& \mathbf{12} 0734775^2 + 11330000^2 = \mathbf{121} 265225^2 \\
& \mathbf{1232} 0734775^2 + 114330000^2 = \mathbf{12321} 265225^2 \\
& \mathbf{123432} 0734775^2 + 1144330000^2 = \mathbf{1234321} 265225^2 \quad (5.515) \\
& \\
& 0733744^2 + 1032000^2 = \mathbf{1} 266256^2 \\
& \mathbf{12} 0733744^2 + 11352000^2 = \mathbf{121} 266256^2 \\
& \mathbf{1232} 0733744^2 + 114552000^2 = \mathbf{12321} 266256^2 \\
& \mathbf{123432} 0733744^2 + 1146552000^2 = \mathbf{1234321} 266256^2 \quad (5.516) \\
& \\
& 0732711^2 + 1034000^2 = \mathbf{1} 267289^2 \\
& \mathbf{12} 0732711^2 + 11374000^2 = \mathbf{121} 267289^2 \\
& \mathbf{1232} 0732711^2 + 114774000^2 = \mathbf{12321} 267289^2 \\
& \mathbf{123432} 0732711^2 + 1148774000^2 = \mathbf{1234321} 267289^2 \quad (5.517) \\
& \\
& 0731676^2 + 1036000^2 = \mathbf{1} 268324^2 \\
& \mathbf{12} 0731676^2 + 11396000^2 = \mathbf{121} 268324^2 \\
& \mathbf{1232} 0731676^2 + 114996000^2 = \mathbf{12321} 268324^2 \\
& \mathbf{123432} 0731676^2 + 1150996000^2 = \mathbf{1234321} 268324^2 \quad (5.518) \\
& \\
& 0730639^2 + 1038000^2 = \mathbf{1} 269361^2 \\
& \mathbf{12} 0730639^2 + 11418000^2 = \mathbf{121} 269361^2 \\
& \mathbf{1232} 0730639^2 + 115218000^2 = \mathbf{12321} 269361^2 \\
& \mathbf{123432} 0730639^2 + 1153218000^2 = \mathbf{1234321} 269361^2 \quad (5.519) \\
& \\
& 0729600^2 + 1040000^2 = \mathbf{1} 270400^2 \\
& \mathbf{12} 0729600^2 + 11440000^2 = \mathbf{121} 270400^2 \\
& \mathbf{1232} 0729600^2 + 115440000^2 = \mathbf{12321} 270400^2 \\
& \mathbf{123432} 0729600^2 + 1155440000^2 = \mathbf{1234321} 270400^2 \quad (5.520) \\
& \\
& 0728559^2 + 1042000^2 = \mathbf{1} 271441^2 \\
& \mathbf{12} 0728559^2 + 11462000^2 = \mathbf{121} 271441^2 \\
& \mathbf{1232} 0728559^2 + 115662000^2 = \mathbf{12321} 271441^2 \\
& \mathbf{123432} 0728559^2 + 1157662000^2 = \mathbf{1234321} 271441^2 \quad (5.521) \\
& \\
& 0727516^2 + 1044000^2 = \mathbf{1} 272484^2 \\
& \mathbf{12} 0727516^2 + 11484000^2 = \mathbf{121} 272484^2 \\
& \mathbf{1232} 0727516^2 + 115884000^2 = \mathbf{12321} 272484^2 \\
& \mathbf{123432} 0727516^2 + 1159884000^2 = \mathbf{1234321} 272484^2 \quad (5.522) \\
& \\
& 0726471^2 + 1046000^2 = \mathbf{1} 273529^2 \\
& \mathbf{12} 0726471^2 + 11506000^2 = \mathbf{121} 273529^2 \\
& \mathbf{1232} 0726471^2 + 116106000^2 = \mathbf{12321} 273529^2 \\
& \mathbf{123432} 0726471^2 + 1162106000^2 = \mathbf{1234321} 273529^2 \quad (5.523) \\
& \\
& 0725424^2 + 1048000^2 = \mathbf{1} 274576^2 \\
& \mathbf{12} 0725424^2 + 11528000^2 = \mathbf{121} 274576^2 \\
& \mathbf{1232} 0725424^2 + 116328000^2 = \mathbf{12321} 274576^2 \\
& \mathbf{123432} 0725424^2 + 1164328000^2 = \mathbf{1234321} 274576^2 \quad (5.524) \\
& \\
& 0724375^2 + 1050000^2 = \mathbf{1} 275625^2 \\
& \mathbf{12} 0724375^2 + 11550000^2 = \mathbf{121} 275625^2 \\
& \mathbf{1232} 0724375^2 + 116550000^2 = \mathbf{12321} 275625^2 \\
& \mathbf{123432} 0724375^2 + 1166550000^2 = \mathbf{1234321} 275625^2 \quad (5.525) \\
& \\
& 0723324^2 + 1052000^2 = \mathbf{1} 276676^2 \\
& \mathbf{12} 0723324^2 + 11572000^2 = \mathbf{121} 276676^2 \\
& \mathbf{1232} 0723324^2 + 116772000^2 = \mathbf{12321} 276676^2 \\
& \mathbf{123432} 0723324^2 + 1168772000^2 = \mathbf{1234321} 276676^2 \quad (5.526) \\
& \\
& 0722271^2 + 1054000^2 = \mathbf{1} 277729^2 \\
& \mathbf{12} 0722271^2 + 11594000^2 = \mathbf{121} 277729^2 \\
& \mathbf{1232} 0722271^2 + 116994000^2 = \mathbf{12321} 277729^2 \\
& \mathbf{123432} 0722271^2 + 1170994000^2 = \mathbf{1234321} 277729^2 \quad (5.527) \\
& \\
& 0721216^2 + 1056000^2 = \mathbf{1} 278784^2 \\
& \mathbf{12} 0721216^2 + 11616000^2 = \mathbf{121} 278784^2 \\
& \mathbf{1232} 0721216^2 + 117216000^2 = \mathbf{12321} 278784^2 \\
& \mathbf{123432} 0721216^2 + 1173216000^2 = \mathbf{1234321} 278784^2 \quad (5.528) \\
& \\
& 0720159^2 + 1058000^2 = \mathbf{1} 279841^2 \\
& \mathbf{12} 0720159^2 + 11638000^2 = \mathbf{121} 279841^2 \\
& \mathbf{1232} 0720159^2 + 117438000^2 = \mathbf{12321} 279841^2 \\
& \mathbf{123432} 0720159^2 + 1175438000^2 = \mathbf{1234321} 279841^2 \quad (5.529) \\
& \\
& 0719100^2 + 1060000^2 = \mathbf{1} 280900^2 \\
& \mathbf{12} 0719100^2 + 11660000^2 = \mathbf{121} 280900^2 \\
& \mathbf{1232} 0719100^2 + 117660000^2 = \mathbf{12321} 280900^2 \\
& \mathbf{123432} 0719100^2 + 1177660000^2 = \mathbf{1234321} 280900^2 \quad (5.530)
\end{aligned}$$

$$\begin{aligned}
& 0718039^2 + 1062000^2 = \mathbf{1} 281961^2 \\
& \mathbf{12} 0718039^2 + 11682000^2 = \mathbf{121} 281961^2 \\
& \mathbf{1232} 0718039^2 + 117882000^2 = \mathbf{12321} 281961^2 \\
& \mathbf{123432} 0718039^2 + 1179882000^2 = \mathbf{1234321} 281961^2 \quad (5.531) \\
& \\
& 0716976^2 + 1064000^2 = \mathbf{1} 283024^2 \\
& \mathbf{12} 0716976^2 + 11704000^2 = \mathbf{121} 283024^2 \\
& \mathbf{1232} 0716976^2 + 118104000^2 = \mathbf{12321} 283024^2 \\
& \mathbf{123432} 0716976^2 + 1182104000^2 = \mathbf{1234321} 283024^2 \quad (5.532) \\
& \\
& 0715911^2 + 1066000^2 = \mathbf{1} 284089^2 \\
& \mathbf{12} 0715911^2 + 11726000^2 = \mathbf{121} 284089^2 \\
& \mathbf{1232} 0715911^2 + 118326000^2 = \mathbf{12321} 284089^2 \\
& \mathbf{123432} 0715911^2 + 1184326000^2 = \mathbf{1234321} 284089^2 \quad (5.533) \\
& \\
& 0714844^2 + 1068000^2 = \mathbf{1} 285156^2 \\
& \mathbf{12} 0714844^2 + 11748000^2 = \mathbf{121} 285156^2 \\
& \mathbf{1232} 0714844^2 + 118548000^2 = \mathbf{12321} 285156^2 \\
& \mathbf{123432} 0714844^2 + 1186548000^2 = \mathbf{1234321} 285156^2 \quad (5.534) \\
& \\
& 0713775^2 + 1070000^2 = \mathbf{1} 286225^2 \\
& \mathbf{12} 0713775^2 + 11770000^2 = \mathbf{121} 286225^2 \\
& \mathbf{1232} 0713775^2 + 118770000^2 = \mathbf{12321} 286225^2 \\
& \mathbf{123432} 0713775^2 + 1188770000^2 = \mathbf{1234321} 286225^2 \quad (5.535) \\
& \\
& 0712704^2 + 1072000^2 = \mathbf{1} 287296^2 \\
& \mathbf{12} 0712704^2 + 11792000^2 = \mathbf{121} 287296^2 \\
& \mathbf{1232} 0712704^2 + 118992000^2 = \mathbf{12321} 287296^2 \\
& \mathbf{123432} 0712704^2 + 1190992000^2 = \mathbf{1234321} 287296^2 \quad (5.536) \\
& \\
& 0711631^2 + 1074000^2 = \mathbf{1} 288369^2 \\
& \mathbf{12} 0711631^2 + 11814000^2 = \mathbf{121} 288369^2 \\
& \mathbf{1232} 0711631^2 + 119214000^2 = \mathbf{12321} 288369^2 \\
& \mathbf{123432} 0711631^2 + 1193214000^2 = \mathbf{1234321} 288369^2 \quad (5.537) \\
& \\
& 0710556^2 + 1076000^2 = \mathbf{1} 289444^2 \\
& \mathbf{12} 0710556^2 + 11836000^2 = \mathbf{121} 289444^2 \\
& \mathbf{1232} 0710556^2 + 119436000^2 = \mathbf{12321} 289444^2 \\
& \mathbf{123432} 0710556^2 + 1195436000^2 = \mathbf{1234321} 289444^2 \quad (5.538) \\
& \\
& 0709479^2 + 1078000^2 = \mathbf{1} 290521^2 \\
& \mathbf{12} 0709479^2 + 11858000^2 = \mathbf{121} 290521^2 \\
& \mathbf{1232} 0709479^2 + 119658000^2 = \mathbf{12321} 290521^2 \\
& \mathbf{123432} 0709479^2 + 1197658000^2 = \mathbf{1234321} 290521^2 \quad (5.539) \\
& \\
& 0708400^2 + 1080000^2 = \mathbf{1} 291600^2 \\
& \mathbf{12} 0708400^2 + 11880000^2 = \mathbf{121} 291600^2 \\
& \mathbf{1232} 0708400^2 + 119880000^2 = \mathbf{12321} 291600^2 \\
& \mathbf{123432} 0708400^2 + 1199880000^2 = \mathbf{1234321} 291600^2 \quad (5.540) \\
& \\
& 0707319^2 + 1082000^2 = \mathbf{1} 292681^2 \\
& \mathbf{12} 0707319^2 + 11902000^2 = \mathbf{121} 292681^2 \\
& \mathbf{1232} 0707319^2 + 120102000^2 = \mathbf{12321} 292681^2 \\
& \mathbf{123432} 0707319^2 + 1202102000^2 = \mathbf{1234321} 292681^2 \quad (5.541) \\
& \\
& 0706236^2 + 1084000^2 = \mathbf{1} 293764^2 \\
& \mathbf{12} 0706236^2 + 11924000^2 = \mathbf{121} 293764^2 \\
& \mathbf{1232} 0706236^2 + 120324000^2 = \mathbf{12321} 293764^2 \\
& \mathbf{123432} 0706236^2 + 1204324000^2 = \mathbf{1234321} 293764^2 \quad (5.542) \\
& \\
& 0705151^2 + 1086000^2 = \mathbf{1} 294849^2 \\
& \mathbf{12} 0705151^2 + 11946000^2 = \mathbf{121} 294849^2 \\
& \mathbf{1232} 0705151^2 + 120546000^2 = \mathbf{12321} 294849^2 \\
& \mathbf{123432} 0705151^2 + 1206546000^2 = \mathbf{1234321} 294849^2 \quad (5.543) \\
& \\
& 0704064^2 + 1088000^2 = \mathbf{1} 295936^2 \\
& \mathbf{12} 0704064^2 + 11968000^2 = \mathbf{121} 295936^2 \\
& \mathbf{1232} 0704064^2 + 120768000^2 = \mathbf{12321} 295936^2 \\
& \mathbf{123432} 0704064^2 + 1208768000^2 = \mathbf{1234321} 295936^2 \quad (5.544) \\
& \\
& 0702975^2 + 1090000^2 = \mathbf{1} 297025^2 \\
& \mathbf{12} 0702975^2 + 11990000^2 = \mathbf{121} 297025^2 \\
& \mathbf{1232} 0702975^2 + 120990000^2 = \mathbf{12321} 297025^2 \\
& \mathbf{123432} 0702975^2 + 1210990000^2 = \mathbf{1234321} 297025^2 \quad (5.545) \\
& \\
& 0701884^2 + 1092000^2 = \mathbf{1} 298116^2 \\
& \mathbf{12} 0701884^2 + 12012000^2 = \mathbf{121} 298116^2 \\
& \mathbf{1232} 0701884^2 + 121212000^2 = \mathbf{12321} 298116^2 \\
& \mathbf{123432} 0701884^2 + 1213212000^2 = \mathbf{1234321} 298116^2 \quad (5.546) \\
& \\
& 0700791^2 + 1094000^2 = \mathbf{1} 299209^2 \\
& \mathbf{12} 0700791^2 + 12034000^2 = \mathbf{121} 299209^2 \\
& \mathbf{1232} 0700791^2 + 121434000^2 = \mathbf{12321} 299209^2 \\
& \mathbf{123432} 0700791^2 + 1215434000^2 = \mathbf{1234321} 299209^2 \quad (5.547)
\end{aligned}$$

$$\begin{aligned}
& 0699696^2 + 1096000^2 = \mathbf{1} 300304^2 \\
& \mathbf{12} 0699696^2 + 12056000^2 = \mathbf{121} 300304^2 \\
& \mathbf{1232} 0699696^2 + 121656000^2 = \mathbf{12321} 300304^2 \\
& \mathbf{123432} 0699696^2 + 1217656000^2 = \mathbf{1234321} 300304^2 \quad (5.548) \\
& \\
& 0698599^2 + 1098000^2 = \mathbf{1} 301401^2 \\
& \mathbf{12} 0698599^2 + 12078000^2 = \mathbf{121} 301401^2 \\
& \mathbf{1232} 0698599^2 + 121878000^2 = \mathbf{12321} 301401^2 \\
& \mathbf{123432} 0698599^2 + 1219878000^2 = \mathbf{1234321} 301401^2 \quad (5.549) \\
& \\
& 0697500^2 + 1100000^2 = \mathbf{1} 302500^2 \\
& \mathbf{12} 0697500^2 + 12100000^2 = \mathbf{121} 302500^2 \\
& \mathbf{1232} 0697500^2 + 122100000^2 = \mathbf{12321} 302500^2 \\
& \mathbf{123432} 0697500^2 + 1222100000^2 = \mathbf{1234321} 302500^2 \quad (5.550) \\
& \\
& 0696399^2 + 1102000^2 = \mathbf{1} 303601^2 \\
& \mathbf{12} 0696399^2 + 12122000^2 = \mathbf{121} 303601^2 \\
& \mathbf{1232} 0696399^2 + 122322000^2 = \mathbf{12321} 303601^2 \\
& \mathbf{123432} 0696399^2 + 1224322000^2 = \mathbf{1234321} 303601^2 \quad (5.551) \\
& \\
& 0695296^2 + 1104000^2 = \mathbf{1} 304704^2 \\
& \mathbf{12} 0695296^2 + 12144000^2 = \mathbf{121} 304704^2 \\
& \mathbf{1232} 0695296^2 + 122544000^2 = \mathbf{12321} 304704^2 \\
& \mathbf{123432} 0695296^2 + 1226544000^2 = \mathbf{1234321} 304704^2 \quad (5.552) \\
& \\
& 0694191^2 + 1106000^2 = \mathbf{1} 305809^2 \\
& \mathbf{12} 0694191^2 + 12166000^2 = \mathbf{121} 305809^2 \\
& \mathbf{1232} 0694191^2 + 122766000^2 = \mathbf{12321} 305809^2 \\
& \mathbf{123432} 0694191^2 + 1228766000^2 = \mathbf{1234321} 305809^2 \quad (5.553) \\
& \\
& 0693084^2 + 1108000^2 = \mathbf{1} 306916^2 \\
& \mathbf{12} 0693084^2 + 12188000^2 = \mathbf{121} 306916^2 \\
& \mathbf{1232} 0693084^2 + 122988000^2 = \mathbf{12321} 306916^2 \\
& \mathbf{123432} 0693084^2 + 1230988000^2 = \mathbf{1234321} 306916^2 \quad (5.554) \\
& \\
& 0691975^2 + 1110000^2 = \mathbf{1} 308025^2 \\
& \mathbf{12} 0691975^2 + 12210000^2 = \mathbf{121} 308025^2 \\
& \mathbf{1232} 0691975^2 + 123210000^2 = \mathbf{12321} 308025^2 \\
& \mathbf{123432} 0691975^2 + 1233210000^2 = \mathbf{1234321} 308025^2 \quad (5.555) \\
& \\
& 0690864^2 + 1112000^2 = \mathbf{1} 309136^2 \\
& \mathbf{12} 0690864^2 + 12232000^2 = \mathbf{121} 309136^2 \\
& \mathbf{1232} 0690864^2 + 123432000^2 = \mathbf{12321} 309136^2 \\
& \mathbf{123432} 0690864^2 + 1235432000^2 = \mathbf{1234321} 309136^2 \quad (5.556)
\end{aligned}$$

$$\begin{aligned}
& 0680775^2 + 1130000^2 = \mathbf{1} 319225^2 \\
& \mathbf{12} 0680775^2 + 12430000^2 = \mathbf{121} 319225^2 \\
& \mathbf{1232} 0680775^2 + 125430000^2 = \mathbf{12321} 319225^2 \\
& \mathbf{123432} 0680775^2 + 1255430000^2 = \mathbf{1234321} 319225^2 \quad (5.565) \\
& \\
& 0679644^2 + 1132000^2 = \mathbf{1} 320356^2 \\
& \mathbf{12} 0679644^2 + 12452000^2 = \mathbf{121} 320356^2 \\
& \mathbf{1232} 0679644^2 + 125652000^2 = \mathbf{12321} 320356^2 \\
& \mathbf{123432} 0679644^2 + 1257652000^2 = \mathbf{1234321} 320356^2 \quad (5.566) \\
& \\
& 0678511^2 + 1134000^2 = \mathbf{1} 321489^2 \\
& \mathbf{12} 0678511^2 + 12474000^2 = \mathbf{121} 321489^2 \\
& \mathbf{1232} 0678511^2 + 125874000^2 = \mathbf{12321} 321489^2 \\
& \mathbf{123432} 0678511^2 + 1259874000^2 = \mathbf{1234321} 321489^2 \quad (5.567) \\
& \\
& 0677376^2 + 1136000^2 = \mathbf{1} 322624^2 \\
& \mathbf{12} 0677376^2 + 12496000^2 = \mathbf{121} 322624^2 \\
& \mathbf{1232} 0677376^2 + 126096000^2 = \mathbf{12321} 322624^2 \\
& \mathbf{123432} 0677376^2 + 1262096000^2 = \mathbf{1234321} 322624^2 \quad (5.568) \\
& \\
& 0676239^2 + 1138000^2 = \mathbf{1} 323761^2 \\
& \mathbf{12} 0676239^2 + 12518000^2 = \mathbf{121} 323761^2 \\
& \mathbf{1232} 0676239^2 + 126318000^2 = \mathbf{12321} 323761^2 \\
& \mathbf{123432} 0676239^2 + 1264318000^2 = \mathbf{1234321} 323761^2 \quad (5.569) \\
& \\
& 0675100^2 + 1140000^2 = \mathbf{1} 324900^2 \\
& \mathbf{12} 0675100^2 + 12540000^2 = \mathbf{121} 324900^2 \\
& \mathbf{1232} 0675100^2 + 126540000^2 = \mathbf{12321} 324900^2 \\
& \mathbf{123432} 0675100^2 + 1266540000^2 = \mathbf{1234321} 324900^2 \quad (5.570) \\
& \\
& 0673959^2 + 1142000^2 = \mathbf{1} 326041^2 \\
& \mathbf{12} 0673959^2 + 12562000^2 = \mathbf{121} 326041^2 \\
& \mathbf{1232} 0673959^2 + 126762000^2 = \mathbf{12321} 326041^2 \\
& \mathbf{123432} 0673959^2 + 1268762000^2 = \mathbf{1234321} 326041^2 \quad (5.571) \\
& \\
& 0672816^2 + 1144000^2 = \mathbf{1} 327184^2 \\
& \mathbf{12} 0672816^2 + 12584000^2 = \mathbf{121} 327184^2 \\
& \mathbf{1232} 0672816^2 + 126984000^2 = \mathbf{12321} 327184^2 \\
& \mathbf{123432} 0672816^2 + 1270984000^2 = \mathbf{1234321} 327184^2 \quad (5.572) \\
& \\
& 0671671^2 + 1146000^2 = \mathbf{1} 328329^2 \\
& \mathbf{12} 0671671^2 + 12606000^2 = \mathbf{121} 328329^2 \\
& \mathbf{1232} 0671671^2 + 127206000^2 = \mathbf{12321} 328329^2 \\
& \mathbf{123432} 0671671^2 + 1273206000^2 = \mathbf{1234321} 328329^2 \quad (5.573) \\
& \\
& 0670524^2 + 1148000^2 = \mathbf{1} 329476^2 \\
& \mathbf{12} 0670524^2 + 12628000^2 = \mathbf{121} 329476^2 \\
& \mathbf{1232} 0670524^2 + 127428000^2 = \mathbf{12321} 329476^2 \\
& \mathbf{123432} 0670524^2 + 1275428000^2 = \mathbf{1234321} 329476^2 \quad (5.574) \\
& \\
& 0669375^2 + 1150000^2 = \mathbf{1} 330625^2 \\
& \mathbf{12} 0669375^2 + 12650000^2 = \mathbf{121} 330625^2 \\
& \mathbf{1232} 0669375^2 + 127650000^2 = \mathbf{12321} 330625^2 \\
& \mathbf{123432} 0669375^2 + 1277650000^2 = \mathbf{1234321} 330625^2 \quad (5.575) \\
& \\
& 0668224^2 + 1152000^2 = \mathbf{1} 331776^2 \\
& \mathbf{12} 0668224^2 + 12672000^2 = \mathbf{121} 331776^2 \\
& \mathbf{1232} 0668224^2 + 127872000^2 = \mathbf{12321} 331776^2 \\
& \mathbf{123432} 0668224^2 + 1279872000^2 = \mathbf{1234321} 331776^2 \quad (5.576) \\
& \\
& 0667071^2 + 1154000^2 = \mathbf{1} 332929^2 \\
& \mathbf{12} 0667071^2 + 12694000^2 = \mathbf{121} 332929^2 \\
& \mathbf{1232} 0667071^2 + 128094000^2 = \mathbf{12321} 332929^2 \\
& \mathbf{123432} 0667071^2 + 1282094000^2 = \mathbf{1234321} 332929^2 \quad (5.577) \\
& \\
& 0665916^2 + 1156000^2 = \mathbf{1} 334084^2 \\
& \mathbf{12} 0665916^2 + 12716000^2 = \mathbf{121} 334084^2 \\
& \mathbf{1232} 0665916^2 + 128316000^2 = \mathbf{12321} 334084^2 \\
& \mathbf{123432} 0665916^2 + 1284316000^2 = \mathbf{1234321} 334084^2 \quad (5.578) \\
& \\
& 0664759^2 + 1158000^2 = \mathbf{1} 335241^2 \\
& \mathbf{12} 0664759^2 + 12738000^2 = \mathbf{121} 335241^2 \\
& \mathbf{1232} 0664759^2 + 128538000^2 = \mathbf{12321} 335241^2 \\
& \mathbf{123432} 0664759^2 + 1286538000^2 = \mathbf{1234321} 335241^2 \quad (5.579) \\
& \\
& 0663600^2 + 1160000^2 = \mathbf{1} 336400^2 \\
& \mathbf{12} 0663600^2 + 12760000^2 = \mathbf{121} 336400^2 \\
& \mathbf{1232} 0663600^2 + 128760000^2 = \mathbf{12321} 336400^2 \\
& \mathbf{123432} 0663600^2 + 1288760000^2 = \mathbf{1234321} 336400^2 \quad (5.580) \\
& \\
& 0662439^2 + 1162000^2 = \mathbf{1} 337561^2 \\
& \mathbf{12} 0662439^2 + 12782000^2 = \mathbf{121} 337561^2 \\
& \mathbf{1232} 0662439^2 + 128982000^2 = \mathbf{12321} 337561^2 \\
& \mathbf{123432} 0662439^2 + 1290982000^2 = \mathbf{1234321} 337561^2 \quad (5.581)
\end{aligned}$$

$0661276^2 + 1164000^2 = \textcolor{red}{1} \textcolor{blue}{3}38724^2$	$0650719^2 + 1182000^2 = \textcolor{red}{1} \textcolor{blue}{3}49281^2$
$12 \ 0661276^2 + 12804000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 338724^2$	$12 \ 0650719^2 + 13002000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 349281^2$
$1232 \ 0661276^2 + 129204000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 338724^2$	$1232 \ 0650719^2 + 131202000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 349281^2$
$123432 \ 0661276^2 + 1293204000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 338724^2 \ (5.582)$	$123432 \ 0650719^2 + 1313202000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 349281^2 \ (5.591)$
$0660111^2 + 1166000^2 = \textcolor{red}{1} \textcolor{blue}{3}39889^2$	$0649536^2 + 1184000^2 = \textcolor{red}{1} \textcolor{blue}{3}50464^2$
$12 \ 0660111^2 + 12826000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 339889^2$	$12 \ 0649536^2 + 13024000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 350464^2$
$1232 \ 0660111^2 + 129426000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 339889^2$	$1232 \ 0649536^2 + 131424000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 350464^2$
$123432 \ 0660111^2 + 1295426000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 339889^2 \ (5.583)$	$123432 \ 0649536^2 + 1315424000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 350464^2 \ (5.592)$
$0658944^2 + 1168000^2 = \textcolor{red}{1} \textcolor{blue}{3}41056^2$	$0648351^2 + 1186000^2 = \textcolor{red}{1} \textcolor{blue}{3}51649^2$
$12 \ 0658944^2 + 12848000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 341056^2$	$12 \ 0648351^2 + 13046000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 351649^2$
$1232 \ 0658944^2 + 129648000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 341056^2$	$1232 \ 0648351^2 + 131646000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 351649^2$
$123432 \ 0658944^2 + 1297648000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 341056^2 \ (5.584)$	$123432 \ 0648351^2 + 1317646000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 351649^2 \ (5.593)$
$0657775^2 + 1170000^2 = \textcolor{red}{1} \textcolor{blue}{3}42225^2$	$0647164^2 + 1188000^2 = \textcolor{red}{1} \textcolor{blue}{3}52836^2$
$12 \ 0657775^2 + 12870000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 342225^2$	$12 \ 0647164^2 + 13068000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 352836^2$
$1232 \ 0657775^2 + 129870000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 342225^2$	$1232 \ 0647164^2 + 131868000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 352836^2$
$123432 \ 0657775^2 + 1299870000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 342225^2 \ (5.585)$	$123432 \ 0647164^2 + 1319868000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 352836^2 \ (5.594)$
$0656604^2 + 1172000^2 = \textcolor{red}{1} \textcolor{blue}{3}43396^2$	$0645975^2 + 1190000^2 = \textcolor{red}{1} \textcolor{blue}{3}54025^2$
$12 \ 0656604^2 + 12892000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 343396^2$	$12 \ 0645975^2 + 13090000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 354025^2$
$1232 \ 0656604^2 + 130092000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 343396^2$	$1232 \ 0645975^2 + 132090000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 354025^2$
$123432 \ 0656604^2 + 1302092000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 343396^2 \ (5.586)$	$123432 \ 0645975^2 + 1322090000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 354025^2 \ (5.595)$
$0655431^2 + 1174000^2 = \textcolor{red}{1} \textcolor{blue}{3}44569^2$	$0644784^2 + 1192000^2 = \textcolor{red}{1} \textcolor{blue}{3}55216^2$
$12 \ 0655431^2 + 12914000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 344569^2$	$12 \ 0644784^2 + 13112000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 355216^2$
$1232 \ 0655431^2 + 130314000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 344569^2$	$1232 \ 0644784^2 + 132312000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 355216^2$
$123432 \ 0655431^2 + 1304314000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 344569^2 \ (5.587)$	$123432 \ 0644784^2 + 1324312000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 355216^2 \ (5.596)$
$0654256^2 + 1176000^2 = \textcolor{red}{1} \textcolor{blue}{3}45744^2$	$0643591^2 + 1194000^2 = \textcolor{red}{1} \textcolor{blue}{3}56409^2$
$12 \ 0654256^2 + 12936000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 345744^2$	$12 \ 0643591^2 + 13134000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 356409^2$
$1232 \ 0654256^2 + 130536000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 345744^2$	$1232 \ 0643591^2 + 132534000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 356409^2$
$123432 \ 0654256^2 + 1306536000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 345744^2 \ (5.588)$	$123432 \ 0643591^2 + 1326534000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 356409^2 \ (5.597)$
$0653079^2 + 1178000^2 = \textcolor{red}{1} \textcolor{blue}{3}46921^2$	$0642396^2 + 1196000^2 = \textcolor{red}{1} \textcolor{blue}{3}57604^2$
$12 \ 0653079^2 + 12958000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 346921^2$	$12 \ 0642396^2 + 13156000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 357604^2$
$1232 \ 0653079^2 + 130758000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 346921^2$	$1232 \ 0642396^2 + 132756000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 357604^2$
$123432 \ 0653079^2 + 1308758000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 346921^2 \ (5.589)$	$123432 \ 0642396^2 + 1328756000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 357604^2 \ (5.598)$
$0651900^2 + 1180000^2 = \textcolor{red}{1} \textcolor{blue}{3}48100^2$	$0641199^2 + 1198000^2 = \textcolor{red}{1} \textcolor{blue}{3}58801^2$
$12 \ 0651900^2 + 12980000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 348100^2$	$12 \ 0641199^2 + 13178000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \ 358801^2$
$1232 \ 0651900^2 + 130980000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 348100^2$	$1232 \ 0641199^2 + 132978000^2 = \textcolor{red}{1} \textcolor{blue}{2}321 \ 358801^2$
$123432 \ 0651900^2 + 1310980000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 348100^2 \ (5.590)$	$123432 \ 0641199^2 + 1330978000^2 = \textcolor{red}{1} \textcolor{blue}{2}34321 \ 358801^2 \ (5.599)$

5.7 For $n = 600, 601, 601, \dots, 697, 698, 699$:

Let's consider

$$m = 1000, 11000, 111000, 1111000, 11111000, 111111000, 1111111000, 11111111000$$

in (1.1), then for each value of $n = 600, 601, 601, \dots, 697, 698, 699$; there are 100 *palindromic-type pandigital Pythagorean patterns* given below. In each case, only first four values are written. The other 5 values can be written on similar lines as done in subsection 5.1.1.

$0640000^2 + 1200000^2 = 1360000^2$	$0631551^2 + 1214000^2 = 1368449^2$
$120640000^2 + 13200000^2 = 121360000^2$	$120631551^2 + 13354000^2 = 121368449^2$
$12320640000^2 + 133200000^2 = 12321360000^2$	$12320631551^2 + 134754000^2 = 12321368449^2$
$1234320640000^2 + 1333200000^2 = 1234321360000^2$ (5.600)	$1234320631551^2 + 1348754000^2 = 1234321368449^2$ (5.607)
$0638799^2 + 1202000^2 = 1361201^2$	$0630336^2 + 1216000^2 = 1369664^2$
$120638799^2 + 13222000^2 = 121361201^2$	$120630336^2 + 13376000^2 = 121369664^2$
$12320638799^2 + 133422000^2 = 12321361201^2$	$12320630336^2 + 134976000^2 = 12321369664^2$
$1234320638799^2 + 1335422000^2 = 1234321361201^2$ (5.601)	$1234320630336^2 + 1350976000^2 = 1234321369664^2$ (5.608)
$0637596^2 + 1204000^2 = 1362404^2$	$0629119^2 + 1218000^2 = 1370881^2$
$120637596^2 + 13244000^2 = 121362404^2$	$120629119^2 + 13398000^2 = 121370881^2$
$12320637596^2 + 133644000^2 = 12321362404^2$	$12320629119^2 + 135198000^2 = 12321370881^2$
$1234320637596^2 + 1337644000^2 = 1234321362404^2$ (5.602)	$1234320629119^2 + 1353198000^2 = 1234321370881^2$ (5.609)
$0636391^2 + 1206000^2 = 1363609^2$	$0627900^2 + 1220000^2 = 1372100^2$
$120636391^2 + 13266000^2 = 121363609^2$	$120627900^2 + 13420000^2 = 121372100^2$
$12320636391^2 + 133866000^2 = 12321363609^2$	$12320627900^2 + 135420000^2 = 12321372100^2$
$1234320636391^2 + 1339866000^2 = 1234321363609^2$ (5.603)	$1234320627900^2 + 1355420000^2 = 1234321372100^2$ (5.610)
$0635184^2 + 1208000^2 = 1364816^2$	$0626679^2 + 1222000^2 = 1373321^2$
$120635184^2 + 13288000^2 = 121364816^2$	$120626679^2 + 13442000^2 = 121373321^2$
$12320635184^2 + 134088000^2 = 12321364816^2$	$12320626679^2 + 135642000^2 = 12321373321^2$
$1234320635184^2 + 1342088000^2 = 1234321364816^2$ (5.604)	$1234320626679^2 + 1357642000^2 = 1234321373321^2$ (5.611)
$0633975^2 + 1210000^2 = 1366025^2$	$0625456^2 + 1224000^2 = 1374544^2$
$120633975^2 + 13310000^2 = 121366025^2$	$120625456^2 + 13464000^2 = 121374544^2$
$12320633975^2 + 134310000^2 = 12321366025^2$	$12320625456^2 + 135864000^2 = 12321374544^2$
$1234320633975^2 + 1344310000^2 = 1234321366025^2$ (5.605)	$1234320625456^2 + 1359864000^2 = 1234321374544^2$ (5.612)
$0632764^2 + 1212000^2 = 1367236^2$	$0624231^2 + 1226000^2 = 1375769^2$
$120632764^2 + 13332000^2 = 121367236^2$	$120624231^2 + 13486000^2 = 121375769^2$
$12320632764^2 + 134532000^2 = 12321367236^2$	$12320624231^2 + 136086000^2 = 12321375769^2$
$1234320632764^2 + 1346532000^2 = 1234321367236^2$ (5.606)	$1234320624231^2 + 1362086000^2 = 1234321375769^2$ (5.613)

$$\begin{aligned}
& 0623004^2 + 1228000^2 = \mathbf{1} 376996^2 \\
& \mathbf{12} 0623004^2 + 13508000^2 = \mathbf{121} 376996^2 \\
& \mathbf{1232} 0623004^2 + 136308000^2 = \mathbf{12321} 376996^2 \\
& \mathbf{123432} 0623004^2 + 1364308000^2 = \mathbf{1234321} 376996^2 \quad (5.614) \\
& \\
& 0621775^2 + 1230000^2 = \mathbf{1} 378225^2 \\
& \mathbf{12} 0621775^2 + 13530000^2 = \mathbf{121} 378225^2 \\
& \mathbf{1232} 0621775^2 + 136530000^2 = \mathbf{12321} 378225^2 \\
& \mathbf{123432} 0621775^2 + 1366530000^2 = \mathbf{1234321} 378225^2 \quad (5.615) \\
& \\
& 0620544^2 + 1232000^2 = \mathbf{1} 379456^2 \\
& \mathbf{12} 0620544^2 + 13552000^2 = \mathbf{121} 379456^2 \\
& \mathbf{1232} 0620544^2 + 136752000^2 = \mathbf{12321} 379456^2 \\
& \mathbf{123432} 0620544^2 + 1368752000^2 = \mathbf{1234321} 379456^2 \quad (5.616) \\
& \\
& 0619311^2 + 1234000^2 = \mathbf{1} 380689^2 \\
& \mathbf{12} 0619311^2 + 13574000^2 = \mathbf{121} 380689^2 \\
& \mathbf{1232} 0619311^2 + 136974000^2 = \mathbf{12321} 380689^2 \\
& \mathbf{123432} 0619311^2 + 1370974000^2 = \mathbf{1234321} 380689^2 \quad (5.617) \\
& \\
& 0618076^2 + 1236000^2 = \mathbf{1} 381924^2 \\
& \mathbf{12} 0618076^2 + 13596000^2 = \mathbf{121} 381924^2 \\
& \mathbf{1232} 0618076^2 + 137196000^2 = \mathbf{12321} 381924^2 \\
& \mathbf{123432} 0618076^2 + 1373196000^2 = \mathbf{1234321} 381924^2 \quad (5.618) \\
& \\
& 0616839^2 + 1238000^2 = \mathbf{1} 383161^2 \\
& \mathbf{12} 0616839^2 + 13618000^2 = \mathbf{121} 383161^2 \\
& \mathbf{1232} 0616839^2 + 137418000^2 = \mathbf{12321} 383161^2 \\
& \mathbf{123432} 0616839^2 + 1375418000^2 = \mathbf{1234321} 383161^2 \quad (5.619) \\
& \\
& 0615600^2 + 1240000^2 = \mathbf{1} 384400^2 \\
& \mathbf{12} 0615600^2 + 13640000^2 = \mathbf{121} 384400^2 \\
& \mathbf{1232} 0615600^2 + 137640000^2 = \mathbf{12321} 384400^2 \\
& \mathbf{123432} 0615600^2 + 1377640000^2 = \mathbf{1234321} 384400^2 \quad (5.620) \\
& \\
& 0614359^2 + 1242000^2 = \mathbf{1} 385641^2 \\
& \mathbf{12} 0614359^2 + 13662000^2 = \mathbf{121} 385641^2 \\
& \mathbf{1232} 0614359^2 + 137862000^2 = \mathbf{12321} 385641^2 \\
& \mathbf{123432} 0614359^2 + 1379862000^2 = \mathbf{1234321} 385641^2 \quad (5.621) \\
& \\
& 0613116^2 + 1244000^2 = \mathbf{1} 386884^2 \\
& \mathbf{12} 0613116^2 + 13684000^2 = \mathbf{121} 386884^2 \\
& \mathbf{1232} 0613116^2 + 138084000^2 = \mathbf{12321} 386884^2 \\
& \mathbf{123432} 0613116^2 + 1382084000^2 = \mathbf{1234321} 386884^2 \quad (5.622) \\
& \\
& 0611871^2 + 1246000^2 = \mathbf{1} 388129^2 \\
& \mathbf{12} 0611871^2 + 13706000^2 = \mathbf{121} 388129^2 \\
& \mathbf{1232} 0611871^2 + 138306000^2 = \mathbf{12321} 388129^2 \\
& \mathbf{123432} 0611871^2 + 1384306000^2 = \mathbf{1234321} 388129^2 \quad (5.623) \\
& \\
& 0610624^2 + 1248000^2 = \mathbf{1} 389376^2 \\
& \mathbf{12} 0610624^2 + 13728000^2 = \mathbf{121} 389376^2 \\
& \mathbf{1232} 0610624^2 + 138528000^2 = \mathbf{12321} 389376^2 \\
& \mathbf{123432} 0610624^2 + 1386528000^2 = \mathbf{1234321} 389376^2 \quad (5.624) \\
& \\
& 0609375^2 + 1250000^2 = \mathbf{1} 390625^2 \\
& \mathbf{12} 0609375^2 + 13750000^2 = \mathbf{121} 390625^2 \\
& \mathbf{1232} 0609375^2 + 138750000^2 = \mathbf{12321} 390625^2 \\
& \mathbf{123432} 0609375^2 + 1388750000^2 = \mathbf{1234321} 390625^2 \quad (5.625) \\
& \\
& 0608124^2 + 1252000^2 = \mathbf{1} 391876^2 \\
& \mathbf{12} 0608124^2 + 13772000^2 = \mathbf{121} 391876^2 \\
& \mathbf{1232} 0608124^2 + 138972000^2 = \mathbf{12321} 391876^2 \\
& \mathbf{123432} 0608124^2 + 1390972000^2 = \mathbf{1234321} 391876^2 \quad (5.626) \\
& \\
& 0606871^2 + 1254000^2 = \mathbf{1} 393129^2 \\
& \mathbf{12} 0606871^2 + 13794000^2 = \mathbf{121} 393129^2 \\
& \mathbf{1232} 0606871^2 + 139194000^2 = \mathbf{12321} 393129^2 \\
& \mathbf{123432} 0606871^2 + 1393194000^2 = \mathbf{1234321} 393129^2 \quad (5.627) \\
& \\
& 0605616^2 + 1256000^2 = \mathbf{1} 394384^2 \\
& \mathbf{12} 0605616^2 + 13816000^2 = \mathbf{121} 394384^2 \\
& \mathbf{1232} 0605616^2 + 139416000^2 = \mathbf{12321} 394384^2 \\
& \mathbf{123432} 0605616^2 + 1395416000^2 = \mathbf{1234321} 394384^2 \quad (5.628) \\
& \\
& 0604359^2 + 1258000^2 = \mathbf{1} 395641^2 \\
& \mathbf{12} 0604359^2 + 13838000^2 = \mathbf{121} 395641^2 \\
& \mathbf{1232} 0604359^2 + 139638000^2 = \mathbf{12321} 395641^2 \\
& \mathbf{123432} 0604359^2 + 1397638000^2 = \mathbf{1234321} 395641^2 \quad (5.629) \\
& \\
& 0603100^2 + 1260000^2 = \mathbf{1} 396900^2 \\
& \mathbf{12} 0603100^2 + 13860000^2 = \mathbf{121} 396900^2 \\
& \mathbf{1232} 0603100^2 + 139860000^2 = \mathbf{12321} 396900^2 \\
& \mathbf{123432} 0603100^2 + 1399860000^2 = \mathbf{1234321} 396900^2 \quad (5.630)
\end{aligned}$$

$$\begin{aligned}
& 0601839^2 + 1262000^2 = \mathbf{1} 398161^2 \\
& \mathbf{12} 0601839^2 + 13882000^2 = \mathbf{121} 398161^2 \\
& \mathbf{1232} 0601839^2 + 140082000^2 = \mathbf{12321} 398161^2 \\
& \mathbf{123432} 0601839^2 + 1402082000^2 = \mathbf{1234321} 398161^2 \quad (5.631) \\
& \\
& 0600576^2 + 1264000^2 = \mathbf{1} 399424^2 \\
& \mathbf{12} 0600576^2 + 13904000^2 = \mathbf{121} 399424^2 \\
& \mathbf{1232} 0600576^2 + 140304000^2 = \mathbf{12321} 399424^2 \\
& \mathbf{123432} 0600576^2 + 1404304000^2 = \mathbf{1234321} 399424^2 \quad (5.632) \\
& \\
& 0599311^2 + 1266000^2 = \mathbf{1} 400689^2 \\
& \mathbf{12} 0599311^2 + 13926000^2 = \mathbf{121} 400689^2 \\
& \mathbf{1232} 0599311^2 + 140526000^2 = \mathbf{12321} 400689^2 \\
& \mathbf{123432} 0599311^2 + 1406526000^2 = \mathbf{1234321} 400689^2 \quad (5.633) \\
& \\
& 0598044^2 + 1268000^2 = \mathbf{1} 401956^2 \\
& \mathbf{12} 0598044^2 + 13948000^2 = \mathbf{121} 401956^2 \\
& \mathbf{1232} 0598044^2 + 140748000^2 = \mathbf{12321} 401956^2 \\
& \mathbf{123432} 0598044^2 + 1408748000^2 = \mathbf{1234321} 401956^2 \quad (5.634) \\
& \\
& 0596775^2 + 1270000^2 = \mathbf{1} 403225^2 \\
& \mathbf{12} 0596775^2 + 13970000^2 = \mathbf{121} 403225^2 \\
& \mathbf{1232} 0596775^2 + 140970000^2 = \mathbf{12321} 403225^2 \\
& \mathbf{123432} 0596775^2 + 1410970000^2 = \mathbf{1234321} 403225^2 \quad (5.635) \\
& \\
& 0595504^2 + 1272000^2 = \mathbf{1} 404496^2 \\
& \mathbf{12} 0595504^2 + 13992000^2 = \mathbf{121} 404496^2 \\
& \mathbf{1232} 0595504^2 + 141192000^2 = \mathbf{12321} 404496^2 \\
& \mathbf{123432} 0595504^2 + 1413192000^2 = \mathbf{1234321} 404496^2 \quad (5.636) \\
& \\
& 0594231^2 + 1274000^2 = \mathbf{1} 405769^2 \\
& \mathbf{12} 0594231^2 + 14014000^2 = \mathbf{121} 405769^2 \\
& \mathbf{1232} 0594231^2 + 141414000^2 = \mathbf{12321} 405769^2 \\
& \mathbf{123432} 0594231^2 + 1415414000^2 = \mathbf{1234321} 405769^2 \quad (5.637) \\
& \\
& 0592956^2 + 1276000^2 = \mathbf{1} 407044^2 \\
& \mathbf{12} 0592956^2 + 14036000^2 = \mathbf{121} 407044^2 \\
& \mathbf{1232} 0592956^2 + 141636000^2 = \mathbf{12321} 407044^2 \\
& \mathbf{123432} 0592956^2 + 1417636000^2 = \mathbf{1234321} 407044^2 \quad (5.638) \\
& \\
& 0591679^2 + 1278000^2 = \mathbf{1} 408321^2 \\
& \mathbf{12} 0591679^2 + 14058000^2 = \mathbf{121} 408321^2 \\
& \mathbf{1232} 0591679^2 + 141858000^2 = \mathbf{12321} 408321^2 \\
& \mathbf{123432} 0591679^2 + 1419858000^2 = \mathbf{1234321} 408321^2 \quad (5.639)
\end{aligned}$$

$$\begin{aligned}
& 0580096^2 + 1296000^2 = \mathbf{1} 419904^2 \\
& \mathbf{12} 0580096^2 + 14256000^2 = \mathbf{121} 419904^2 \\
& \mathbf{1232} 0580096^2 + 143856000^2 = \mathbf{12321} 419904^2 \\
& \mathbf{123432} 0580096^2 + 1439856000^2 = \mathbf{1234321} 419904^2 \quad (5.648) \\
& \\
& 0578799^2 + 1298000^2 = \mathbf{1} 421201^2 \\
& \mathbf{12} 0578799^2 + 14278000^2 = \mathbf{121} 421201^2 \\
& \mathbf{1232} 0578799^2 + 144078000^2 = \mathbf{12321} 421201^2 \\
& \mathbf{123432} 0578799^2 + 1442078000^2 = \mathbf{1234321} 421201^2 \quad (5.649) \\
& \\
& 0577500^2 + 1300000^2 = \mathbf{1} 422500^2 \\
& \mathbf{12} 0577500^2 + 14300000^2 = \mathbf{121} 422500^2 \\
& \mathbf{1232} 0577500^2 + 144300000^2 = \mathbf{12321} 422500^2 \\
& \mathbf{123432} 0577500^2 + 1444300000^2 = \mathbf{1234321} 422500^2 \quad (5.650) \\
& \\
& 0576199^2 + 1302000^2 = \mathbf{1} 423801^2 \\
& \mathbf{12} 0576199^2 + 14322000^2 = \mathbf{121} 423801^2 \\
& \mathbf{1232} 0576199^2 + 144522000^2 = \mathbf{12321} 423801^2 \\
& \mathbf{123432} 0576199^2 + 1446522000^2 = \mathbf{1234321} 423801^2 \quad (5.651) \\
& \\
& 0574896^2 + 1304000^2 = \mathbf{1} 425104^2 \\
& \mathbf{12} 0574896^2 + 14344000^2 = \mathbf{121} 425104^2 \\
& \mathbf{1232} 0574896^2 + 144744000^2 = \mathbf{12321} 425104^2 \\
& \mathbf{123432} 0574896^2 + 1448744000^2 = \mathbf{1234321} 425104^2 \quad (5.652) \\
& \\
& 0573591^2 + 1306000^2 = \mathbf{1} 426409^2 \\
& \mathbf{12} 0573591^2 + 14366000^2 = \mathbf{121} 426409^2 \\
& \mathbf{1232} 0573591^2 + 144966000^2 = \mathbf{12321} 426409^2 \\
& \mathbf{123432} 0573591^2 + 1450966000^2 = \mathbf{1234321} 426409^2 \quad (5.653) \\
& \\
& 0572284^2 + 1308000^2 = \mathbf{1} 427716^2 \\
& \mathbf{12} 0572284^2 + 14388000^2 = \mathbf{121} 427716^2 \\
& \mathbf{1232} 0572284^2 + 145188000^2 = \mathbf{12321} 427716^2 \\
& \mathbf{123432} 0572284^2 + 1453188000^2 = \mathbf{1234321} 427716^2 \quad (5.654) \\
& \\
& 0570975^2 + 1310000^2 = \mathbf{1} 429025^2 \\
& \mathbf{12} 0570975^2 + 14410000^2 = \mathbf{121} 429025^2 \\
& \mathbf{1232} 0570975^2 + 145410000^2 = \mathbf{12321} 429025^2 \\
& \mathbf{123432} 0570975^2 + 1455410000^2 = \mathbf{1234321} 429025^2 \quad (5.655) \\
& \\
& 0569664^2 + 1312000^2 = \mathbf{1} 430336^2 \\
& \mathbf{12} 0569664^2 + 14432000^2 = \mathbf{121} 430336^2 \\
& \mathbf{1232} 0569664^2 + 145632000^2 = \mathbf{12321} 430336^2 \\
& \mathbf{123432} 0569664^2 + 1457632000^2 = \mathbf{1234321} 430336^2 \quad (5.656) \\
& \\
& 0568351^2 + 1314000^2 = \mathbf{1} 431649^2 \\
& \mathbf{12} 0568351^2 + 14454000^2 = \mathbf{121} 431649^2 \\
& \mathbf{1232} 0568351^2 + 145854000^2 = \mathbf{12321} 431649^2 \\
& \mathbf{123432} 0568351^2 + 1459854000^2 = \mathbf{1234321} 431649^2 \quad (5.657) \\
& \\
& 0567036^2 + 1316000^2 = \mathbf{1} 432964^2 \\
& \mathbf{12} 0567036^2 + 14476000^2 = \mathbf{121} 432964^2 \\
& \mathbf{1232} 0567036^2 + 146076000^2 = \mathbf{12321} 432964^2 \\
& \mathbf{123432} 0567036^2 + 1462076000^2 = \mathbf{1234321} 432964^2 \quad (5.658) \\
& \\
& 0565719^2 + 1318000^2 = \mathbf{1} 434281^2 \\
& \mathbf{12} 0565719^2 + 14498000^2 = \mathbf{121} 434281^2 \\
& \mathbf{1232} 0565719^2 + 146298000^2 = \mathbf{12321} 434281^2 \\
& \mathbf{123432} 0565719^2 + 1464298000^2 = \mathbf{1234321} 434281^2 \quad (5.659) \\
& \\
& 0564400^2 + 1320000^2 = \mathbf{1} 435600^2 \\
& \mathbf{12} 0564400^2 + 14520000^2 = \mathbf{121} 435600^2 \\
& \mathbf{1232} 0564400^2 + 146520000^2 = \mathbf{12321} 435600^2 \\
& \mathbf{123432} 0564400^2 + 1466520000^2 = \mathbf{1234321} 435600^2 \quad (5.660) \\
& \\
& 0563079^2 + 1322000^2 = \mathbf{1} 436921^2 \\
& \mathbf{12} 0563079^2 + 14542000^2 = \mathbf{121} 436921^2 \\
& \mathbf{1232} 0563079^2 + 146742000^2 = \mathbf{12321} 436921^2 \\
& \mathbf{123432} 0563079^2 + 1468742000^2 = \mathbf{1234321} 436921^2 \quad (5.661) \\
& \\
& 0561756^2 + 1324000^2 = \mathbf{1} 438244^2 \\
& \mathbf{12} 0561756^2 + 14564000^2 = \mathbf{121} 438244^2 \\
& \mathbf{1232} 0561756^2 + 146964000^2 = \mathbf{12321} 438244^2 \\
& \mathbf{123432} 0561756^2 + 1470964000^2 = \mathbf{1234321} 438244^2 \quad (5.662) \\
& \\
& 0560431^2 + 1326000^2 = \mathbf{1} 439569^2 \\
& \mathbf{12} 0560431^2 + 14586000^2 = \mathbf{121} 439569^2 \\
& \mathbf{1232} 0560431^2 + 147186000^2 = \mathbf{12321} 439569^2 \\
& \mathbf{123432} 0560431^2 + 1473186000^2 = \mathbf{1234321} 439569^2 \quad (5.663) \\
& \\
& 0559104^2 + 1328000^2 = \mathbf{1} 440896^2 \\
& \mathbf{12} 0559104^2 + 14608000^2 = \mathbf{121} 440896^2 \\
& \mathbf{1232} 0559104^2 + 147408000^2 = \mathbf{12321} 440896^2 \\
& \mathbf{123432} 0559104^2 + 1475408000^2 = \mathbf{1234321} 440896^2 \quad (5.664)
\end{aligned}$$

$$\begin{aligned}
& 0557775^2 + 1330000^2 = \mathbf{1} 442225^2 \\
& \mathbf{12} 0557775^2 + 14630000^2 = \mathbf{121} 442225^2 \\
& \mathbf{1232} 0557775^2 + 147630000^2 = \mathbf{12321} 442225^2 \\
& \mathbf{123432} 0557775^2 + 1477630000^2 = \mathbf{1234321} 442225^2 \quad (5.665) \\
& \\
& 0556444^2 + 1332000^2 = \mathbf{1} 443556^2 \\
& \mathbf{12} 0556444^2 + 14652000^2 = \mathbf{121} 443556^2 \\
& \mathbf{1232} 0556444^2 + 147852000^2 = \mathbf{12321} 443556^2 \\
& \mathbf{123432} 0556444^2 + 1479852000^2 = \mathbf{1234321} 443556^2 \quad (5.666) \\
& \\
& 0555111^2 + 1334000^2 = \mathbf{1} 444889^2 \\
& \mathbf{12} 0555111^2 + 14674000^2 = \mathbf{121} 444889^2 \\
& \mathbf{1232} 0555111^2 + 148074000^2 = \mathbf{12321} 444889^2 \\
& \mathbf{123432} 0555111^2 + 1482074000^2 = \mathbf{1234321} 444889^2 \quad (5.667) \\
& \\
& 0553776^2 + 1336000^2 = \mathbf{1} 446224^2 \\
& \mathbf{12} 0553776^2 + 14696000^2 = \mathbf{121} 446224^2 \\
& \mathbf{1232} 0553776^2 + 148296000^2 = \mathbf{12321} 446224^2 \\
& \mathbf{123432} 0553776^2 + 1484296000^2 = \mathbf{1234321} 446224^2 \quad (5.668) \\
& \\
& 0552439^2 + 1338000^2 = \mathbf{1} 447561^2 \\
& \mathbf{12} 0552439^2 + 14718000^2 = \mathbf{121} 447561^2 \\
& \mathbf{1232} 0552439^2 + 148518000^2 = \mathbf{12321} 447561^2 \\
& \mathbf{123432} 0552439^2 + 1486518000^2 = \mathbf{1234321} 447561^2 \quad (5.669) \\
& \\
& 0551100^2 + 1340000^2 = \mathbf{1} 448900^2 \\
& \mathbf{12} 0551100^2 + 14740000^2 = \mathbf{121} 448900^2 \\
& \mathbf{1232} 0551100^2 + 148740000^2 = \mathbf{12321} 448900^2 \\
& \mathbf{123432} 0551100^2 + 1488740000^2 = \mathbf{1234321} 448900^2 \quad (5.670) \\
& \\
& 0549759^2 + 1342000^2 = \mathbf{1} 450241^2 \\
& \mathbf{12} 0549759^2 + 14762000^2 = \mathbf{121} 450241^2 \\
& \mathbf{1232} 0549759^2 + 148962000^2 = \mathbf{12321} 450241^2 \\
& \mathbf{123432} 0549759^2 + 1490962000^2 = \mathbf{1234321} 450241^2 \quad (5.671) \\
& \\
& 0548416^2 + 1344000^2 = \mathbf{1} 451584^2 \\
& \mathbf{12} 0548416^2 + 14784000^2 = \mathbf{121} 451584^2 \\
& \mathbf{1232} 0548416^2 + 149184000^2 = \mathbf{12321} 451584^2 \\
& \mathbf{123432} 0548416^2 + 1493184000^2 = \mathbf{1234321} 451584^2 \quad (5.672) \\
& \\
& 0547071^2 + 1346000^2 = \mathbf{1} 452929^2 \\
& \mathbf{12} 0547071^2 + 14806000^2 = \mathbf{121} 452929^2 \\
& \mathbf{1232} 0547071^2 + 149406000^2 = \mathbf{12321} 452929^2 \\
& \mathbf{123432} 0547071^2 + 1495406000^2 = \mathbf{1234321} 452929^2 \quad (5.673) \\
& \\
& 0545724^2 + 1348000^2 = \mathbf{1} 454276^2 \\
& \mathbf{12} 0545724^2 + 14828000^2 = \mathbf{121} 454276^2 \\
& \mathbf{1232} 0545724^2 + 149628000^2 = \mathbf{12321} 454276^2 \\
& \mathbf{123432} 0545724^2 + 1497628000^2 = \mathbf{1234321} 454276^2 \quad (5.674) \\
& \\
& 0544375^2 + 1350000^2 = \mathbf{1} 455625^2 \\
& \mathbf{12} 0544375^2 + 14850000^2 = \mathbf{121} 455625^2 \\
& \mathbf{1232} 0544375^2 + 149850000^2 = \mathbf{12321} 455625^2 \\
& \mathbf{123432} 0544375^2 + 1499850000^2 = \mathbf{1234321} 455625^2 \quad (5.675) \\
& \\
& 0543024^2 + 1352000^2 = \mathbf{1} 456976^2 \\
& \mathbf{12} 0543024^2 + 14872000^2 = \mathbf{121} 456976^2 \\
& \mathbf{1232} 0543024^2 + 150072000^2 = \mathbf{12321} 456976^2 \\
& \mathbf{123432} 0543024^2 + 1502072000^2 = \mathbf{1234321} 456976^2 \quad (5.676) \\
& \\
& 0541671^2 + 1354000^2 = \mathbf{1} 458329^2 \\
& \mathbf{12} 0541671^2 + 14894000^2 = \mathbf{121} 458329^2 \\
& \mathbf{1232} 0541671^2 + 150294000^2 = \mathbf{12321} 458329^2 \\
& \mathbf{123432} 0541671^2 + 1504294000^2 = \mathbf{1234321} 458329^2 \quad (5.677) \\
& \\
& 0540316^2 + 1356000^2 = \mathbf{1} 459684^2 \\
& \mathbf{12} 0540316^2 + 14916000^2 = \mathbf{121} 459684^2 \\
& \mathbf{1232} 0540316^2 + 150516000^2 = \mathbf{12321} 459684^2 \\
& \mathbf{123432} 0540316^2 + 1506516000^2 = \mathbf{1234321} 459684^2 \quad (5.678) \\
& \\
& 0538959^2 + 1358000^2 = \mathbf{1} 461041^2 \\
& \mathbf{12} 0538959^2 + 14938000^2 = \mathbf{121} 461041^2 \\
& \mathbf{1232} 0538959^2 + 150738000^2 = \mathbf{12321} 461041^2 \\
& \mathbf{123432} 0538959^2 + 1508738000^2 = \mathbf{1234321} 461041^2 \quad (5.679) \\
& \\
& 0537600^2 + 1360000^2 = \mathbf{1} 462400^2 \\
& \mathbf{12} 0537600^2 + 14960000^2 = \mathbf{121} 462400^2 \\
& \mathbf{1232} 0537600^2 + 150960000^2 = \mathbf{12321} 462400^2 \\
& \mathbf{123432} 0537600^2 + 1510960000^2 = \mathbf{1234321} 462400^2 \quad (5.680) \\
& \\
& 0536239^2 + 1362000^2 = \mathbf{1} 463761^2 \\
& \mathbf{12} 0536239^2 + 14982000^2 = \mathbf{121} 463761^2 \\
& \mathbf{1232} 0536239^2 + 151182000^2 = \mathbf{12321} 463761^2 \\
& \mathbf{123432} 0536239^2 + 1513182000^2 = \mathbf{1234321} 463761^2 \quad (5.681)
\end{aligned}$$

$0534876^2 + 1364000^2 = \mathbf{1} 465124^2$	$0522519^2 + 1382000^2 = \mathbf{1} 477481^2$
$12 0534876^2 + 15004000^2 = \mathbf{121} 465124^2$	$12 0522519^2 + 15202000^2 = \mathbf{121} 477481^2$
$1232 0534876^2 + 151404000^2 = \mathbf{12321} 465124^2$	$1232 0522519^2 + 153402000^2 = \mathbf{12321} 477481^2$
$123432 0534876^2 + 1515404000^2 = \mathbf{1234321} 465124^2 \quad (5.682)$	$123432 0522519^2 + 1535402000^2 = \mathbf{1234321} 477481^2 \quad (5.691)$
$0533511^2 + 1366000^2 = \mathbf{1} 466489^2$	$0521136^2 + 1384000^2 = \mathbf{1} 478864^2$
$12 0533511^2 + 15026000^2 = \mathbf{121} 466489^2$	$12 0521136^2 + 15224000^2 = \mathbf{121} 478864^2$
$1232 0533511^2 + 151626000^2 = \mathbf{12321} 466489^2$	$1232 0521136^2 + 153624000^2 = \mathbf{12321} 478864^2$
$123432 0533511^2 + 1517626000^2 = \mathbf{1234321} 466489^2 \quad (5.683)$	$123432 0521136^2 + 1537624000^2 = \mathbf{1234321} 478864^2 \quad (5.692)$
$0532144^2 + 1368000^2 = \mathbf{1} 467856^2$	$0519751^2 + 1386000^2 = \mathbf{1} 480249^2$
$12 0532144^2 + 15048000^2 = \mathbf{121} 467856^2$	$12 0519751^2 + 15246000^2 = \mathbf{121} 480249^2$
$1232 0532144^2 + 151848000^2 = \mathbf{12321} 467856^2$	$1232 0519751^2 + 153846000^2 = \mathbf{12321} 480249^2$
$123432 0532144^2 + 1519848000^2 = \mathbf{1234321} 467856^2 \quad (5.684)$	$123432 0519751^2 + 1539846000^2 = \mathbf{1234321} 480249^2 \quad (5.693)$
$0530775^2 + 1370000^2 = \mathbf{1} 469225^2$	$0518364^2 + 1388000^2 = \mathbf{1} 481636^2$
$12 0530775^2 + 15070000^2 = \mathbf{121} 469225^2$	$12 0518364^2 + 15268000^2 = \mathbf{121} 481636^2$
$1232 0530775^2 + 152070000^2 = \mathbf{12321} 469225^2$	$1232 0518364^2 + 154068000^2 = \mathbf{12321} 481636^2$
$123432 0530775^2 + 1522070000^2 = \mathbf{1234321} 469225^2 \quad (5.685)$	$123432 0518364^2 + 1542068000^2 = \mathbf{1234321} 481636^2 \quad (5.694)$
$0529404^2 + 1372000^2 = \mathbf{1} 470596^2$	$0516975^2 + 1390000^2 = \mathbf{1} 483025^2$
$12 0529404^2 + 15092000^2 = \mathbf{121} 470596^2$	$12 0516975^2 + 15290000^2 = \mathbf{121} 483025^2$
$1232 0529404^2 + 152292000^2 = \mathbf{12321} 470596^2$	$1232 0516975^2 + 154290000^2 = \mathbf{12321} 483025^2$
$123432 0529404^2 + 1524292000^2 = \mathbf{1234321} 470596^2 \quad (5.686)$	$123432 0516975^2 + 1544290000^2 = \mathbf{1234321} 483025^2 \quad (5.695)$
$0528031^2 + 1374000^2 = \mathbf{1} 471969^2$	$0515584^2 + 1392000^2 = \mathbf{1} 484416^2$
$12 0528031^2 + 15114000^2 = \mathbf{121} 471969^2$	$12 0515584^2 + 15312000^2 = \mathbf{121} 484416^2$
$1232 0528031^2 + 152514000^2 = \mathbf{12321} 471969^2$	$1232 0515584^2 + 154512000^2 = \mathbf{12321} 484416^2$
$123432 0528031^2 + 1526514000^2 = \mathbf{1234321} 471969^2 \quad (5.687)$	$123432 0515584^2 + 1546512000^2 = \mathbf{1234321} 484416^2 \quad (5.696)$
$0526656^2 + 1376000^2 = \mathbf{1} 473344^2$	$0514191^2 + 1394000^2 = \mathbf{1} 485809^2$
$12 0526656^2 + 15136000^2 = \mathbf{121} 473344^2$	$12 0514191^2 + 15334000^2 = \mathbf{121} 485809^2$
$1232 0526656^2 + 152736000^2 = \mathbf{12321} 473344^2$	$1232 0514191^2 + 154734000^2 = \mathbf{12321} 485809^2$
$123432 0526656^2 + 1528736000^2 = \mathbf{1234321} 473344^2 \quad (5.688)$	$123432 0514191^2 + 1548734000^2 = \mathbf{1234321} 485809^2 \quad (5.697)$
$0525279^2 + 1378000^2 = \mathbf{1} 474721^2$	$0512796^2 + 1396000^2 = \mathbf{1} 487204^2$
$12 0525279^2 + 15158000^2 = \mathbf{121} 474721^2$	$12 0512796^2 + 15356000^2 = \mathbf{121} 487204^2$
$1232 0525279^2 + 152958000^2 = \mathbf{12321} 474721^2$	$1232 0512796^2 + 154956000^2 = \mathbf{12321} 487204^2$
$123432 0525279^2 + 1530958000^2 = \mathbf{1234321} 474721^2 \quad (5.689)$	$123432 0512796^2 + 1550956000^2 = \mathbf{1234321} 487204^2 \quad (5.698)$
$0523900^2 + 1380000^2 = \mathbf{1} 476100^2$	$0511399^2 + 1398000^2 = \mathbf{1} 488601^2$
$12 0523900^2 + 15180000^2 = \mathbf{121} 476100^2$	$12 0511399^2 + 15378000^2 = \mathbf{121} 488601^2$
$1232 0523900^2 + 153180000^2 = \mathbf{12321} 476100^2$	$1232 0511399^2 + 155178000^2 = \mathbf{12321} 488601^2$
$123432 0523900^2 + 1533180000^2 = \mathbf{1234321} 476100^2 \quad (5.690)$	$123432 0511399^2 + 1553178000^2 = \mathbf{1234321} 488601^2 \quad (5.699)$

5.8 For $n = 700, 701, 701, \dots, 797, 798, 799$:

Let's consider

$$m = 1000, 11000, 111000, 1111000, 11111000, 111111000, 1111111000, 11111111000$$

in (1.1), then for each value of $n = 700, 701, 701, \dots, 797, 798, 799$; there are 100 *palindromic-type pandigital Pythagorean patterns* given below. In each case, only first four values are written. The other 5 values can be written on similar lines as done in subsection 5.1.1.

$0510000^2 + 1400000^2 = 1490000^2$	$0500151^2 + 1414000^2 = 1499849^2$
$120510000^2 + 15400000^2 = 121490000^2$	$120500151^2 + 15554000^2 = 121499849^2$
$12320510000^2 + 155400000^2 = 12321490000^2$	$12320500151^2 + 156954000^2 = 12321499849^2$
$1234320510000^2 + 1555400000^2 = 1234321490000^2$ (5.700)	$1234320500151^2 + 1570954000^2 = 1234321499849^2$ (5.707)
$0508599^2 + 1402000^2 = 1491401^2$	$0498736^2 + 1416000^2 = 1501264^2$
$120508599^2 + 15422000^2 = 121491401^2$	$120498736^2 + 15576000^2 = 121501264^2$
$12320508599^2 + 155622000^2 = 12321491401^2$	$12320498736^2 + 157176000^2 = 12321501264^2$
$1234320508599^2 + 1557622000^2 = 1234321491401^2$ (5.701)	$1234320498736^2 + 1573176000^2 = 1234321501264^2$ (5.708)
$0507196^2 + 1404000^2 = 1492804^2$	$0497319^2 + 1418000^2 = 1502681^2$
$120507196^2 + 15444000^2 = 121492804^2$	$120497319^2 + 15598000^2 = 121502681^2$
$12320507196^2 + 155844000^2 = 12321492804^2$	$12320497319^2 + 157398000^2 = 12321502681^2$
$1234320507196^2 + 1559844000^2 = 1234321492804^2$ (5.702)	$1234320497319^2 + 1575398000^2 = 1234321502681^2$ (5.709)
$0505791^2 + 1406000^2 = 1494209^2$	$0495900^2 + 1420000^2 = 1504100^2$
$120505791^2 + 15466000^2 = 121494209^2$	$120495900^2 + 15620000^2 = 121504100^2$
$12320505791^2 + 156066000^2 = 12321494209^2$	$12320495900^2 + 157620000^2 = 12321504100^2$
$1234320505791^2 + 1562066000^2 = 1234321494209^2$ (5.703)	$1234320495900^2 + 1577620000^2 = 1234321504100^2$ (5.710)
$0504384^2 + 1408000^2 = 1495616^2$	$0494479^2 + 1422000^2 = 1505521^2$
$120504384^2 + 15488000^2 = 121495616^2$	$120494479^2 + 15642000^2 = 121505521^2$
$12320504384^2 + 156288000^2 = 12321495616^2$	$12320494479^2 + 157842000^2 = 12321505521^2$
$1234320504384^2 + 1564288000^2 = 1234321495616^2$ (5.704)	$1234320494479^2 + 1579842000^2 = 1234321505521^2$ (5.711)
$0502975^2 + 1410000^2 = 1497025^2$	$0493056^2 + 1424000^2 = 1506944^2$
$120502975^2 + 15510000^2 = 121497025^2$	$120493056^2 + 15664000^2 = 121506944^2$
$12320502975^2 + 156510000^2 = 12321497025^2$	$12320493056^2 + 158064000^2 = 12321506944^2$
$1234320502975^2 + 1566510000^2 = 1234321497025^2$ (5.705)	$1234320493056^2 + 1582064000^2 = 1234321506944^2$ (5.712)
$0501564^2 + 1412000^2 = 1498436^2$	$0491631^2 + 1426000^2 = 1508369^2$
$120501564^2 + 15532000^2 = 121498436^2$	$120491631^2 + 15686000^2 = 121508369^2$
$12320501564^2 + 156732000^2 = 12321498436^2$	$12320491631^2 + 158286000^2 = 12321508369^2$
$1234320501564^2 + 1568732000^2 = 1234321498436^2$ (5.706)	$1234320491631^2 + 1584286000^2 = 1234321508369^2$ (5.713)

$0490204^2 + 1428000^2 = \textcolor{red}{1} 509796^2$	$0477271^2 + 1446000^2 = \textcolor{red}{1} 522729^2$
$12 0490204^2 + 15708000^2 = \textcolor{red}{121} 509796^2$	$12 0477271^2 + 15906000^2 = \textcolor{red}{121} 522729^2$
$1232 0490204^2 + 158508000^2 = \textcolor{red}{12321} 509796^2$	$1232 0477271^2 + 160506000^2 = \textcolor{red}{12321} 522729^2$
$123432 0490204^2 + 1586508000^2 = \textcolor{red}{1234321} 509796^2 \quad (5.714)$	$123432 0477271^2 + 1606506000^2 = \textcolor{red}{1234321} 522729^2 \quad (5.723)$
$0488775^2 + 1430000^2 = \textcolor{red}{1} 511225^2$	$0475824^2 + 1448000^2 = \textcolor{red}{1} 524176^2$
$12 0488775^2 + 15730000^2 = \textcolor{red}{121} 511225^2$	$12 0475824^2 + 15928000^2 = \textcolor{red}{121} 524176^2$
$1232 0488775^2 + 158730000^2 = \textcolor{red}{12321} 511225^2$	$1232 0475824^2 + 160728000^2 = \textcolor{red}{12321} 524176^2$
$123432 0488775^2 + 1588730000^2 = \textcolor{red}{1234321} 511225^2 \quad (5.715)$	$123432 0475824^2 + 1608728000^2 = \textcolor{red}{1234321} 524176^2 \quad (5.724)$
$0487344^2 + 1432000^2 = \textcolor{red}{1} 512656^2$	$0474375^2 + 1450000^2 = \textcolor{red}{1} 525625^2$
$12 0487344^2 + 15752000^2 = \textcolor{red}{121} 512656^2$	$12 0474375^2 + 15950000^2 = \textcolor{red}{121} 525625^2$
$1232 0487344^2 + 158952000^2 = \textcolor{red}{12321} 512656^2$	$1232 0474375^2 + 160950000^2 = \textcolor{red}{12321} 525625^2$
$123432 0487344^2 + 1590952000^2 = \textcolor{red}{1234321} 512656^2 \quad (5.716)$	$123432 0474375^2 + 1610950000^2 = \textcolor{red}{1234321} 525625^2 \quad (5.725)$
$0485911^2 + 1434000^2 = \textcolor{red}{1} 514089^2$	$0472924^2 + 1452000^2 = \textcolor{red}{1} 527076^2$
$12 0485911^2 + 15774000^2 = \textcolor{red}{121} 514089^2$	$12 0472924^2 + 15972000^2 = \textcolor{red}{121} 527076^2$
$1232 0485911^2 + 159174000^2 = \textcolor{red}{12321} 514089^2$	$1232 0472924^2 + 161172000^2 = \textcolor{red}{12321} 527076^2$
$123432 0485911^2 + 1593174000^2 = \textcolor{red}{1234321} 514089^2 \quad (5.717)$	$123432 0472924^2 + 1613172000^2 = \textcolor{red}{1234321} 527076^2 \quad (5.726)$
$0484476^2 + 1436000^2 = \textcolor{red}{1} 515524^2$	$0471471^2 + 1454000^2 = \textcolor{red}{1} 528529^2$
$12 0484476^2 + 15796000^2 = \textcolor{red}{121} 515524^2$	$12 0471471^2 + 15994000^2 = \textcolor{red}{121} 528529^2$
$1232 0484476^2 + 159396000^2 = \textcolor{red}{12321} 515524^2$	$1232 0471471^2 + 161394000^2 = \textcolor{red}{12321} 528529^2$
$123432 0484476^2 + 1595396000^2 = \textcolor{red}{1234321} 515524^2 \quad (5.718)$	$123432 0471471^2 + 1615394000^2 = \textcolor{red}{1234321} 528529^2 \quad (5.727)$
$0483039^2 + 1438000^2 = \textcolor{red}{1} 516961^2$	$0470016^2 + 1456000^2 = \textcolor{red}{1} 529984^2$
$12 0483039^2 + 15818000^2 = \textcolor{red}{121} 516961^2$	$12 0470016^2 + 16016000^2 = \textcolor{red}{121} 529984^2$
$1232 0483039^2 + 159618000^2 = \textcolor{red}{12321} 516961^2$	$1232 0470016^2 + 161616000^2 = \textcolor{red}{12321} 529984^2$
$123432 0483039^2 + 1597618000^2 = \textcolor{red}{1234321} 516961^2 \quad (5.719)$	$123432 0470016^2 + 1617616000^2 = \textcolor{red}{1234321} 529984^2 \quad (5.728)$
$0481600^2 + 1440000^2 = \textcolor{red}{1} 518400^2$	$0468559^2 + 1458000^2 = \textcolor{red}{1} 531441^2$
$12 0481600^2 + 15840000^2 = \textcolor{red}{121} 518400^2$	$12 0468559^2 + 16038000^2 = \textcolor{red}{121} 531441^2$
$1232 0481600^2 + 159840000^2 = \textcolor{red}{12321} 518400^2$	$1232 0468559^2 + 161838000^2 = \textcolor{red}{12321} 531441^2$
$123432 0481600^2 + 1599840000^2 = \textcolor{red}{1234321} 518400^2 \quad (5.720)$	$123432 0468559^2 + 1619838000^2 = \textcolor{red}{1234321} 531441^2 \quad (5.729)$
$0480159^2 + 1442000^2 = \textcolor{red}{1} 519841^2$	$0467100^2 + 1460000^2 = \textcolor{red}{1} 532900^2$
$12 0480159^2 + 15862000^2 = \textcolor{red}{121} 519841^2$	$12 0467100^2 + 16060000^2 = \textcolor{red}{121} 532900^2$
$1232 0480159^2 + 160062000^2 = \textcolor{red}{12321} 519841^2$	$1232 0467100^2 + 162060000^2 = \textcolor{red}{12321} 532900^2$
$123432 0480159^2 + 1602062000^2 = \textcolor{red}{1234321} 519841^2 \quad (5.721)$	$123432 0467100^2 + 1622060000^2 = \textcolor{red}{1234321} 532900^2 \quad (5.730)$
$0478716^2 + 1444000^2 = \textcolor{red}{1} 521284^2$	
$12 0478716^2 + 15884000^2 = \textcolor{red}{121} 521284^2$	
$1232 0478716^2 + 160284000^2 = \textcolor{red}{12321} 521284^2$	
$123432 0478716^2 + 1604284000^2 = \textcolor{red}{1234321} 521284^2 \quad (5.722)$	

$$\begin{aligned}
& 0465639^2 + 1462000^2 = \mathbf{1} \ 534361^2 \\
& \mathbf{12} \ 0465639^2 + 16082000^2 = \mathbf{121} \ 534361^2 \\
& \mathbf{1232} \ 0465639^2 + 162282000^2 = \mathbf{12321} \ 534361^2 \\
& \mathbf{123432} \ 0465639^2 + 1624282000^2 = \mathbf{1234321} \ 534361^2 \ (5.731) \\
& \\
& 0464176^2 + 1464000^2 = \mathbf{1} \ 535824^2 \\
& \mathbf{12} \ 0464176^2 + 16104000^2 = \mathbf{121} \ 535824^2 \\
& \mathbf{1232} \ 0464176^2 + 162504000^2 = \mathbf{12321} \ 535824^2 \\
& \mathbf{123432} \ 0464176^2 + 1626504000^2 = \mathbf{1234321} \ 535824^2 \ (5.732) \\
& \\
& 0462711^2 + 1466000^2 = \mathbf{1} \ 537289^2 \\
& \mathbf{12} \ 0462711^2 + 16126000^2 = \mathbf{121} \ 537289^2 \\
& \mathbf{1232} \ 0462711^2 + 162726000^2 = \mathbf{12321} \ 537289^2 \\
& \mathbf{123432} \ 0462711^2 + 1628726000^2 = \mathbf{1234321} \ 537289^2 \ (5.733) \\
& \\
& 0461244^2 + 1468000^2 = \mathbf{1} \ 538756^2 \\
& \mathbf{12} \ 0461244^2 + 16148000^2 = \mathbf{121} \ 538756^2 \\
& \mathbf{1232} \ 0461244^2 + 162948000^2 = \mathbf{12321} \ 538756^2 \\
& \mathbf{123432} \ 0461244^2 + 1630948000^2 = \mathbf{1234321} \ 538756^2 \ (5.734) \\
& \\
& 0459775^2 + 1470000^2 = \mathbf{1} \ 540225^2 \\
& \mathbf{12} \ 0459775^2 + 16170000^2 = \mathbf{121} \ 540225^2 \\
& \mathbf{1232} \ 0459775^2 + 163170000^2 = \mathbf{12321} \ 540225^2 \\
& \mathbf{123432} \ 0459775^2 + 1633170000^2 = \mathbf{1234321} \ 540225^2 \ (5.735) \\
& \\
& 0458304^2 + 1472000^2 = \mathbf{1} \ 541696^2 \\
& \mathbf{12} \ 0458304^2 + 16192000^2 = \mathbf{121} \ 541696^2 \\
& \mathbf{1232} \ 0458304^2 + 163392000^2 = \mathbf{12321} \ 541696^2 \\
& \mathbf{123432} \ 0458304^2 + 1635392000^2 = \mathbf{1234321} \ 541696^2 \ (5.736) \\
& \\
& 0456831^2 + 1474000^2 = \mathbf{1} \ 543169^2 \\
& \mathbf{12} \ 0456831^2 + 16214000^2 = \mathbf{121} \ 543169^2 \\
& \mathbf{1232} \ 0456831^2 + 163614000^2 = \mathbf{12321} \ 543169^2 \\
& \mathbf{123432} \ 0456831^2 + 1637614000^2 = \mathbf{1234321} \ 543169^2 \ (5.737) \\
& \\
& 0455356^2 + 1476000^2 = \mathbf{1} \ 544644^2 \\
& \mathbf{12} \ 0455356^2 + 16236000^2 = \mathbf{121} \ 544644^2 \\
& \mathbf{1232} \ 0455356^2 + 163836000^2 = \mathbf{12321} \ 544644^2 \\
& \mathbf{123432} \ 0455356^2 + 1639836000^2 = \mathbf{1234321} \ 544644^2 \ (5.738) \\
& \\
& 0453879^2 + 1478000^2 = \mathbf{1} \ 546121^2 \\
& \mathbf{12} \ 0453879^2 + 16258000^2 = \mathbf{121} \ 546121^2 \\
& \mathbf{1232} \ 0453879^2 + 164058000^2 = \mathbf{12321} \ 546121^2 \\
& \mathbf{123432} \ 0453879^2 + 1642058000^2 = \mathbf{1234321} \ 546121^2 \ (5.739)
\end{aligned}$$

$\begin{aligned} 0440496^2 + 1496000^2 &= \textcolor{red}{1} 559504^2 \\ \textcolor{blue}{12} 0440496^2 + 16456000^2 &= \textcolor{red}{121} 559504^2 \\ \textcolor{blue}{1232} 0440496^2 + 166056000^2 &= \textcolor{red}{12321} 559504^2 \\ \textcolor{blue}{123432} 0440496^2 + 1662056000^2 &= \textcolor{red}{1234321} 559504^2 \quad (5.748) \end{aligned}$ $\begin{aligned} 0438999^2 + 1498000^2 &= \textcolor{red}{1} 561001^2 \\ \textcolor{blue}{12} 0438999^2 + 16478000^2 &= \textcolor{red}{121} 561001^2 \\ \textcolor{blue}{1232} 0438999^2 + 166278000^2 &= \textcolor{red}{12321} 561001^2 \\ \textcolor{blue}{123432} 0438999^2 + 1664278000^2 &= \textcolor{red}{1234321} 561001^2 \quad (5.749) \end{aligned}$ $\begin{aligned} 0437500^2 + 1500000^2 &= \textcolor{red}{1} 562500^2 \\ \textcolor{blue}{12} 0437500^2 + 16500000^2 &= \textcolor{red}{121} 562500^2 \\ \textcolor{blue}{1232} 0437500^2 + 166500000^2 &= \textcolor{red}{12321} 562500^2 \\ \textcolor{blue}{123432} 0437500^2 + 1666500000^2 &= \textcolor{red}{1234321} 562500^2 \quad (5.750) \end{aligned}$ $\begin{aligned} 0435999^2 + 1502000^2 &= \textcolor{red}{1} 564001^2 \\ \textcolor{blue}{12} 0435999^2 + 16522000^2 &= \textcolor{red}{121} 564001^2 \\ \textcolor{blue}{1232} 0435999^2 + 166722000^2 &= \textcolor{red}{12321} 564001^2 \\ \textcolor{blue}{123432} 0435999^2 + 1668722000^2 &= \textcolor{red}{1234321} 564001^2 \quad (5.751) \end{aligned}$ $\begin{aligned} 0434496^2 + 1504000^2 &= \textcolor{red}{1} 565504^2 \\ \textcolor{blue}{12} 0434496^2 + 16544000^2 &= \textcolor{red}{121} 565504^2 \\ \textcolor{blue}{1232} 0434496^2 + 166944000^2 &= \textcolor{red}{12321} 565504^2 \\ \textcolor{blue}{123432} 0434496^2 + 1670944000^2 &= \textcolor{red}{1234321} 565504^2 \quad (5.752) \end{aligned}$ $\begin{aligned} 0432991^2 + 1506000^2 &= \textcolor{red}{1} 567009^2 \\ \textcolor{blue}{12} 0432991^2 + 16566000^2 &= \textcolor{red}{121} 567009^2 \\ \textcolor{blue}{1232} 0432991^2 + 167166000^2 &= \textcolor{red}{12321} 567009^2 \\ \textcolor{blue}{123432} 0432991^2 + 1673166000^2 &= \textcolor{red}{1234321} 567009^2 \quad (5.753) \end{aligned}$ $\begin{aligned} 0431484^2 + 1508000^2 &= \textcolor{red}{1} 568516^2 \\ \textcolor{blue}{12} 0431484^2 + 16588000^2 &= \textcolor{red}{121} 568516^2 \\ \textcolor{blue}{1232} 0431484^2 + 167388000^2 &= \textcolor{red}{12321} 568516^2 \\ \textcolor{blue}{123432} 0431484^2 + 1675388000^2 &= \textcolor{red}{1234321} 568516^2 \quad (5.754) \end{aligned}$ $\begin{aligned} 0429975^2 + 1510000^2 &= \textcolor{red}{1} 570025^2 \\ \textcolor{blue}{12} 0429975^2 + 16610000^2 &= \textcolor{red}{121} 570025^2 \\ \textcolor{blue}{1232} 0429975^2 + 167610000^2 &= \textcolor{red}{12321} 570025^2 \\ \textcolor{blue}{123432} 0429975^2 + 1677610000^2 &= \textcolor{red}{1234321} 570025^2 \quad (5.755) \end{aligned}$ $\begin{aligned} 0428464^2 + 1512000^2 &= \textcolor{red}{1} 571536^2 \\ \textcolor{blue}{12} 0428464^2 + 16632000^2 &= \textcolor{red}{121} 571536^2 \\ \textcolor{blue}{1232} 0428464^2 + 167832000^2 &= \textcolor{red}{12321} 571536^2 \\ \textcolor{blue}{123432} 0428464^2 + 1679832000^2 &= \textcolor{red}{1234321} 571536^2 \quad (5.756) \end{aligned}$	$\begin{aligned} 0426951^2 + 1514000^2 &= \textcolor{red}{1} 573049^2 \\ \textcolor{blue}{12} 0426951^2 + 16654000^2 &= \textcolor{red}{121} 573049^2 \\ \textcolor{blue}{1232} 0426951^2 + 168054000^2 &= \textcolor{red}{12321} 573049^2 \\ \textcolor{blue}{123432} 0426951^2 + 1682054000^2 &= \textcolor{red}{1234321} 573049^2 \quad (5.757) \end{aligned}$ $\begin{aligned} 0425436^2 + 1516000^2 &= \textcolor{red}{1} 574564^2 \\ \textcolor{blue}{12} 0425436^2 + 16676000^2 &= \textcolor{red}{121} 574564^2 \\ \textcolor{blue}{1232} 0425436^2 + 168276000^2 &= \textcolor{red}{12321} 574564^2 \\ \textcolor{blue}{123432} 0425436^2 + 1684276000^2 &= \textcolor{red}{1234321} 574564^2 \quad (5.758) \end{aligned}$ $\begin{aligned} 0423919^2 + 1518000^2 &= \textcolor{red}{1} 576081^2 \\ \textcolor{blue}{12} 0423919^2 + 16698000^2 &= \textcolor{red}{121} 576081^2 \\ \textcolor{blue}{1232} 0423919^2 + 168498000^2 &= \textcolor{red}{12321} 576081^2 \\ \textcolor{blue}{123432} 0423919^2 + 1686498000^2 &= \textcolor{red}{1234321} 576081^2 \quad (5.759) \end{aligned}$ $\begin{aligned} 0422400^2 + 1520000^2 &= \textcolor{red}{1} 577600^2 \\ \textcolor{blue}{12} 0422400^2 + 16720000^2 &= \textcolor{red}{121} 577600^2 \\ \textcolor{blue}{1232} 0422400^2 + 168720000^2 &= \textcolor{red}{12321} 577600^2 \\ \textcolor{blue}{123432} 0422400^2 + 1688720000^2 &= \textcolor{red}{1234321} 577600^2 \quad (5.760) \end{aligned}$ $\begin{aligned} 0420879^2 + 1522000^2 &= \textcolor{red}{1} 579121^2 \\ \textcolor{blue}{12} 0420879^2 + 16742000^2 &= \textcolor{red}{121} 579121^2 \\ \textcolor{blue}{1232} 0420879^2 + 168942000^2 &= \textcolor{red}{12321} 579121^2 \\ \textcolor{blue}{123432} 0420879^2 + 1690942000^2 &= \textcolor{red}{1234321} 579121^2 \quad (5.761) \end{aligned}$ $\begin{aligned} 0419356^2 + 1524000^2 &= \textcolor{red}{1} 580644^2 \\ \textcolor{blue}{12} 0419356^2 + 16764000^2 &= \textcolor{red}{121} 580644^2 \\ \textcolor{blue}{1232} 0419356^2 + 169164000^2 &= \textcolor{red}{12321} 580644^2 \\ \textcolor{blue}{123432} 0419356^2 + 1693164000^2 &= \textcolor{red}{1234321} 580644^2 \quad (5.762) \end{aligned}$ $\begin{aligned} 0417831^2 + 1526000^2 &= \textcolor{red}{1} 582169^2 \\ \textcolor{blue}{12} 0417831^2 + 16786000^2 &= \textcolor{red}{121} 582169^2 \\ \textcolor{blue}{1232} 0417831^2 + 169386000^2 &= \textcolor{red}{12321} 582169^2 \\ \textcolor{blue}{123432} 0417831^2 + 1695386000^2 &= \textcolor{red}{1234321} 582169^2 \quad (5.763) \end{aligned}$ $\begin{aligned} 0416304^2 + 1528000^2 &= \textcolor{red}{1} 583696^2 \\ \textcolor{blue}{12} 0416304^2 + 16808000^2 &= \textcolor{red}{121} 583696^2 \\ \textcolor{blue}{1232} 0416304^2 + 169608000^2 &= \textcolor{red}{12321} 583696^2 \\ \textcolor{blue}{123432} 0416304^2 + 1697608000^2 &= \textcolor{red}{1234321} 583696^2 \quad (5.764) \end{aligned}$
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$$\begin{aligned}
& 0414775^2 + 1530000^2 = \mathbf{1} 585225^2 \\
& \mathbf{12} 0414775^2 + 16830000^2 = \mathbf{121} 585225^2 \\
& \mathbf{1232} 0414775^2 + 169830000^2 = \mathbf{12321} 585225^2 \\
& \mathbf{123432} 0414775^2 + 1699830000^2 = \mathbf{1234321} 585225^2 \quad (5.765) \\
& \\
& 0413244^2 + 1532000^2 = \mathbf{1} 586756^2 \\
& \mathbf{12} 0413244^2 + 16852000^2 = \mathbf{121} 586756^2 \\
& \mathbf{1232} 0413244^2 + 170052000^2 = \mathbf{12321} 586756^2 \\
& \mathbf{123432} 0413244^2 + 1702052000^2 = \mathbf{1234321} 586756^2 \quad (5.766) \\
& \\
& 0411711^2 + 1534000^2 = \mathbf{1} 588289^2 \\
& \mathbf{12} 0411711^2 + 16874000^2 = \mathbf{121} 588289^2 \\
& \mathbf{1232} 0411711^2 + 170274000^2 = \mathbf{12321} 588289^2 \\
& \mathbf{123432} 0411711^2 + 1704274000^2 = \mathbf{1234321} 588289^2 \quad (5.767) \\
& \\
& 0410176^2 + 1536000^2 = \mathbf{1} 589824^2 \\
& \mathbf{12} 0410176^2 + 16896000^2 = \mathbf{121} 589824^2 \\
& \mathbf{1232} 0410176^2 + 170496000^2 = \mathbf{12321} 589824^2 \\
& \mathbf{123432} 0410176^2 + 1706496000^2 = \mathbf{1234321} 589824^2 \quad (5.768) \\
& \\
& 0408639^2 + 1538000^2 = \mathbf{1} 591361^2 \\
& \mathbf{12} 0408639^2 + 16918000^2 = \mathbf{121} 591361^2 \\
& \mathbf{1232} 0408639^2 + 170718000^2 = \mathbf{12321} 591361^2 \\
& \mathbf{123432} 0408639^2 + 1708718000^2 = \mathbf{1234321} 591361^2 \quad (5.769) \\
& \\
& 0407100^2 + 1540000^2 = \mathbf{1} 592900^2 \\
& \mathbf{12} 0407100^2 + 16940000^2 = \mathbf{121} 592900^2 \\
& \mathbf{1232} 0407100^2 + 170940000^2 = \mathbf{12321} 592900^2 \\
& \mathbf{123432} 0407100^2 + 1710940000^2 = \mathbf{1234321} 592900^2 \quad (5.770) \\
& \\
& 0405559^2 + 1542000^2 = \mathbf{1} 594441^2 \\
& \mathbf{12} 0405559^2 + 16962000^2 = \mathbf{121} 594441^2 \\
& \mathbf{1232} 0405559^2 + 171162000^2 = \mathbf{12321} 594441^2 \\
& \mathbf{123432} 0405559^2 + 1713162000^2 = \mathbf{1234321} 594441^2 \quad (5.771) \\
& \\
& 0404016^2 + 1544000^2 = \mathbf{1} 595984^2 \\
& \mathbf{12} 0404016^2 + 16984000^2 = \mathbf{121} 595984^2 \\
& \mathbf{1232} 0404016^2 + 171384000^2 = \mathbf{12321} 595984^2 \\
& \mathbf{123432} 0404016^2 + 1715384000^2 = \mathbf{1234321} 595984^2 \quad (5.772) \\
& \\
& 0402471^2 + 1546000^2 = \mathbf{1} 597529^2 \\
& \mathbf{12} 0402471^2 + 17006000^2 = \mathbf{121} 597529^2 \\
& \mathbf{1232} 0402471^2 + 171606000^2 = \mathbf{12321} 597529^2 \\
& \mathbf{123432} 0402471^2 + 1717606000^2 = \mathbf{1234321} 597529^2 \quad (5.773)
\end{aligned}$$

$0388476^2 + 1564000^2 = \textcolor{red}{1} \textcolor{blue}{6}11524^2$	$0374319^2 + 1582000^2 = \textcolor{red}{1} \textcolor{blue}{6}25681^2$
$12 \ 0388476^2 + 17204000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}11524^2$	$12 \ 0374319^2 + 17402000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}25681^2$
$1232 \ 0388476^2 + 173604000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}11524^2$	$1232 \ 0374319^2 + 175602000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}25681^2$
$123432 \ 0388476^2 + 1737604000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}11524^2 \ (5.782)$	$123432 \ 0374319^2 + 1757602000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}25681^2 \ (5.791)$
$0386911^2 + 1566000^2 = \textcolor{red}{1} \textcolor{blue}{6}13089^2$	$0372736^2 + 1584000^2 = \textcolor{red}{1} \textcolor{blue}{6}27264^2$
$12 \ 0386911^2 + 17226000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}13089^2$	$12 \ 0372736^2 + 17424000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}27264^2$
$1232 \ 0386911^2 + 173826000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}13089^2$	$1232 \ 0372736^2 + 175824000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}27264^2$
$123432 \ 0386911^2 + 1739826000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}13089^2 \ (5.783)$	$123432 \ 0372736^2 + 1759824000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}27264^2 \ (5.792)$
$0385344^2 + 1568000^2 = \textcolor{red}{1} \textcolor{blue}{6}14656^2$	$0371151^2 + 1586000^2 = \textcolor{red}{1} \textcolor{blue}{6}28849^2$
$12 \ 0385344^2 + 17248000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}14656^2$	$12 \ 0371151^2 + 17446000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}28849^2$
$1232 \ 0385344^2 + 174048000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}14656^2$	$1232 \ 0371151^2 + 176046000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}28849^2$
$123432 \ 0385344^2 + 1742048000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}14656^2 \ (5.784)$	$123432 \ 0371151^2 + 1762046000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}28849^2 \ (5.793)$
$0383775^2 + 1570000^2 = \textcolor{red}{1} \textcolor{blue}{6}16225^2$	$0369564^2 + 1588000^2 = \textcolor{red}{1} \textcolor{blue}{6}30436^2$
$12 \ 0383775^2 + 17270000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}16225^2$	$12 \ 0369564^2 + 17468000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}30436^2$
$1232 \ 0383775^2 + 174270000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}16225^2$	$1232 \ 0369564^2 + 176268000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}30436^2$
$123432 \ 0383775^2 + 1744270000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}16225^2 \ (5.785)$	$123432 \ 0369564^2 + 1764268000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}30436^2 \ (5.794)$
$0382204^2 + 1572000^2 = \textcolor{red}{1} \textcolor{blue}{6}17796^2$	$0367975^2 + 1590000^2 = \textcolor{red}{1} \textcolor{blue}{6}32025^2$
$12 \ 0382204^2 + 17292000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}17796^2$	$12 \ 0367975^2 + 17490000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}32025^2$
$1232 \ 0382204^2 + 174492000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}17796^2$	$1232 \ 0367975^2 + 176490000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}32025^2$
$123432 \ 0382204^2 + 1746492000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}17796^2 \ (5.786)$	$123432 \ 0367975^2 + 1766490000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}32025^2 \ (5.795)$
$0380631^2 + 1574000^2 = \textcolor{red}{1} \textcolor{blue}{6}19369^2$	$0366384^2 + 1592000^2 = \textcolor{red}{1} \textcolor{blue}{6}33616^2$
$12 \ 0380631^2 + 17314000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}19369^2$	$12 \ 0366384^2 + 17512000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}33616^2$
$1232 \ 0380631^2 + 174714000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}19369^2$	$1232 \ 0366384^2 + 176712000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}33616^2$
$123432 \ 0380631^2 + 1748714000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}19369^2 \ (5.787)$	$123432 \ 0366384^2 + 1768712000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}33616^2 \ (5.796)$
$0379056^2 + 1576000^2 = \textcolor{red}{1} \textcolor{blue}{6}20944^2$	$0364791^2 + 1594000^2 = \textcolor{red}{1} \textcolor{blue}{6}35209^2$
$12 \ 0379056^2 + 17336000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}20944^2$	$12 \ 0364791^2 + 17534000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}35209^2$
$1232 \ 0379056^2 + 174936000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}20944^2$	$1232 \ 0364791^2 + 176934000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}35209^2$
$123432 \ 0379056^2 + 1750936000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}20944^2 \ (5.788)$	$123432 \ 0364791^2 + 1770934000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}35209^2 \ (5.797)$
$0377479^2 + 1578000^2 = \textcolor{red}{1} \textcolor{blue}{6}22521^2$	$0363196^2 + 1596000^2 = \textcolor{red}{1} \textcolor{blue}{6}36804^2$
$12 \ 0377479^2 + 17358000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}22521^2$	$12 \ 0363196^2 + 17556000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}36804^2$
$1232 \ 0377479^2 + 175158000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}22521^2$	$1232 \ 0363196^2 + 177156000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}36804^2$
$123432 \ 0377479^2 + 1753158000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}22521^2 \ (5.789)$	$123432 \ 0363196^2 + 1773156000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}36804^2 \ (5.798)$
$0375900^2 + 1580000^2 = \textcolor{red}{1} \textcolor{blue}{6}24100^2$	$0361599^2 + 1598000^2 = \textcolor{red}{1} \textcolor{blue}{6}38401^2$
$12 \ 0375900^2 + 17380000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}24100^2$	$12 \ 0361599^2 + 17578000^2 = \textcolor{red}{1} \textcolor{blue}{2}1 \textcolor{blue}{6}38401^2$
$1232 \ 0375900^2 + 175380000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}24100^2$	$1232 \ 0361599^2 + 177378000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{2}1 \textcolor{blue}{6}38401^2$
$123432 \ 0375900^2 + 1755380000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}24100^2 \ (5.790)$	$123432 \ 0361599^2 + 1775378000^2 = \textcolor{red}{1} \textcolor{blue}{2}3\textcolor{red}{4}3\textcolor{red}{2}1 \textcolor{blue}{6}38401^2 \ (5.799)$

5.9 For $n = 800, 801, 801, \dots, 897, 898, 899$:

Let's consider

$$m = 1000, 11000, 111000, 1111000, 11111000, 111111000, 1111111000, 11111111000$$

in (1.1), then for each value of $n = 800, 801, 801, \dots, 897, 898, 899$; there are 100 *palindromic-type pandigital Pythagorean patterns* given below. In each case, only first four values are written. The other 5 values can be written on similar lines as done in subsection 5.1.1.

$0360000^2 + 1600000^2 = 1640000^2$	$0348751^2 + 1614000^2 = 1651249^2$
$120360000^2 + 17600000^2 = 121640000^2$	$120348751^2 + 17754000^2 = 121651249^2$
$12320360000^2 + 177600000^2 = 12321640000^2$	$12320348751^2 + 179154000^2 = 12321651249^2$
$1234320360000^2 + 1777600000^2 = 1234321640000^2$ (5.800)	$1234320348751^2 + 1793154000^2 = 1234321651249^2$ (5.807)
$0358399^2 + 1602000^2 = 1641601^2$	$0347136^2 + 1616000^2 = 1652864^2$
$120358399^2 + 17622000^2 = 121641601^2$	$120347136^2 + 17776000^2 = 121652864^2$
$12320358399^2 + 177822000^2 = 12321641601^2$	$12320347136^2 + 179376000^2 = 12321652864^2$
$1234320358399^2 + 1779822000^2 = 1234321641601^2$ (5.801)	$1234320347136^2 + 1795376000^2 = 1234321652864^2$ (5.808)
$0356796^2 + 1604000^2 = 1643204^2$	$0345519^2 + 1618000^2 = 1654481^2$
$120356796^2 + 17644000^2 = 121643204^2$	$120345519^2 + 17798000^2 = 121654481^2$
$12320356796^2 + 178044000^2 = 12321643204^2$	$12320345519^2 + 179598000^2 = 12321654481^2$
$1234320356796^2 + 1782044000^2 = 1234321643204^2$ (5.802)	$1234320345519^2 + 1797598000^2 = 1234321654481^2$ (5.809)
$0355191^2 + 1606000^2 = 1644809^2$	$0343900^2 + 1620000^2 = 1656100^2$
$120355191^2 + 17666000^2 = 121644809^2$	$120343900^2 + 17820000^2 = 121656100^2$
$12320355191^2 + 178266000^2 = 12321644809^2$	$12320343900^2 + 179820000^2 = 12321656100^2$
$1234320355191^2 + 1784266000^2 = 1234321644809^2$ (5.803)	$1234320343900^2 + 1799820000^2 = 1234321656100^2$ (5.810)
$0353584^2 + 1608000^2 = 1646416^2$	$0342279^2 + 1622000^2 = 1657721^2$
$120353584^2 + 17688000^2 = 121646416^2$	$120342279^2 + 17842000^2 = 121657721^2$
$12320353584^2 + 178488000^2 = 12321646416^2$	$12320342279^2 + 180042000^2 = 12321657721^2$
$1234320353584^2 + 1786488000^2 = 1234321646416^2$ (5.804)	$1234320342279^2 + 1802042000^2 = 1234321657721^2$ (5.811)
$0351975^2 + 1610000^2 = 1648025^2$	$0340656^2 + 1624000^2 = 1659344^2$
$120351975^2 + 17710000^2 = 121648025^2$	$120340656^2 + 17864000^2 = 121659344^2$
$12320351975^2 + 178710000^2 = 12321648025^2$	$12320340656^2 + 180264000^2 = 12321659344^2$
$1234320351975^2 + 1788710000^2 = 1234321648025^2$ (5.805)	$1234320340656^2 + 1804264000^2 = 1234321659344^2$ (5.812)
$0350364^2 + 1612000^2 = 1649636^2$	$0339031^2 + 1626000^2 = 1660969^2$
$120350364^2 + 17732000^2 = 121649636^2$	$120339031^2 + 17886000^2 = 121660969^2$
$12320350364^2 + 178932000^2 = 12321649636^2$	$12320339031^2 + 180486000^2 = 12321660969^2$
$1234320350364^2 + 1790932000^2 = 1234321649636^2$ (5.806)	$1234320339031^2 + 1806486000^2 = 1234321660969^2$ (5.813)

$$\begin{aligned}
& 0337404^2 + 1628000^2 = \mathbf{1} 662596^2 \\
& \mathbf{12} 0337404^2 + 17908000^2 = \mathbf{121} 662596^2 \\
& \mathbf{1232} 0337404^2 + 180708000^2 = \mathbf{12321} 662596^2 \\
& \mathbf{123432} 0337404^2 + 1808708000^2 = \mathbf{1234321} 662596^2 \quad (5.814) \\
& \\
& 0335775^2 + 1630000^2 = \mathbf{1} 664225^2 \\
& \mathbf{12} 0335775^2 + 17930000^2 = \mathbf{121} 664225^2 \\
& \mathbf{1232} 0335775^2 + 180930000^2 = \mathbf{12321} 664225^2 \\
& \mathbf{123432} 0335775^2 + 1810930000^2 = \mathbf{1234321} 664225^2 \quad (5.815) \\
& \\
& 0334144^2 + 1632000^2 = \mathbf{1} 665856^2 \\
& \mathbf{12} 0334144^2 + 17952000^2 = \mathbf{121} 665856^2 \\
& \mathbf{1232} 0334144^2 + 181152000^2 = \mathbf{12321} 665856^2 \\
& \mathbf{123432} 0334144^2 + 1813152000^2 = \mathbf{1234321} 665856^2 \quad (5.816) \\
& \\
& 0332511^2 + 1634000^2 = \mathbf{1} 667489^2 \\
& \mathbf{12} 0332511^2 + 17974000^2 = \mathbf{121} 667489^2 \\
& \mathbf{1232} 0332511^2 + 181374000^2 = \mathbf{12321} 667489^2 \\
& \mathbf{123432} 0332511^2 + 1815374000^2 = \mathbf{1234321} 667489^2 \quad (5.817) \\
& \\
& 0330876^2 + 1636000^2 = \mathbf{1} 669124^2 \\
& \mathbf{12} 0330876^2 + 17996000^2 = \mathbf{121} 669124^2 \\
& \mathbf{1232} 0330876^2 + 181596000^2 = \mathbf{12321} 669124^2 \\
& \mathbf{123432} 0330876^2 + 1817596000^2 = \mathbf{1234321} 669124^2 \quad (5.818) \\
& \\
& 0329239^2 + 1638000^2 = \mathbf{1} 670761^2 \\
& \mathbf{12} 0329239^2 + 18018000^2 = \mathbf{121} 670761^2 \\
& \mathbf{1232} 0329239^2 + 181818000^2 = \mathbf{12321} 670761^2 \\
& \mathbf{123432} 0329239^2 + 1819818000^2 = \mathbf{1234321} 670761^2 \quad (5.819) \\
& \\
& 0327600^2 + 1640000^2 = \mathbf{1} 672400^2 \\
& \mathbf{12} 0327600^2 + 18040000^2 = \mathbf{121} 672400^2 \\
& \mathbf{1232} 0327600^2 + 182040000^2 = \mathbf{12321} 672400^2 \\
& \mathbf{123432} 0327600^2 + 1822040000^2 = \mathbf{1234321} 672400^2 \quad (5.820) \\
& \\
& 0325959^2 + 1642000^2 = \mathbf{1} 674041^2 \\
& \mathbf{12} 0325959^2 + 18062000^2 = \mathbf{121} 674041^2 \\
& \mathbf{1232} 0325959^2 + 182262000^2 = \mathbf{12321} 674041^2 \\
& \mathbf{123432} 0325959^2 + 1824262000^2 = \mathbf{1234321} 674041^2 \quad (5.821) \\
& \\
& 0324316^2 + 1644000^2 = \mathbf{1} 675684^2 \\
& \mathbf{12} 0324316^2 + 18084000^2 = \mathbf{121} 675684^2 \\
& \mathbf{1232} 0324316^2 + 182484000^2 = \mathbf{12321} 675684^2 \\
& \mathbf{123432} 0324316^2 + 1826484000^2 = \mathbf{1234321} 675684^2 \quad (5.822) \\
& \\
& 0322671^2 + 1646000^2 = \mathbf{1} 677329^2 \\
& \mathbf{12} 0322671^2 + 18106000^2 = \mathbf{121} 677329^2 \\
& \mathbf{1232} 0322671^2 + 182706000^2 = \mathbf{12321} 677329^2 \\
& \mathbf{123432} 0322671^2 + 1828706000^2 = \mathbf{1234321} 677329^2 \quad (5.823) \\
& \\
& 0321024^2 + 1648000^2 = \mathbf{1} 678976^2 \\
& \mathbf{12} 0321024^2 + 18128000^2 = \mathbf{121} 678976^2 \\
& \mathbf{1232} 0321024^2 + 182928000^2 = \mathbf{12321} 678976^2 \\
& \mathbf{123432} 0321024^2 + 1830928000^2 = \mathbf{1234321} 678976^2 \quad (5.824) \\
& \\
& 0319375^2 + 1650000^2 = \mathbf{1} 680625^2 \\
& \mathbf{12} 0319375^2 + 18150000^2 = \mathbf{121} 680625^2 \\
& \mathbf{1232} 0319375^2 + 183150000^2 = \mathbf{12321} 680625^2 \\
& \mathbf{123432} 0319375^2 + 1833150000^2 = \mathbf{1234321} 680625^2 \quad (5.825) \\
& \\
& 0317724^2 + 1652000^2 = \mathbf{1} 682276^2 \\
& \mathbf{12} 0317724^2 + 18172000^2 = \mathbf{121} 682276^2 \\
& \mathbf{1232} 0317724^2 + 183372000^2 = \mathbf{12321} 682276^2 \\
& \mathbf{123432} 0317724^2 + 1835372000^2 = \mathbf{1234321} 682276^2 \quad (5.826) \\
& \\
& 0316071^2 + 1654000^2 = \mathbf{1} 683929^2 \\
& \mathbf{12} 0316071^2 + 18194000^2 = \mathbf{121} 683929^2 \\
& \mathbf{1232} 0316071^2 + 183594000^2 = \mathbf{12321} 683929^2 \\
& \mathbf{123432} 0316071^2 + 1837594000^2 = \mathbf{1234321} 683929^2 \quad (5.827) \\
& \\
& 0314416^2 + 1656000^2 = \mathbf{1} 685584^2 \\
& \mathbf{12} 0314416^2 + 18216000^2 = \mathbf{121} 685584^2 \\
& \mathbf{1232} 0314416^2 + 183816000^2 = \mathbf{12321} 685584^2 \\
& \mathbf{123432} 0314416^2 + 1839816000^2 = \mathbf{1234321} 685584^2 \quad (5.828) \\
& \\
& 0312759^2 + 1658000^2 = \mathbf{1} 687241^2 \\
& \mathbf{12} 0312759^2 + 18238000^2 = \mathbf{121} 687241^2 \\
& \mathbf{1232} 0312759^2 + 184038000^2 = \mathbf{12321} 687241^2 \\
& \mathbf{123432} 0312759^2 + 1842038000^2 = \mathbf{1234321} 687241^2 \quad (5.829) \\
& \\
& 0311100^2 + 1660000^2 = \mathbf{1} 688900^2 \\
& \mathbf{12} 0311100^2 + 18260000^2 = \mathbf{121} 688900^2 \\
& \mathbf{1232} 0311100^2 + 184260000^2 = \mathbf{12321} 688900^2 \\
& \mathbf{123432} 0311100^2 + 1844260000^2 = \mathbf{1234321} 688900^2 \quad (5.830)
\end{aligned}$$

$$\begin{aligned}
& 0309439^2 + 1662000^2 = \mathbf{1} 690561^2 \\
& \mathbf{12} 0309439^2 + 18282000^2 = \mathbf{121} 690561^2 \\
& \mathbf{1232} 0309439^2 + 184482000^2 = \mathbf{12321} 690561^2 \\
& \mathbf{123432} 0309439^2 + 1846482000^2 = \mathbf{1234321} 690561^2 \quad (5.831) \\
& \\
& 0307776^2 + 1664000^2 = \mathbf{1} 692224^2 \\
& \mathbf{12} 0307776^2 + 18304000^2 = \mathbf{121} 692224^2 \\
& \mathbf{1232} 0307776^2 + 184704000^2 = \mathbf{12321} 692224^2 \\
& \mathbf{123432} 0307776^2 + 1848704000^2 = \mathbf{1234321} 692224^2 \quad (5.832) \\
& \\
& 0306111^2 + 1666000^2 = \mathbf{1} 693889^2 \\
& \mathbf{12} 0306111^2 + 18326000^2 = \mathbf{121} 693889^2 \\
& \mathbf{1232} 0306111^2 + 184926000^2 = \mathbf{12321} 693889^2 \\
& \mathbf{123432} 0306111^2 + 1850926000^2 = \mathbf{1234321} 693889^2 \quad (5.833) \\
& \\
& 0304444^2 + 1668000^2 = \mathbf{1} 695556^2 \\
& \mathbf{12} 0304444^2 + 18348000^2 = \mathbf{121} 695556^2 \\
& \mathbf{1232} 0304444^2 + 185148000^2 = \mathbf{12321} 695556^2 \\
& \mathbf{123432} 0304444^2 + 1853148000^2 = \mathbf{1234321} 695556^2 \quad (5.834) \\
& \\
& 0302775^2 + 1670000^2 = \mathbf{1} 697225^2 \\
& \mathbf{12} 0302775^2 + 18370000^2 = \mathbf{121} 697225^2 \\
& \mathbf{1232} 0302775^2 + 185370000^2 = \mathbf{12321} 697225^2 \\
& \mathbf{123432} 0302775^2 + 1855370000^2 = \mathbf{1234321} 697225^2 \quad (5.835) \\
& \\
& 0301104^2 + 1672000^2 = \mathbf{1} 698896^2 \\
& \mathbf{12} 0301104^2 + 18392000^2 = \mathbf{121} 698896^2 \\
& \mathbf{1232} 0301104^2 + 185592000^2 = \mathbf{12321} 698896^2 \\
& \mathbf{123432} 0301104^2 + 1857592000^2 = \mathbf{1234321} 698896^2 \quad (5.836) \\
& \\
& 0299431^2 + 1674000^2 = \mathbf{1} 700569^2 \\
& \mathbf{12} 0299431^2 + 18414000^2 = \mathbf{121} 700569^2 \\
& \mathbf{1232} 0299431^2 + 185814000^2 = \mathbf{12321} 700569^2 \\
& \mathbf{123432} 0299431^2 + 1859814000^2 = \mathbf{1234321} 700569^2 \quad (5.837) \\
& \\
& 0297756^2 + 1676000^2 = \mathbf{1} 702244^2 \\
& \mathbf{12} 0297756^2 + 18436000^2 = \mathbf{121} 702244^2 \\
& \mathbf{1232} 0297756^2 + 186036000^2 = \mathbf{12321} 702244^2 \\
& \mathbf{123432} 0297756^2 + 1862036000^2 = \mathbf{1234321} 702244^2 \quad (5.838) \\
& \\
& 0296079^2 + 1678000^2 = \mathbf{1} 703921^2 \\
& \mathbf{12} 0296079^2 + 18458000^2 = \mathbf{121} 703921^2 \\
& \mathbf{1232} 0296079^2 + 186258000^2 = \mathbf{12321} 703921^2 \\
& \mathbf{123432} 0296079^2 + 1864258000^2 = \mathbf{1234321} 703921^2 \quad (5.839)
\end{aligned}$$

$0280896^2 + 1696000^2 = \textcolor{red}{1}719104^2$	$0265551^2 + 1714000^2 = \textcolor{blue}{1}734449^2$
$12\ 0280896^2 + 18656000^2 = \textcolor{red}{121}719104^2$	$12\ 0265551^2 + 18854000^2 = \textcolor{blue}{121}734449^2$
$1232\ 0280896^2 + 188256000^2 = \textcolor{red}{12321}719104^2$	$1232\ 0265551^2 + 190254000^2 = \textcolor{blue}{12321}734449^2$
$123432\ 0280896^2 + 1884256000^2 = \textcolor{red}{1234321}719104^2 \quad (5.848)$	$123432\ 0265551^2 + 1904254000^2 = \textcolor{blue}{1234321}734449^2 \quad (5.857)$
$0279199^2 + 1698000^2 = \textcolor{red}{1}720801^2$	$0263836^2 + 1716000^2 = \textcolor{blue}{1}736164^2$
$12\ 0279199^2 + 18678000^2 = \textcolor{red}{121}720801^2$	$12\ 0263836^2 + 18876000^2 = \textcolor{blue}{121}736164^2$
$1232\ 0279199^2 + 188478000^2 = \textcolor{red}{12321}720801^2$	$1232\ 0263836^2 + 190476000^2 = \textcolor{blue}{12321}736164^2$
$123432\ 0279199^2 + 1886478000^2 = \textcolor{red}{1234321}720801^2 \quad (5.849)$	$123432\ 0263836^2 + 1906476000^2 = \textcolor{blue}{1234321}736164^2 \quad (5.858)$
$0277500^2 + 1700000^2 = \textcolor{red}{1}722500^2$	$0262119^2 + 1718000^2 = \textcolor{blue}{1}737881^2$
$12\ 0277500^2 + 18700000^2 = \textcolor{red}{121}722500^2$	$12\ 0262119^2 + 18898000^2 = \textcolor{blue}{121}737881^2$
$1232\ 0277500^2 + 188700000^2 = \textcolor{red}{12321}722500^2$	$1232\ 0262119^2 + 190698000^2 = \textcolor{blue}{12321}737881^2$
$123432\ 0277500^2 + 1888700000^2 = \textcolor{red}{1234321}722500^2 \quad (5.850)$	$123432\ 0262119^2 + 1908698000^2 = \textcolor{blue}{1234321}737881^2 \quad (5.859)$
$0275799^2 + 1702000^2 = \textcolor{red}{1}724201^2$	$0260400^2 + 1720000^2 = \textcolor{blue}{1}739600^2$
$12\ 0275799^2 + 18722000^2 = \textcolor{red}{121}724201^2$	$12\ 0260400^2 + 18920000^2 = \textcolor{blue}{121}739600^2$
$1232\ 0275799^2 + 188922000^2 = \textcolor{red}{12321}724201^2$	$1232\ 0260400^2 + 190920000^2 = \textcolor{blue}{12321}739600^2$
$123432\ 0275799^2 + 1890922000^2 = \textcolor{red}{1234321}724201^2 \quad (5.851)$	$123432\ 0260400^2 + 1910920000^2 = \textcolor{blue}{1234321}739600^2 \quad (5.860)$
$0274096^2 + 1704000^2 = \textcolor{red}{1}725904^2$	$0258679^2 + 1722000^2 = \textcolor{blue}{1}741321^2$
$12\ 0274096^2 + 18744000^2 = \textcolor{red}{121}725904^2$	$12\ 0258679^2 + 18942000^2 = \textcolor{blue}{121}741321^2$
$1232\ 0274096^2 + 189144000^2 = \textcolor{red}{12321}725904^2$	$1232\ 0258679^2 + 191142000^2 = \textcolor{blue}{12321}741321^2$
$123432\ 0274096^2 + 1893144000^2 = \textcolor{red}{1234321}725904^2 \quad (5.852)$	$123432\ 0258679^2 + 1913142000^2 = \textcolor{blue}{1234321}741321^2 \quad (5.861)$
$0272391^2 + 1706000^2 = \textcolor{red}{1}727609^2$	$0256956^2 + 1724000^2 = \textcolor{blue}{1}743044^2$
$12\ 0272391^2 + 18766000^2 = \textcolor{red}{121}727609^2$	$12\ 0256956^2 + 18964000^2 = \textcolor{blue}{121}743044^2$
$1232\ 0272391^2 + 189366000^2 = \textcolor{red}{12321}727609^2$	$1232\ 0256956^2 + 191364000^2 = \textcolor{blue}{12321}743044^2$
$123432\ 0272391^2 + 1895366000^2 = \textcolor{red}{1234321}727609^2 \quad (5.853)$	$123432\ 0256956^2 + 1915364000^2 = \textcolor{blue}{1234321}743044^2 \quad (5.862)$
$0270684^2 + 1708000^2 = \textcolor{red}{1}729316^2$	$0255231^2 + 1726000^2 = \textcolor{blue}{1}744769^2$
$12\ 0270684^2 + 18788000^2 = \textcolor{red}{121}729316^2$	$12\ 0255231^2 + 18986000^2 = \textcolor{blue}{121}744769^2$
$1232\ 0270684^2 + 189588000^2 = \textcolor{red}{12321}729316^2$	$1232\ 0255231^2 + 191586000^2 = \textcolor{blue}{12321}744769^2$
$123432\ 0270684^2 + 1897588000^2 = \textcolor{red}{1234321}729316^2 \quad (5.854)$	$123432\ 0255231^2 + 1917586000^2 = \textcolor{blue}{1234321}744769^2 \quad (5.863)$
$0268975^2 + 1710000^2 = \textcolor{red}{1}731025^2$	$0253504^2 + 1728000^2 = \textcolor{blue}{1}746496^2$
$12\ 0268975^2 + 18810000^2 = \textcolor{red}{121}731025^2$	$12\ 0253504^2 + 19008000^2 = \textcolor{blue}{121}746496^2$
$1232\ 0268975^2 + 189810000^2 = \textcolor{red}{12321}731025^2$	$1232\ 0253504^2 + 191808000^2 = \textcolor{blue}{12321}746496^2$
$123432\ 0268975^2 + 1899810000^2 = \textcolor{red}{1234321}731025^2 \quad (5.855)$	$123432\ 0253504^2 + 1919808000^2 = \textcolor{blue}{1234321}746496^2 \quad (5.864)$
$0267264^2 + 1712000^2 = \textcolor{red}{1}732736^2$	
$12\ 0267264^2 + 18832000^2 = \textcolor{red}{121}732736^2$	
$1232\ 0267264^2 + 190032000^2 = \textcolor{red}{12321}732736^2$	
$123432\ 0267264^2 + 1902032000^2 = \textcolor{red}{1234321}732736^2 \quad (5.856)$	

$$\begin{aligned}
& 0251775^2 + 1730000^2 = \mathbf{1} 748225^2 \\
& \mathbf{12} 0251775^2 + 19030000^2 = \mathbf{121} 748225^2 \\
& \mathbf{1232} 0251775^2 + 192030000^2 = \mathbf{12321} 748225^2 \\
& \mathbf{123432} 0251775^2 + 1922030000^2 = \mathbf{1234321} 748225^2 \quad (5.865) \\
& \\
& 0250044^2 + 1732000^2 = \mathbf{1} 749956^2 \\
& \mathbf{12} 0250044^2 + 19052000^2 = \mathbf{121} 749956^2 \\
& \mathbf{1232} 0250044^2 + 192252000^2 = \mathbf{12321} 749956^2 \\
& \mathbf{123432} 0250044^2 + 1924252000^2 = \mathbf{1234321} 749956^2 \quad (5.866) \\
& \\
& 0248311^2 + 1734000^2 = \mathbf{1} 751689^2 \\
& \mathbf{12} 0248311^2 + 19074000^2 = \mathbf{121} 751689^2 \\
& \mathbf{1232} 0248311^2 + 192474000^2 = \mathbf{12321} 751689^2 \\
& \mathbf{123432} 0248311^2 + 1926474000^2 = \mathbf{1234321} 751689^2 \quad (5.867) \\
& \\
& 0246576^2 + 1736000^2 = \mathbf{1} 753424^2 \\
& \mathbf{12} 0246576^2 + 19096000^2 = \mathbf{121} 753424^2 \\
& \mathbf{1232} 0246576^2 + 192696000^2 = \mathbf{12321} 753424^2 \\
& \mathbf{123432} 0246576^2 + 1928696000^2 = \mathbf{1234321} 753424^2 \quad (5.868) \\
& \\
& 0244839^2 + 1738000^2 = \mathbf{1} 755161^2 \\
& \mathbf{12} 0244839^2 + 19118000^2 = \mathbf{121} 755161^2 \\
& \mathbf{1232} 0244839^2 + 192918000^2 = \mathbf{12321} 755161^2 \\
& \mathbf{123432} 0244839^2 + 1930918000^2 = \mathbf{1234321} 755161^2 \quad (5.869) \\
& \\
& 0243100^2 + 1740000^2 = \mathbf{1} 756900^2 \\
& \mathbf{12} 0243100^2 + 19140000^2 = \mathbf{121} 756900^2 \\
& \mathbf{1232} 0243100^2 + 193140000^2 = \mathbf{12321} 756900^2 \\
& \mathbf{123432} 0243100^2 + 1933140000^2 = \mathbf{1234321} 756900^2 \quad (5.870) \\
& \\
& 0241359^2 + 1742000^2 = \mathbf{1} 758641^2 \\
& \mathbf{12} 0241359^2 + 19162000^2 = \mathbf{121} 758641^2 \\
& \mathbf{1232} 0241359^2 + 193362000^2 = \mathbf{12321} 758641^2 \\
& \mathbf{123432} 0241359^2 + 1935362000^2 = \mathbf{1234321} 758641^2 \quad (5.871) \\
& \\
& 0239616^2 + 1744000^2 = \mathbf{1} 760384^2 \\
& \mathbf{12} 0239616^2 + 19184000^2 = \mathbf{121} 760384^2 \\
& \mathbf{1232} 0239616^2 + 193584000^2 = \mathbf{12321} 760384^2 \\
& \mathbf{123432} 0239616^2 + 1937584000^2 = \mathbf{1234321} 760384^2 \quad (5.872) \\
& \\
& 0237871^2 + 1746000^2 = \mathbf{1} 762129^2 \\
& \mathbf{12} 0237871^2 + 19206000^2 = \mathbf{121} 762129^2 \\
& \mathbf{1232} 0237871^2 + 193806000^2 = \mathbf{12321} 762129^2 \\
& \mathbf{123432} 0237871^2 + 1939806000^2 = \mathbf{1234321} 762129^2 \quad (5.873) \\
& \\
& 0236124^2 + 1748000^2 = \mathbf{1} 763876^2 \\
& \mathbf{12} 0236124^2 + 19228000^2 = \mathbf{121} 763876^2 \\
& \mathbf{1232} 0236124^2 + 194028000^2 = \mathbf{12321} 763876^2 \\
& \mathbf{123432} 0236124^2 + 1942028000^2 = \mathbf{1234321} 763876^2 \quad (5.874) \\
& \\
& 0234375^2 + 1750000^2 = \mathbf{1} 765625^2 \\
& \mathbf{12} 0234375^2 + 19250000^2 = \mathbf{121} 765625^2 \\
& \mathbf{1232} 0234375^2 + 194250000^2 = \mathbf{12321} 765625^2 \\
& \mathbf{123432} 0234375^2 + 1944250000^2 = \mathbf{1234321} 765625^2 \quad (5.875) \\
& \\
& 0232624^2 + 1752000^2 = \mathbf{1} 767376^2 \\
& \mathbf{12} 0232624^2 + 19272000^2 = \mathbf{121} 767376^2 \\
& \mathbf{1232} 0232624^2 + 194472000^2 = \mathbf{12321} 767376^2 \\
& \mathbf{123432} 0232624^2 + 1946472000^2 = \mathbf{1234321} 767376^2 \quad (5.876) \\
& \\
& 0230871^2 + 1754000^2 = \mathbf{1} 769129^2 \\
& \mathbf{12} 0230871^2 + 19294000^2 = \mathbf{121} 769129^2 \\
& \mathbf{1232} 0230871^2 + 194694000^2 = \mathbf{12321} 769129^2 \\
& \mathbf{123432} 0230871^2 + 1948694000^2 = \mathbf{1234321} 769129^2 \quad (5.877) \\
& \\
& 0229116^2 + 1756000^2 = \mathbf{1} 770884^2 \\
& \mathbf{12} 0229116^2 + 19316000^2 = \mathbf{121} 770884^2 \\
& \mathbf{1232} 0229116^2 + 194916000^2 = \mathbf{12321} 770884^2 \\
& \mathbf{123432} 0229116^2 + 1950916000^2 = \mathbf{1234321} 770884^2 \quad (5.878) \\
& \\
& 0227359^2 + 1758000^2 = \mathbf{1} 772641^2 \\
& \mathbf{12} 0227359^2 + 19338000^2 = \mathbf{121} 772641^2 \\
& \mathbf{1232} 0227359^2 + 195138000^2 = \mathbf{12321} 772641^2 \\
& \mathbf{123432} 0227359^2 + 1953138000^2 = \mathbf{1234321} 772641^2 \quad (5.879) \\
& \\
& 0225600^2 + 1760000^2 = \mathbf{1} 774400^2 \\
& \mathbf{12} 0225600^2 + 19360000^2 = \mathbf{121} 774400^2 \\
& \mathbf{1232} 0225600^2 + 195360000^2 = \mathbf{12321} 774400^2 \\
& \mathbf{123432} 0225600^2 + 1955360000^2 = \mathbf{1234321} 774400^2 \quad (5.880) \\
& \\
& 0223839^2 + 1762000^2 = \mathbf{1} 776161^2 \\
& \mathbf{12} 0223839^2 + 19382000^2 = \mathbf{121} 776161^2 \\
& \mathbf{1232} 0223839^2 + 195582000^2 = \mathbf{12321} 776161^2 \\
& \mathbf{123432} 0223839^2 + 1957582000^2 = \mathbf{1234321} 776161^2 \quad (5.881)
\end{aligned}$$

$0222076^2 + 1764000^2 = \textcolor{red}{1} \textcolor{blue}{777924}^2$	$0206119^2 + 1782000^2 = \textcolor{red}{1} \textcolor{blue}{793881}^2$
$12 \ 0222076^2 + 19404000^2 = \textcolor{red}{121} \textcolor{blue}{777924}^2$	$12 \ 0206119^2 + 19602000^2 = \textcolor{red}{121} \textcolor{blue}{793881}^2$
$1232 \ 0222076^2 + 195804000^2 = \textcolor{red}{12321} \textcolor{blue}{777924}^2$	$1232 \ 0206119^2 + 197802000^2 = \textcolor{red}{12321} \textcolor{blue}{793881}^2$
$123432 \ 0222076^2 + 1959804000^2 = \textcolor{red}{1234321} \textcolor{blue}{777924}^2 \ (5.882)$	$123432 \ 0206119^2 + 1979802000^2 = \textcolor{red}{1234321} \textcolor{blue}{793881}^2 \ (5.891)$
$0220311^2 + 1766000^2 = \textcolor{red}{1} \textcolor{blue}{779689}^2$	$0204336^2 + 1784000^2 = \textcolor{red}{1} \textcolor{blue}{795664}^2$
$12 \ 0220311^2 + 19426000^2 = \textcolor{red}{121} \textcolor{blue}{779689}^2$	$12 \ 0204336^2 + 19624000^2 = \textcolor{red}{121} \textcolor{blue}{795664}^2$
$1232 \ 0220311^2 + 196026000^2 = \textcolor{red}{12321} \textcolor{blue}{779689}^2$	$1232 \ 0204336^2 + 198024000^2 = \textcolor{red}{12321} \textcolor{blue}{795664}^2$
$123432 \ 0220311^2 + 1962026000^2 = \textcolor{red}{1234321} \textcolor{blue}{779689}^2 \ (5.883)$	$123432 \ 0204336^2 + 1982024000^2 = \textcolor{red}{1234321} \textcolor{blue}{795664}^2 \ (5.892)$
$0218544^2 + 1768000^2 = \textcolor{red}{1} \textcolor{blue}{781456}^2$	$0202551^2 + 1786000^2 = \textcolor{red}{1} \textcolor{blue}{797449}^2$
$12 \ 0218544^2 + 19448000^2 = \textcolor{red}{121} \textcolor{blue}{781456}^2$	$12 \ 0202551^2 + 19646000^2 = \textcolor{red}{121} \textcolor{blue}{797449}^2$
$1232 \ 0218544^2 + 196248000^2 = \textcolor{red}{12321} \textcolor{blue}{781456}^2$	$1232 \ 0202551^2 + 198246000^2 = \textcolor{red}{12321} \textcolor{blue}{797449}^2$
$123432 \ 0218544^2 + 1964248000^2 = \textcolor{red}{1234321} \textcolor{blue}{781456}^2 \ (5.884)$	$123432 \ 0202551^2 + 1984246000^2 = \textcolor{red}{1234321} \textcolor{blue}{797449}^2 \ (5.893)$
$0216775^2 + 1770000^2 = \textcolor{red}{1} \textcolor{blue}{783225}^2$	$0200764^2 + 1788000^2 = \textcolor{red}{1} \textcolor{blue}{799236}^2$
$12 \ 0216775^2 + 19470000^2 = \textcolor{red}{121} \textcolor{blue}{783225}^2$	$12 \ 0200764^2 + 19668000^2 = \textcolor{red}{121} \textcolor{blue}{799236}^2$
$1232 \ 0216775^2 + 196470000^2 = \textcolor{red}{12321} \textcolor{blue}{783225}^2$	$1232 \ 0200764^2 + 198468000^2 = \textcolor{red}{12321} \textcolor{blue}{799236}^2$
$123432 \ 0216775^2 + 1966470000^2 = \textcolor{red}{1234321} \textcolor{blue}{783225}^2 \ (5.885)$	$123432 \ 0200764^2 + 1986468000^2 = \textcolor{red}{1234321} \textcolor{blue}{799236}^2 \ (5.894)$
$0215004^2 + 1772000^2 = \textcolor{red}{1} \textcolor{blue}{784996}^2$	$0198975^2 + 1790000^2 = \textcolor{red}{1} \textcolor{blue}{801025}^2$
$12 \ 0215004^2 + 19492000^2 = \textcolor{red}{121} \textcolor{blue}{784996}^2$	$12 \ 0198975^2 + 19690000^2 = \textcolor{red}{121} \textcolor{blue}{801025}^2$
$1232 \ 0215004^2 + 196692000^2 = \textcolor{red}{12321} \textcolor{blue}{784996}^2$	$1232 \ 0198975^2 + 198690000^2 = \textcolor{red}{12321} \textcolor{blue}{801025}^2$
$123432 \ 0215004^2 + 1968692000^2 = \textcolor{red}{1234321} \textcolor{blue}{784996}^2 \ (5.886)$	$123432 \ 0198975^2 + 1988690000^2 = \textcolor{red}{1234321} \textcolor{blue}{801025}^2 \ (5.895)$
$0213231^2 + 1774000^2 = \textcolor{red}{1} \textcolor{blue}{786769}^2$	$0197184^2 + 1792000^2 = \textcolor{red}{1} \textcolor{blue}{802816}^2$
$12 \ 0213231^2 + 19514000^2 = \textcolor{red}{121} \textcolor{blue}{786769}^2$	$12 \ 0197184^2 + 19712000^2 = \textcolor{red}{121} \textcolor{blue}{802816}^2$
$1232 \ 0213231^2 + 196914000^2 = \textcolor{red}{12321} \textcolor{blue}{786769}^2$	$1232 \ 0197184^2 + 198912000^2 = \textcolor{red}{12321} \textcolor{blue}{802816}^2$
$123432 \ 0213231^2 + 1970914000^2 = \textcolor{red}{1234321} \textcolor{blue}{786769}^2 \ (5.887)$	$123432 \ 0197184^2 + 1990912000^2 = \textcolor{red}{1234321} \textcolor{blue}{802816}^2 \ (5.896)$
$0211456^2 + 1776000^2 = \textcolor{red}{1} \textcolor{blue}{788544}^2$	$0195391^2 + 1794000^2 = \textcolor{red}{1} \textcolor{blue}{804609}^2$
$12 \ 0211456^2 + 19536000^2 = \textcolor{red}{121} \textcolor{blue}{788544}^2$	$12 \ 0195391^2 + 19734000^2 = \textcolor{red}{121} \textcolor{blue}{804609}^2$
$1232 \ 0211456^2 + 197136000^2 = \textcolor{red}{12321} \textcolor{blue}{788544}^2$	$1232 \ 0195391^2 + 199134000^2 = \textcolor{red}{12321} \textcolor{blue}{804609}^2$
$123432 \ 0211456^2 + 1973136000^2 = \textcolor{red}{1234321} \textcolor{blue}{788544}^2 \ (5.888)$	$123432 \ 0195391^2 + 1993134000^2 = \textcolor{red}{1234321} \textcolor{blue}{804609}^2 \ (5.897)$
$0209679^2 + 1778000^2 = \textcolor{red}{1} \textcolor{blue}{790321}^2$	$0193596^2 + 1796000^2 = \textcolor{red}{1} \textcolor{blue}{806404}^2$
$12 \ 0209679^2 + 19558000^2 = \textcolor{red}{121} \textcolor{blue}{790321}^2$	$12 \ 0193596^2 + 19756000^2 = \textcolor{red}{121} \textcolor{blue}{806404}^2$
$1232 \ 0209679^2 + 197358000^2 = \textcolor{red}{12321} \textcolor{blue}{790321}^2$	$1232 \ 0193596^2 + 199356000^2 = \textcolor{red}{12321} \textcolor{blue}{806404}^2$
$123432 \ 0209679^2 + 1975358000^2 = \textcolor{red}{1234321} \textcolor{blue}{790321}^2 \ (5.889)$	$123432 \ 0193596^2 + 1995356000^2 = \textcolor{red}{1234321} \textcolor{blue}{806404}^2 \ (5.898)$
$0207900^2 + 1780000^2 = \textcolor{red}{1} \textcolor{blue}{792100}^2$	$0191799^2 + 1798000^2 = \textcolor{red}{1} \textcolor{blue}{808201}^2$
$12 \ 0207900^2 + 19580000^2 = \textcolor{red}{121} \textcolor{blue}{792100}^2$	$12 \ 0191799^2 + 19778000^2 = \textcolor{red}{121} \textcolor{blue}{808201}^2$
$1232 \ 0207900^2 + 197580000^2 = \textcolor{red}{12321} \textcolor{blue}{792100}^2$	$1232 \ 0191799^2 + 199578000^2 = \textcolor{red}{12321} \textcolor{blue}{808201}^2$
$123432 \ 0207900^2 + 197758000^2 = \textcolor{red}{1234321} \textcolor{blue}{792100}^2 \ (5.890)$	$123432 \ 0191799^2 + 1997578000^2 = \textcolor{red}{1234321} \textcolor{blue}{808201}^2 \ (5.899)$

5.10 For $n = 900, 901, 901, \dots, 997, 998, 999$:

Let's consider

$$m = 1000, 11000, 111000, 1111000, 11111000, 111111000, 1111111000, 11111111000$$

in (1.1), then for each value of $n = 900, 901, 901, \dots, 997, 998, 999$; there are 100 *palindromic-type pandigital Pythagorean patterns* given below. In each case, only first four values are written. The other 5 values can be written on similar lines as done in subsection 5.1.1.

$0190000^2 + 1800000^2 = 1810000^2$	$0177351^2 + 1814000^2 = 1822649^2$
$120190000^2 + 19800000^2 = 121810000^2$	$120177351^2 + 19954000^2 = 121822649^2$
$12320190000^2 + 199800000^2 = 12321810000^2$	$12320177351^2 + 201354000^2 = 12321822649^2$
$1234320190000^2 + 1999800000^2 = 1234321810000^2$ (5.900)	$1234320177351^2 + 2015354000^2 = 1234321822649^2$ (5.907)
$0188199^2 + 1802000^2 = 1811801^2$	$0175536^2 + 1816000^2 = 1824464^2$
$120188199^2 + 19822000^2 = 121811801^2$	$120175536^2 + 19976000^2 = 121824464^2$
$12320188199^2 + 200022000^2 = 12321811801^2$	$12320175536^2 + 201576000^2 = 12321824464^2$
$1234320188199^2 + 2002022000^2 = 1234321811801^2$ (5.901)	$1234320175536^2 + 2017576000^2 = 1234321824464^2$ (5.908)
$0186396^2 + 1804000^2 = 1813604^2$	$0173719^2 + 1818000^2 = 1826281^2$
$120186396^2 + 19844000^2 = 121813604^2$	$120173719^2 + 19998000^2 = 121826281^2$
$12320186396^2 + 200244000^2 = 12321813604^2$	$12320173719^2 + 201798000^2 = 12321826281^2$
$1234320186396^2 + 2004244000^2 = 1234321813604^2$ (5.902)	$1234320173719^2 + 2019798000^2 = 1234321826281^2$ (5.909)
$0184591^2 + 1806000^2 = 1815409^2$	$0171900^2 + 1820000^2 = 1828100^2$
$120184591^2 + 19866000^2 = 121815409^2$	$120171900^2 + 20020000^2 = 121828100^2$
$12320184591^2 + 200466000^2 = 12321815409^2$	$12320171900^2 + 202020000^2 = 12321828100^2$
$1234320184591^2 + 2006466000^2 = 1234321815409^2$ (5.903)	$1234320171900^2 + 2022020000^2 = 1234321828100^2$ (5.910)
$0182784^2 + 1808000^2 = 1817216^2$	$0170079^2 + 1822000^2 = 1829921^2$
$120182784^2 + 19888000^2 = 121817216^2$	$120170079^2 + 20042000^2 = 121829921^2$
$12320182784^2 + 200688000^2 = 12321817216^2$	$12320170079^2 + 202242000^2 = 12321829921^2$
$1234320182784^2 + 2008688000^2 = 1234321817216^2$ (5.904)	$1234320170079^2 + 2024242000^2 = 1234321829921^2$ (5.911)
$0180975^2 + 1810000^2 = 1819025^2$	$0168256^2 + 1824000^2 = 1831744^2$
$120180975^2 + 19910000^2 = 121819025^2$	$120168256^2 + 20064000^2 = 121831744^2$
$12320180975^2 + 200910000^2 = 12321819025^2$	$12320168256^2 + 202464000^2 = 12321831744^2$
$1234320180975^2 + 2010910000^2 = 1234321819025^2$ (5.905)	$1234320168256^2 + 2026464000^2 = 1234321831744^2$ (5.912)
$0179164^2 + 1812000^2 = 1820836^2$	$0166431^2 + 1826000^2 = 1833569^2$
$120179164^2 + 19932000^2 = 121820836^2$	$120166431^2 + 20086000^2 = 121833569^2$
$12320179164^2 + 201132000^2 = 12321820836^2$	$12320166431^2 + 202686000^2 = 12321833569^2$
$1234320179164^2 + 2013132000^2 = 1234321820836^2$ (5.906)	$1234320166431^2 + 2028686000^2 = 1234321833569^2$ (5.913)

$$\begin{aligned}
& 0164604^2 + 1828000^2 = \mathbf{1} 835396^2 \\
& \mathbf{12} 0164604^2 + 20108000^2 = \mathbf{121} 835396^2 \\
& \mathbf{1232} 0164604^2 + 202908000^2 = \mathbf{12321} 835396^2 \\
& \mathbf{123432} 0164604^2 + 2030908000^2 = \mathbf{1234321} 835396^2 \quad (5.914) \\
& \\
& 0162775^2 + 1830000^2 = \mathbf{1} 837225^2 \\
& \mathbf{12} 0162775^2 + 20130000^2 = \mathbf{121} 837225^2 \\
& \mathbf{1232} 0162775^2 + 203130000^2 = \mathbf{12321} 837225^2 \\
& \mathbf{123432} 0162775^2 + 2033130000^2 = \mathbf{1234321} 837225^2 \quad (5.915) \\
& \\
& 0160944^2 + 1832000^2 = \mathbf{1} 839056^2 \\
& \mathbf{12} 0160944^2 + 20152000^2 = \mathbf{121} 839056^2 \\
& \mathbf{1232} 0160944^2 + 203352000^2 = \mathbf{12321} 839056^2 \\
& \mathbf{123432} 0160944^2 + 2035352000^2 = \mathbf{1234321} 839056^2 \quad (5.916) \\
& \\
& 0159111^2 + 1834000^2 = \mathbf{1} 840889^2 \\
& \mathbf{12} 0159111^2 + 20174000^2 = \mathbf{121} 840889^2 \\
& \mathbf{1232} 0159111^2 + 203574000^2 = \mathbf{12321} 840889^2 \\
& \mathbf{123432} 0159111^2 + 2037574000^2 = \mathbf{1234321} 840889^2 \quad (5.917) \\
& \\
& 0157276^2 + 1836000^2 = \mathbf{1} 842724^2 \\
& \mathbf{12} 0157276^2 + 20196000^2 = \mathbf{121} 842724^2 \\
& \mathbf{1232} 0157276^2 + 203796000^2 = \mathbf{12321} 842724^2 \\
& \mathbf{123432} 0157276^2 + 2039796000^2 = \mathbf{1234321} 842724^2 \quad (5.918) \\
& \\
& 0155439^2 + 1838000^2 = \mathbf{1} 844561^2 \\
& \mathbf{12} 0155439^2 + 20218000^2 = \mathbf{121} 844561^2 \\
& \mathbf{1232} 0155439^2 + 204018000^2 = \mathbf{12321} 844561^2 \\
& \mathbf{123432} 0155439^2 + 2042018000^2 = \mathbf{1234321} 844561^2 \quad (5.919) \\
& \\
& 0153600^2 + 1840000^2 = \mathbf{1} 846400^2 \\
& \mathbf{12} 0153600^2 + 20240000^2 = \mathbf{121} 846400^2 \\
& \mathbf{1232} 0153600^2 + 204240000^2 = \mathbf{12321} 846400^2 \\
& \mathbf{123432} 0153600^2 + 2044240000^2 = \mathbf{1234321} 846400^2 \quad (5.920) \\
& \\
& 0151759^2 + 1842000^2 = \mathbf{1} 848241^2 \\
& \mathbf{12} 0151759^2 + 20262000^2 = \mathbf{121} 848241^2 \\
& \mathbf{1232} 0151759^2 + 204462000^2 = \mathbf{12321} 848241^2 \\
& \mathbf{123432} 0151759^2 + 2046462000^2 = \mathbf{1234321} 848241^2 \quad (5.921) \\
& \\
& 0149916^2 + 1844000^2 = \mathbf{1} 850084^2 \\
& \mathbf{12} 0149916^2 + 20284000^2 = \mathbf{121} 850084^2 \\
& \mathbf{1232} 0149916^2 + 204684000^2 = \mathbf{12321} 850084^2 \\
& \mathbf{123432} 0149916^2 + 2048684000^2 = \mathbf{1234321} 850084^2 \quad (5.922)
\end{aligned}$$

$$\begin{aligned}
& 0133239^2 + 1862000^2 = \mathbf{1} 866761^2 \\
& \mathbf{12} 0133239^2 + 20482000^2 = \mathbf{121} 866761^2 \\
& \mathbf{1232} 0133239^2 + 206682000^2 = \mathbf{12321} 866761^2 \\
& \mathbf{123432} 0133239^2 + 2068682000^2 = \mathbf{1234321} 866761^2 \quad (5.931) \\
& \\
& 0131376^2 + 1864000^2 = \mathbf{1} 868624^2 \\
& \mathbf{12} 0131376^2 + 20504000^2 = \mathbf{121} 868624^2 \\
& \mathbf{1232} 0131376^2 + 206904000^2 = \mathbf{12321} 868624^2 \\
& \mathbf{123432} 0131376^2 + 2070904000^2 = \mathbf{1234321} 868624^2 \quad (5.932) \\
& \\
& 00129511^2 + 1866000^2 = \mathbf{1} 870489^2 \\
& \mathbf{12} 0129511^2 + 20526000^2 = \mathbf{121} 870489^2 \\
& \mathbf{1232} 0129511^2 + 207126000^2 = \mathbf{12321} 870489^2 \\
& \mathbf{123432} 0129511^2 + 2073126000^2 = \mathbf{1234321} 870489^2 \quad (5.933) \\
& \\
& 00127644^2 + 1868000^2 = \mathbf{1} 872356^2 \\
& \mathbf{12} 0127644^2 + 20548000^2 = \mathbf{121} 872356^2 \\
& \mathbf{1232} 0127644^2 + 207348000^2 = \mathbf{12321} 872356^2 \\
& \mathbf{123432} 0127644^2 + 2075348000^2 = \mathbf{1234321} 872356^2 \quad (5.934) \\
& \\
& 00125775^2 + 1870000^2 = \mathbf{1} 874225^2 \\
& \mathbf{12} 0125775^2 + 20570000^2 = \mathbf{121} 874225^2 \\
& \mathbf{1232} 0125775^2 + 207570000^2 = \mathbf{12321} 874225^2 \\
& \mathbf{123432} 0125775^2 + 2077570000^2 = \mathbf{1234321} 874225^2 \quad (5.935) \\
& \\
& 00123904^2 + 1872000^2 = \mathbf{1} 876096^2 \\
& \mathbf{12} 0123904^2 + 20592000^2 = \mathbf{121} 876096^2 \\
& \mathbf{1232} 0123904^2 + 207792000^2 = \mathbf{12321} 876096^2 \\
& \mathbf{123432} 0123904^2 + 2079792000^2 = \mathbf{1234321} 876096^2 \quad (5.936) \\
& \\
& 00122031^2 + 1874000^2 = \mathbf{1} 877969^2 \\
& \mathbf{12} 0122031^2 + 20614000^2 = \mathbf{121} 877969^2 \\
& \mathbf{1232} 0122031^2 + 208014000^2 = \mathbf{12321} 877969^2 \\
& \mathbf{123432} 0122031^2 + 2082014000^2 = \mathbf{1234321} 877969^2 \quad (5.937) \\
& \\
& 00120156^2 + 1876000^2 = \mathbf{1} 879844^2 \\
& \mathbf{12} 0120156^2 + 20636000^2 = \mathbf{121} 879844^2 \\
& \mathbf{1232} 0120156^2 + 208236000^2 = \mathbf{12321} 879844^2 \\
& \mathbf{123432} 0120156^2 + 2084236000^2 = \mathbf{1234321} 879844^2 \quad (5.938) \\
& \\
& 00118279^2 + 1878000^2 = \mathbf{1} 881721^2 \\
& \mathbf{12} 0118279^2 + 20658000^2 = \mathbf{121} 881721^2 \\
& \mathbf{1232} 0118279^2 + 208458000^2 = \mathbf{12321} 881721^2 \\
& \mathbf{123432} 0118279^2 + 2086458000^2 = \mathbf{1234321} 881721^2 \quad (5.939)
\end{aligned}$$

$$\begin{aligned}
& 00101296^2 + 1896000^2 = \mathbf{1} 898704^2 \\
& \mathbf{12} 0101296^2 + 20856000^2 = \mathbf{121} 898704^2 \\
& \mathbf{1232} 0101296^2 + 210456000^2 = \mathbf{12321} 898704^2 \\
& \mathbf{123432} 0101296^2 + 2106456000^2 = \mathbf{1234321} 898704^2 \quad (5.948) \\
& 0099399^2 + 1898000^2 = \mathbf{1} 900601^2 \\
& \mathbf{12} 0099399^2 + 20878000^2 = \mathbf{121} 900601^2 \\
& \mathbf{1232} 0099399^2 + 210678000^2 = \mathbf{12321} 900601^2 \\
& \mathbf{123432} 0099399^2 + 2108678000^2 = \mathbf{1234321} 900601^2 \quad (5.949) \\
& 0097500^2 + 1900000^2 = \mathbf{1} 902500^2 \\
& \mathbf{12} 0097500^2 + 20900000^2 = \mathbf{121} 902500^2 \\
& \mathbf{1232} 0097500^2 + 210900000^2 = \mathbf{12321} 902500^2 \\
& \mathbf{123432} 0097500^2 + 2110900000^2 = \mathbf{1234321} 902500^2 \quad (5.950) \\
& 0095599^2 + 1902000^2 = \mathbf{1} 904401^2 \\
& \mathbf{12} 0095599^2 + 20922000^2 = \mathbf{121} 904401^2 \\
& \mathbf{1232} 0095599^2 + 211122000^2 = \mathbf{12321} 904401^2 \\
& \mathbf{123432} 0095599^2 + 2113122000^2 = \mathbf{1234321} 904401^2 \quad (5.951) \\
& 0093696^2 + 1904000^2 = \mathbf{1} 906304^2 \\
& \mathbf{12} 0093696^2 + 20944000^2 = \mathbf{121} 906304^2 \\
& \mathbf{1232} 0093696^2 + 211344000^2 = \mathbf{12321} 906304^2 \\
& \mathbf{123432} 0093696^2 + 2115344000^2 = \mathbf{1234321} 906304^2 \quad (5.952) \\
& 0091791^2 + 1906000^2 = \mathbf{1} 908209^2 \\
& \mathbf{12} 0091791^2 + 20966000^2 = \mathbf{121} 908209^2 \\
& \mathbf{1232} 0091791^2 + 211566000^2 = \mathbf{12321} 908209^2 \\
& \mathbf{123432} 0091791^2 + 2117566000^2 = \mathbf{1234321} 908209^2 \quad (5.953) \\
& 0089884^2 + 1908000^2 = \mathbf{1} 910116^2 \\
& \mathbf{12} 0089884^2 + 20988000^2 = \mathbf{121} 910116^2 \\
& \mathbf{1232} 0089884^2 + 211788000^2 = \mathbf{12321} 910116^2 \\
& \mathbf{123432} 0089884^2 + 2119788000^2 = \mathbf{1234321} 910116^2 \quad (5.954) \\
& 0087975^2 + 1910000^2 = \mathbf{1} 912025^2 \\
& \mathbf{12} 0087975^2 + 21010000^2 = \mathbf{121} 912025^2 \\
& \mathbf{1232} 0087975^2 + 212010000^2 = \mathbf{12321} 912025^2 \\
& \mathbf{123432} 0087975^2 + 2122010000^2 = \mathbf{1234321} 912025^2 \quad (5.955) \\
& 0086064^2 + 1912000^2 = \mathbf{1} 913936^2 \\
& \mathbf{12} 0086064^2 + 21032000^2 = \mathbf{121} 913936^2 \\
& \mathbf{1232} 0086064^2 + 212232000^2 = \mathbf{12321} 913936^2 \\
& \mathbf{123432} 0086064^2 + 2124232000^2 = \mathbf{1234321} 913936^2 \quad (5.956)
\end{aligned}$$

$$\begin{aligned}
& 0084151^2 + 1914000^2 = \mathbf{1} 915849^2 \\
& \mathbf{12} 0084151^2 + 21054000^2 = \mathbf{121} 915849^2 \\
& \mathbf{1232} 0084151^2 + 212454000^2 = \mathbf{12321} 915849^2 \\
& \mathbf{123432} 0084151^2 + 2126454000^2 = \mathbf{1234321} 915849^2 \quad (5.957) \\
& 0082236^2 + 1916000^2 = \mathbf{1} 917764^2 \\
& \mathbf{12} 0082236^2 + 21076000^2 = \mathbf{121} 917764^2 \\
& \mathbf{1232} 0082236^2 + 212676000^2 = \mathbf{12321} 917764^2 \\
& \mathbf{123432} 0082236^2 + 2128676000^2 = \mathbf{1234321} 917764^2 \quad (5.958) \\
& 0080319^2 + 1918000^2 = \mathbf{1} 919681^2 \\
& \mathbf{12} 0080319^2 + 21098000^2 = \mathbf{121} 919681^2 \\
& \mathbf{1232} 0080319^2 + 212898000^2 = \mathbf{12321} 919681^2 \\
& \mathbf{123432} 0080319^2 + 2130898000^2 = \mathbf{1234321} 919681^2 \quad (5.959) \\
& 0078400^2 + 1920000^2 = \mathbf{1} 921600^2 \\
& \mathbf{12} 0078400^2 + 21120000^2 = \mathbf{121} 921600^2 \\
& \mathbf{1232} 0078400^2 + 213120000^2 = \mathbf{12321} 921600^2 \\
& \mathbf{123432} 0078400^2 + 2133120000^2 = \mathbf{1234321} 921600^2 \quad (5.960) \\
& 0076479^2 + 1922000^2 = \mathbf{1} 923521^2 \\
& \mathbf{12} 0076479^2 + 21142000^2 = \mathbf{121} 923521^2 \\
& \mathbf{1232} 0076479^2 + 213342000^2 = \mathbf{12321} 923521^2 \\
& \mathbf{123432} 0076479^2 + 2135342000^2 = \mathbf{1234321} 923521^2 \quad (5.961) \\
& 0074556^2 + 1924000^2 = \mathbf{1} 925444^2 \\
& \mathbf{12} 0074556^2 + 21164000^2 = \mathbf{121} 925444^2 \\
& \mathbf{1232} 0074556^2 + 213564000^2 = \mathbf{12321} 925444^2 \\
& \mathbf{123432} 0074556^2 + 2137564000^2 = \mathbf{1234321} 925444^2 \quad (5.962) \\
& 0072631^2 + 1926000^2 = \mathbf{1} 927369^2 \\
& \mathbf{12} 0072631^2 + 21186000^2 = \mathbf{121} 927369^2 \\
& \mathbf{1232} 0072631^2 + 213786000^2 = \mathbf{12321} 927369^2 \\
& \mathbf{123432} 0072631^2 + 2139786000^2 = \mathbf{1234321} 927369^2 \quad (5.963) \\
& 0070704^2 + 1928000^2 = \mathbf{1} 929296^2 \\
& \mathbf{12} 0070704^2 + 21208000^2 = \mathbf{121} 929296^2 \\
& \mathbf{1232} 0070704^2 + 214008000^2 = \mathbf{12321} 929296^2 \\
& \mathbf{123432} 0070704^2 + 2142008000^2 = \mathbf{1234321} 929296^2 \quad (5.964)
\end{aligned}$$

$$\begin{aligned}
& 0068775^2 + 1930000^2 = \mathbf{1} 931225^2 \\
& \mathbf{12} 0068775^2 + 21230000^2 = \mathbf{121} 931225^2 \\
& \mathbf{1232} 0068775^2 + 214230000^2 = \mathbf{12321} 931225^2 \\
& \mathbf{123432} 0068775^2 + 2144230000^2 = \mathbf{1234321} 931225^2 \quad (5.965) \\
& \\
& 0066844^2 + 1932000^2 = \mathbf{1} 933156^2 \\
& \mathbf{12} 0066844^2 + 21252000^2 = \mathbf{121} 933156^2 \\
& \mathbf{1232} 0066844^2 + 214452000^2 = \mathbf{12321} 933156^2 \\
& \mathbf{123432} 0066844^2 + 2146452000^2 = \mathbf{1234321} 933156^2 \quad (5.966) \\
& \\
& 0064911^2 + 1934000^2 = \mathbf{1} 935089^2 \\
& \mathbf{12} 0064911^2 + 21274000^2 = \mathbf{121} 935089^2 \\
& \mathbf{1232} 0064911^2 + 214674000^2 = \mathbf{12321} 935089^2 \\
& \mathbf{123432} 0064911^2 + 2148674000^2 = \mathbf{1234321} 935089^2 \quad (5.967) \\
& \\
& 0062976^2 + 1936000^2 = \mathbf{1} 937024^2 \\
& \mathbf{12} 0062976^2 + 21296000^2 = \mathbf{121} 937024^2 \\
& \mathbf{1232} 0062976^2 + 214896000^2 = \mathbf{12321} 937024^2 \\
& \mathbf{123432} 0062976^2 + 2150896000^2 = \mathbf{1234321} 937024^2 \quad (5.968) \\
& \\
& 0061039^2 + 1938000^2 = \mathbf{1} 938961^2 \\
& \mathbf{12} 0061039^2 + 21318000^2 = \mathbf{121} 938961^2 \\
& \mathbf{1232} 0061039^2 + 215118000^2 = \mathbf{12321} 938961^2 \\
& \mathbf{123432} 0061039^2 + 2153118000^2 = \mathbf{1234321} 938961^2 \quad (5.969) \\
& \\
& 0059100^2 + 1940000^2 = \mathbf{1} 940900^2 \\
& \mathbf{12} 0059100^2 + 21340000^2 = \mathbf{121} 940900^2 \\
& \mathbf{1232} 0059100^2 + 215340000^2 = \mathbf{12321} 940900^2 \\
& \mathbf{123432} 0059100^2 + 2155340000^2 = \mathbf{1234321} 940900^2 \quad (5.970) \\
& \\
& 0057159^2 + 1942000^2 = \mathbf{1} 942841^2 \\
& \mathbf{12} 0057159^2 + 21362000^2 = \mathbf{121} 942841^2 \\
& \mathbf{1232} 0057159^2 + 215562000^2 = \mathbf{12321} 942841^2 \\
& \mathbf{123432} 0057159^2 + 2157562000^2 = \mathbf{1234321} 942841^2 \quad (5.971) \\
& \\
& 0055216^2 + 1944000^2 = \mathbf{1} 944784^2 \\
& \mathbf{12} 0055216^2 + 21384000^2 = \mathbf{121} 944784^2 \\
& \mathbf{1232} 0055216^2 + 215784000^2 = \mathbf{12321} 944784^2 \\
& \mathbf{123432} 0055216^2 + 2159784000^2 = \mathbf{1234321} 944784^2 \quad (5.972) \\
& \\
& 0053271^2 + 1946000^2 = \mathbf{1} 946729^2 \\
& \mathbf{12} 0053271^2 + 21406000^2 = \mathbf{121} 946729^2 \\
& \mathbf{1232} 0053271^2 + 216006000^2 = \mathbf{12321} 946729^2 \\
& \mathbf{123432} 0053271^2 + 2162006000^2 = \mathbf{1234321} 946729^2 \quad (5.973) \\
& \\
& 0051324^2 + 1948000^2 = \mathbf{1} 948676^2 \\
& \mathbf{12} 0051324^2 + 21428000^2 = \mathbf{121} 948676^2 \\
& \mathbf{1232} 0051324^2 + 216228000^2 = \mathbf{12321} 948676^2 \\
& \mathbf{123432} 0051324^2 + 2164228000^2 = \mathbf{1234321} 948676^2 \quad (5.974) \\
& \\
& 0049375^2 + 1950000^2 = \mathbf{1} 950625^2 \\
& \mathbf{12} 0049375^2 + 21450000^2 = \mathbf{121} 950625^2 \\
& \mathbf{1232} 0049375^2 + 216450000^2 = \mathbf{12321} 950625^2 \\
& \mathbf{123432} 0049375^2 + 2166450000^2 = \mathbf{1234321} 950625^2 \quad (5.975) \\
& \\
& 0047424^2 + 1952000^2 = \mathbf{1} 952576^2 \\
& \mathbf{12} 0047424^2 + 21472000^2 = \mathbf{121} 952576^2 \\
& \mathbf{1232} 0047424^2 + 216672000^2 = \mathbf{12321} 952576^2 \\
& \mathbf{123432} 0047424^2 + 2168672000^2 = \mathbf{1234321} 952576^2 \quad (5.976) \\
& \\
& 0045471^2 + 1954000^2 = \mathbf{1} 954529^2 \\
& \mathbf{12} 0045471^2 + 21494000^2 = \mathbf{121} 954529^2 \\
& \mathbf{1232} 0045471^2 + 216894000^2 = \mathbf{12321} 954529^2 \\
& \mathbf{123432} 0045471^2 + 2170894000^2 = \mathbf{1234321} 954529^2 \quad (5.977) \\
& \\
& 0043516^2 + 1956000^2 = \mathbf{1} 956484^2 \\
& \mathbf{12} 0043516^2 + 21516000^2 = \mathbf{121} 956484^2 \\
& \mathbf{1232} 0043516^2 + 217116000^2 = \mathbf{12321} 956484^2 \\
& \mathbf{123432} 0043516^2 + 2173116000^2 = \mathbf{1234321} 956484^2 \quad (5.978) \\
& \\
& 0041559^2 + 1958000^2 = \mathbf{1} 958441^2 \\
& \mathbf{12} 0041559^2 + 21538000^2 = \mathbf{121} 958441^2 \\
& \mathbf{1232} 0041559^2 + 217338000^2 = \mathbf{12321} 958441^2 \\
& \mathbf{123432} 0041559^2 + 2175338000^2 = \mathbf{1234321} 958441^2 \quad (5.979) \\
& \\
& 0039600^2 + 1960000^2 = \mathbf{1} 960400^2 \\
& \mathbf{12} 0039600^2 + 21560000^2 = \mathbf{121} 960400^2 \\
& \mathbf{1232} 0039600^2 + 217560000^2 = \mathbf{12321} 960400^2 \\
& \mathbf{123432} 0039600^2 + 2177560000^2 = \mathbf{1234321} 960400^2 \quad (5.980) \\
& \\
& 0037639^2 + 1962000^2 = \mathbf{1} 962361^2 \\
& \mathbf{12} 0037639^2 + 21582000^2 = \mathbf{121} 962361^2 \\
& \mathbf{1232} 0037639^2 + 217782000^2 = \mathbf{12321} 962361^2 \\
& \mathbf{123432} 0037639^2 + 2179782000^2 = \mathbf{1234321} 962361^2 \quad (5.981)
\end{aligned}$$

$0035676^2 + 1964000^2 = \textcolor{red}{1} 964324^2$	$0017919^2 + 1982000^2 = \textcolor{red}{1} 982081^2$
$12\ 0035676^2 + 21604000^2 = \textcolor{red}{121} 964324^2$	$12\ 0017919^2 + 21802000^2 = \textcolor{red}{121} 982081^2$
$1232\ 0035676^2 + 218004000^2 = \textcolor{red}{12321} 964324^2$	$1232\ 0017919^2 + 220002000^2 = \textcolor{red}{12321} 982081^2$
$123432\ 0035676^2 + 2182004000^2 = \textcolor{red}{1234321} 964324^2 \ (5.982)$	$123432\ 0017919^2 + 2202002000^2 = \textcolor{red}{1234321} 982081^2 \ (5.991)$
$0033711^2 + 1966000^2 = \textcolor{red}{1} 966289^2$	$0015936^2 + 1984000^2 = \textcolor{red}{1} 984064^2$
$12\ 0033711^2 + 21626000^2 = \textcolor{red}{121} 966289^2$	$12\ 0015936^2 + 21824000^2 = \textcolor{red}{121} 984064^2$
$1232\ 0033711^2 + 218226000^2 = \textcolor{red}{12321} 966289^2$	$1232\ 0015936^2 + 220224000^2 = \textcolor{red}{12321} 984064^2$
$123432\ 0033711^2 + 2184226000^2 = \textcolor{red}{1234321} 966289^2 \ (5.983)$	$123432\ 0015936^2 + 2204224000^2 = \textcolor{red}{1234321} 984064^2 \ (5.992)$
$0031744^2 + 1968000^2 = \textcolor{red}{1} 968256^2$	$0013951^2 + 1986000^2 = \textcolor{red}{1} 986049^2$
$12\ 0031744^2 + 21648000^2 = \textcolor{red}{121} 968256^2$	$12\ 0013951^2 + 21846000^2 = \textcolor{red}{121} 986049^2$
$1232\ 0031744^2 + 218448000^2 = \textcolor{red}{12321} 968256^2$	$1232\ 0013951^2 + 220446000^2 = \textcolor{red}{12321} 986049^2$
$123432\ 0031744^2 + 2186448000^2 = \textcolor{red}{1234321} 968256^2 \ (5.984)$	$123432\ 0013951^2 + 2206446000^2 = \textcolor{red}{1234321} 986049^2 \ (5.993)$
$0029775^2 + 1970000^2 = \textcolor{red}{1} 970225^2$	$0011964^2 + 1988000^2 = \textcolor{red}{1} 988036^2$
$12\ 0029775^2 + 21670000^2 = \textcolor{red}{121} 970225^2$	$12\ 0011964^2 + 21868000^2 = \textcolor{red}{121} 988036^2$
$1232\ 0029775^2 + 218670000^2 = \textcolor{red}{12321} 970225^2$	$1232\ 0011964^2 + 220668000^2 = \textcolor{red}{12321} 988036^2$
$123432\ 0029775^2 + 2188670000^2 = \textcolor{red}{1234321} 970225^2 \ (5.985)$	$123432\ 0011964^2 + 2208668000^2 = \textcolor{red}{1234321} 988036^2 \ (5.994)$
$0027804^2 + 1972000^2 = \textcolor{red}{1} 972196^2$	$0009975^2 + 1990000^2 = \textcolor{red}{1} 990025^2$
$12\ 0027804^2 + 21692000^2 = \textcolor{red}{121} 972196^2$	$12\ 0009975^2 + 21890000^2 = \textcolor{red}{121} 990025^2$
$1232\ 0027804^2 + 218892000^2 = \textcolor{red}{12321} 972196^2$	$1232\ 0009975^2 + 220890000^2 = \textcolor{red}{12321} 990025^2$
$123432\ 0027804^2 + 2190892000^2 = \textcolor{red}{1234321} 972196^2 \ (5.986)$	$123432\ 0009975^2 + 2210890000^2 = \textcolor{red}{1234321} 990025^2 \ (5.995)$
$0025831^2 + 1974000^2 = \textcolor{red}{1} 974169^2$	$0007984^2 + 1992000^2 = \textcolor{red}{1} 992016^2$
$12\ 0025831^2 + 21714000^2 = \textcolor{red}{121} 974169^2$	$12\ 0007984^2 + 21912000^2 = \textcolor{red}{121} 992016^2$
$1232\ 0025831^2 + 219114000^2 = \textcolor{red}{12321} 974169^2$	$1232\ 0007984^2 + 221112000^2 = \textcolor{red}{12321} 992016^2$
$123432\ 0025831^2 + 2193114000^2 = \textcolor{red}{1234321} 974169^2 \ (5.987)$	$123432\ 0007984^2 + 2213112000^2 = \textcolor{red}{1234321} 992016^2 \ (5.996)$
$0023856^2 + 1976000^2 = \textcolor{red}{1} 976144^2$	$0005991^2 + 1994000^2 = \textcolor{red}{1} 994009^2$
$12\ 0023856^2 + 21736000^2 = \textcolor{red}{121} 976144^2$	$12\ 0005991^2 + 21934000^2 = \textcolor{red}{121} 994009^2$
$1232\ 0023856^2 + 219336000^2 = \textcolor{red}{12321} 976144^2$	$1232\ 0005991^2 + 221334000^2 = \textcolor{red}{12321} 994009^2$
$123432\ 0023856^2 + 2195336000^2 = \textcolor{red}{1234321} 976144^2 \ (5.988)$	$123432\ 0005991^2 + 2215334000^2 = \textcolor{red}{1234321} 994009^2 \ (5.997)$
$0021879^2 + 1978000^2 = \textcolor{red}{1} 978121^2$	$0003996^2 + 1996000^2 = \textcolor{red}{1} 996004^2$
$12\ 0021879^2 + 21758000^2 = \textcolor{red}{121} 978121^2$	$12\ 0003996^2 + 21956000^2 = \textcolor{red}{121} 996004^2$
$1232\ 0021879^2 + 219558000^2 = \textcolor{red}{12321} 978121^2$	$1232\ 0003996^2 + 221556000^2 = \textcolor{red}{12321} 996004^2$
$123432\ 0021879^2 + 2197558000^2 = \textcolor{red}{1234321} 978121^2 \ (5.989)$	$123432\ 0003996^2 + 2217556000^2 = \textcolor{red}{1234321} 996004^2 \ (5.998)$
$0019900^2 + 1980000^2 = \textcolor{red}{1} 980100^2$	$0001999^2 + 1998000^2 = \textcolor{red}{1} 998001^2$
$12\ 0019900^2 + 21780000^2 = \textcolor{red}{121} 980100^2$	$12\ 0001999^2 + 21978000^2 = \textcolor{red}{121} 998001^2$
$1232\ 0019900^2 + 219780000^2 = \textcolor{red}{12321} 980100^2$	$1232\ 0001999^2 + 221778000^2 = \textcolor{red}{12321} 998001^2$
$123432\ 0019900^2 + 2199780000^2 = \textcolor{red}{1234321} 980100^2 \ (5.990)$	$123432\ 0001999^2 + 2219778000^2 = \textcolor{red}{1234321} 998001^2 \ (5.999)$

Based on above 999 patterns, below are some remarks:

Remark 8. From the results appearing in subsections 5.1, 5.2, 5.3 ..., 5.9 5.10, it is interesting to observe that the six digits in each case forms perfect square. See below:

$$\begin{array}{ll}
 \text{Equation (4.1)} & \Rightarrow 000001 = 1^2 \\
 \text{Equation (4.2)} & \Rightarrow 000004 = 2^2 \\
 \text{Equation (4.3)} & \Rightarrow 000009 = 3^2 \\
 \dots & \dots \\
 \dots & \dots \\
 \text{Equation (4.997)} & \Rightarrow 994009 = 997^2 \\
 \text{Equation (4.998)} & \Rightarrow 996004 = 998^2 \\
 \text{Equation (4.999)} & \Rightarrow 998001 = 999^2.
 \end{array}$$

Remark 9. In this paper, we have extended the subsections 2.1, 2.2 and 2.3. These extensions give respectively, 9, 99 and 999 results. Extending the subsections 2.4, 2.5, etc. we get the results 9999, 99999, etc. These results are not written as they are too much, and also follow the similar lines of other subsections.

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